

Convexity

Given a finite set of points $S = \{p_1, \dots, p_n\}$ in \mathbb{R}^d and a point q in \mathbb{R}^d design a Linear Program that answers the following question: Is q in the convex hull of S ?

Write a function `is_in_convex_hull(S, q)` that implements the above algorithm

Because of Carathéodory theorem, a convex hull of n points in \mathbb{R}^d can always be reduced to a convex hull of $d+1$ points. When q is in the convex hull of S , how many non-zero entries do you have in the solution? Why?