

# IMITATOR Formal Verification of Real-time Systems Under Uncertainty



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## Context: Formal Verification of Real-Time Systems

- Critical systems involve timing constants and concurrency
- Bugs can be dramatic (risk of loss of lives or huge financial loss)



⇒ Need for formal verification

Problem: what if the system constants are **uncertain** or are **not yet known**?

Solution: **parametric verification**

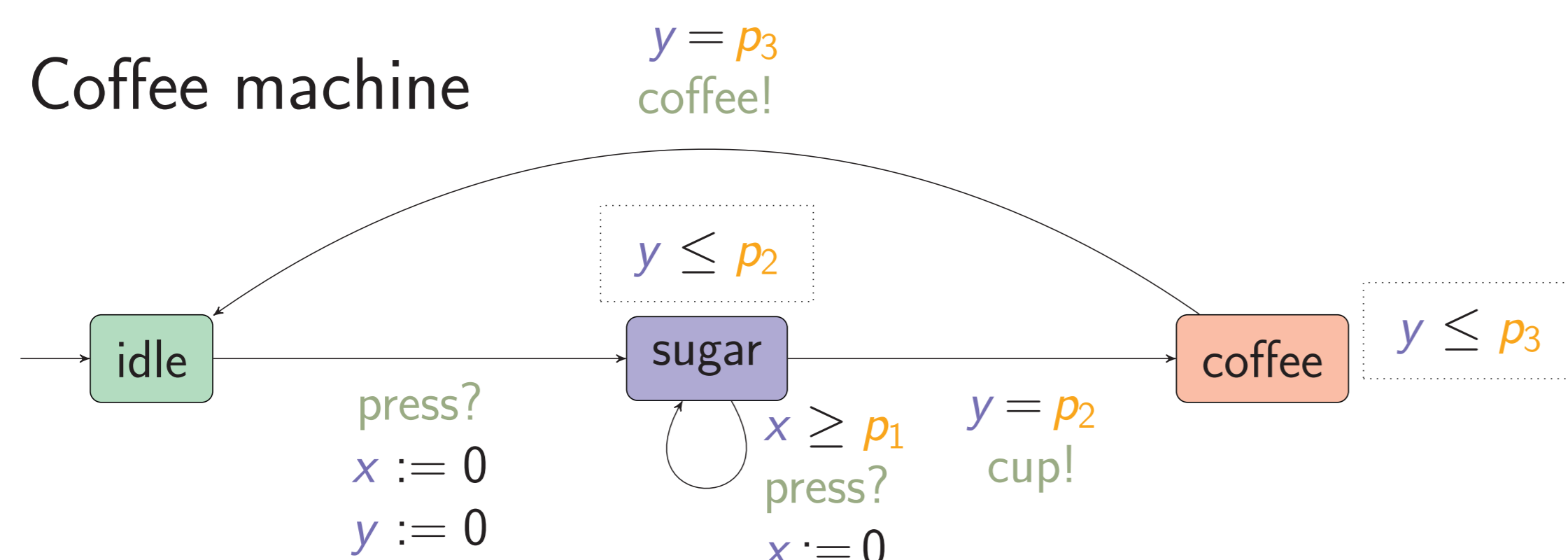
- Timing constants become **parameters**

**Objective:** derive values for these parameters ensuring the **absence of bug** (usually under the form of a set of constraints)

## Parametric Timed Automata (PTA) [Alur et al., 1993]

- Finite automata (sets of locations and actions) extended with:
  - Clocks: real-valued variables evolving linearly
  - Parameters: unknown constants

- Example: Coffee machine



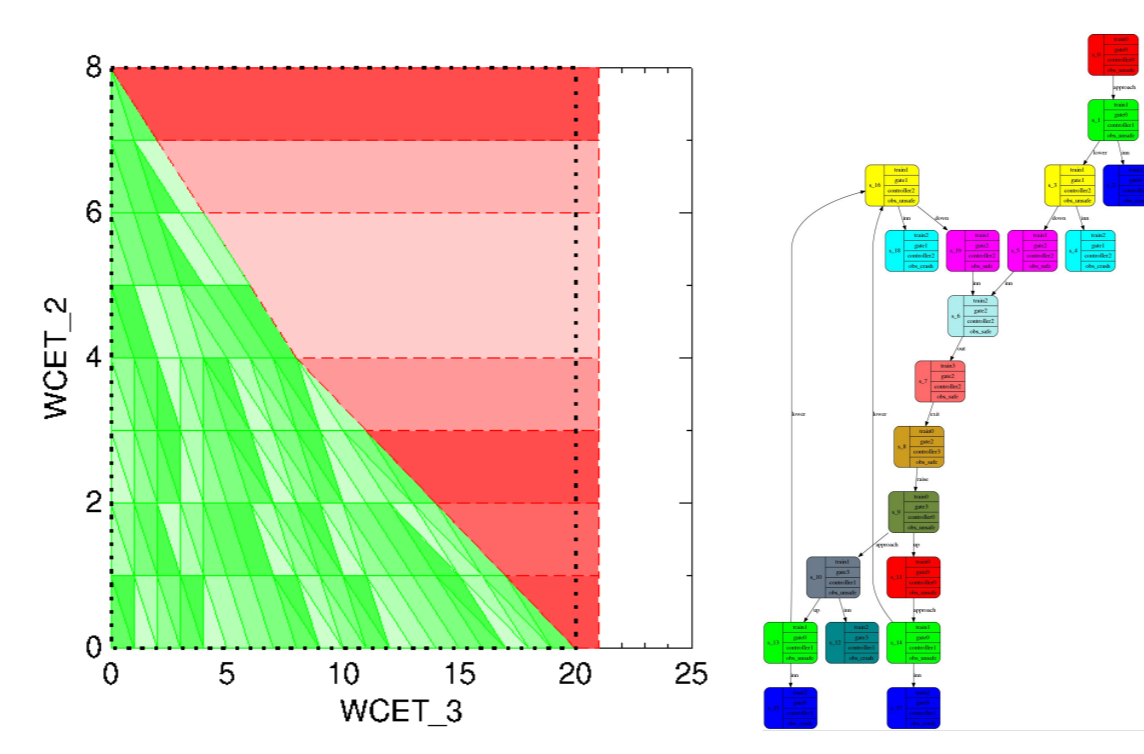
## IMITATOR: Parameter Synthesis for Critical Systems

**Input:** a real-time system modeled by a network of PTA

**Output:** a constraint over the **parameters** guaranteeing the system correctness (e.g., non-reachability of some unsafe state)

Several algorithms:

- Non-reachability synthesis
- Parametric language preservation
- Behavioral cartography



## Try IMITATOR! [André et al., 2012]

- Entirely written in OCaml
- Graphical outputs (behaviors, parameter constraints, etc.)
- Large repository of benchmarks
  - Asynchronous hardware circuits, scheduling problems, communication protocols, train controllers... and more!
- Available for free under the GNU-GPL license

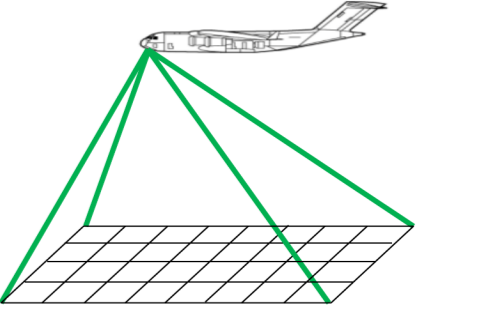
[www.imitator.fr](http://www.imitator.fr)

## What's next?

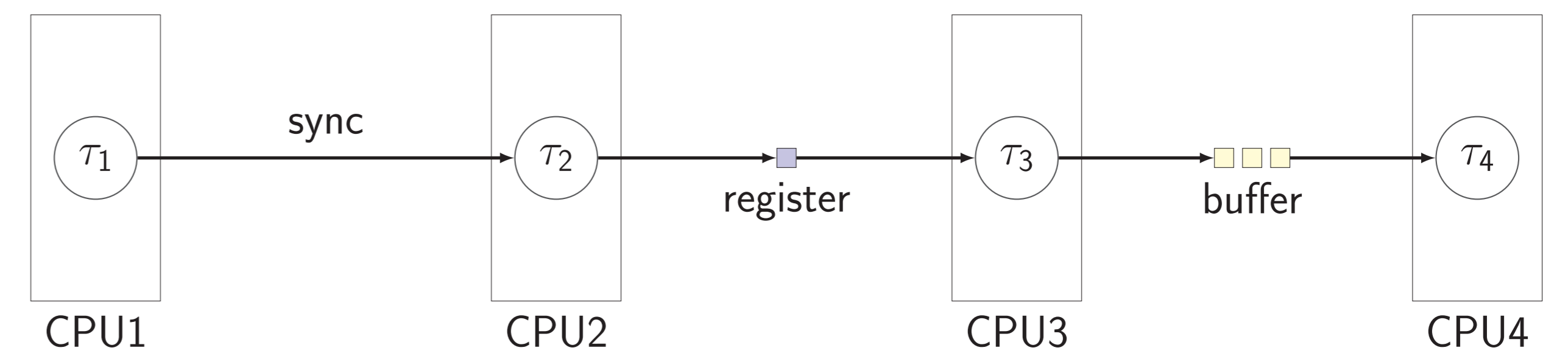
- Improved optimizations to address scalability
- Distributed and multi-core algorithms
- An input language for IMITATOR dedicated to real-time systems
  - Followed by a translation to PTA

## A Case Study: The FMTV Challenge

- A problem proposed by Thales Research & Technology for the video capture in an aerial video system (2014)



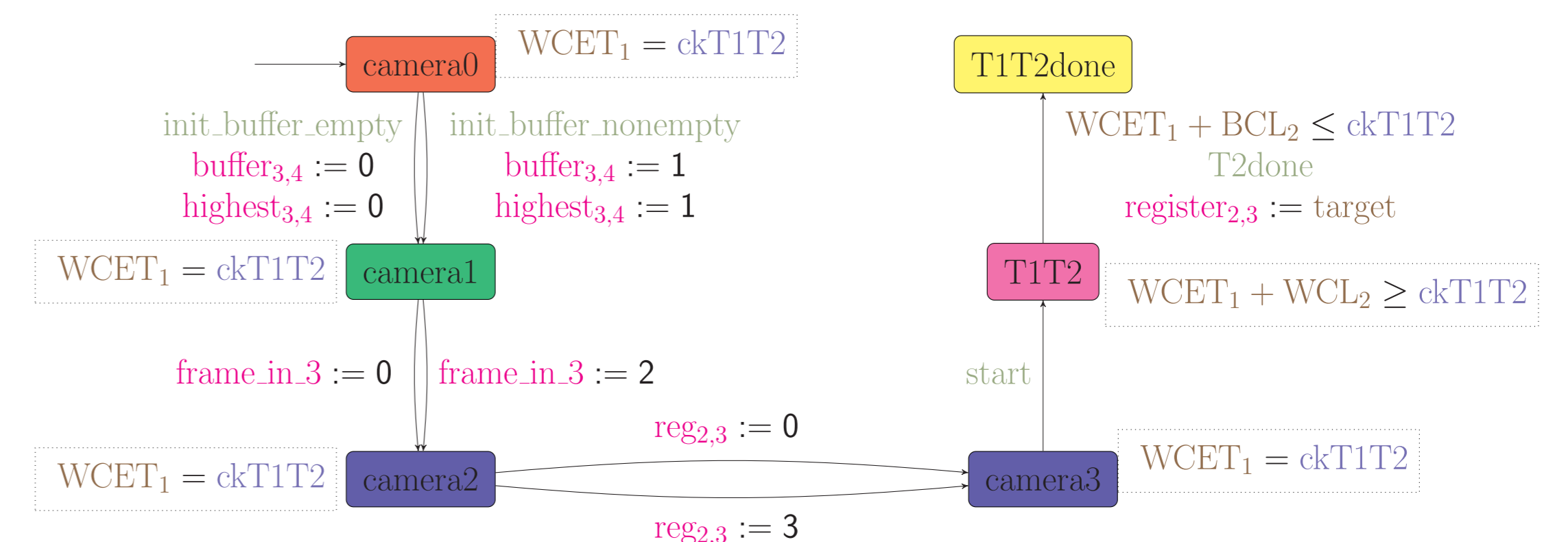
- A distributed video processing system (abstract view)



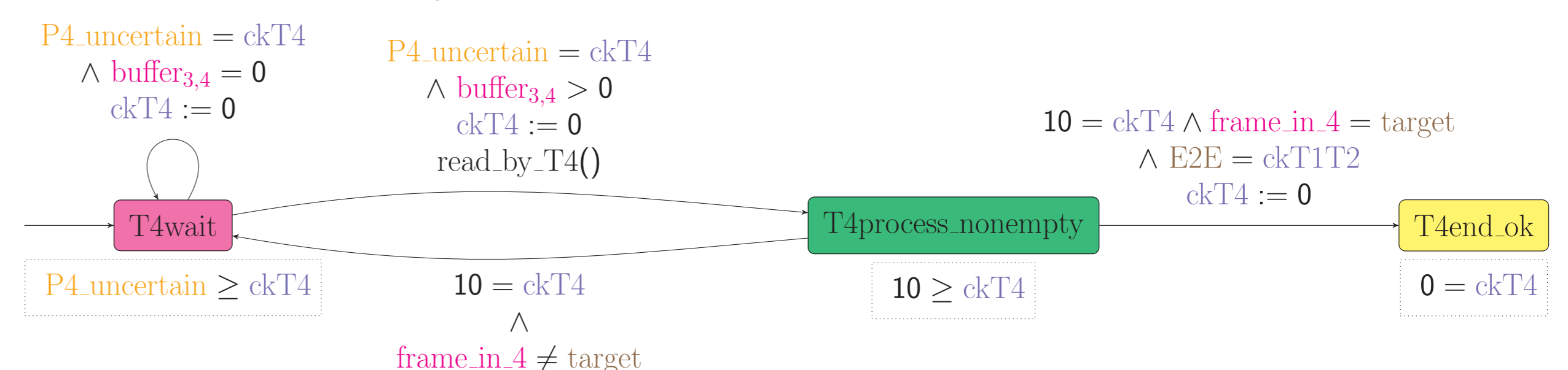
- $\tau_1$ ,  $\tau_3$  and  $\tau_4$  are periodic tasks
  - The exact value for each task's period is constant but **unknown**
    - $P1 \in [40 - 0.004 \text{ ms}, 40 + 0.004 \text{ ms}]$
    - $P3 \in [\frac{40}{3} - \frac{1}{150} \text{ ms}, \frac{40}{3} + \frac{1}{150} \text{ ms}]$
    - $P4 \in [40 - 0.004 \text{ ms}, 40 + 0.004 \text{ ms}]$
- $\tau_2$  is triggered by the completion of  $\tau_1$
- The FIFO buffer between  $\tau_3$  and  $\tau_4$  has a size  $n = 1$  or  $n = 3$
- Challenge:** find the min/max end-to-end latency that a frame may experience in this system

## Our Solution: Parametric Analysis [André et al., 2015]

- Task periods are modeled as **parameters**
  - E.g.,  $P4_{\text{uncertain}} \in [40 - 0.004 \text{ ms}, 40 + 0.004 \text{ ms}]$
- Another parameter: the end-to-end latency **E2E**
  - To focus on the **E2E** of an arbitrary frame (denoted as target)
- Some of the PTA modeling the system (for  $n = 1$ )
  - The system status is initialized to be arbitrary so that the worst-case and best-case scenarios for **E2E** will be included



- PTA model for task  $\tau_4$



- The end-to-end latency results returned by IMITATOR
  - $E2E \in [63 \text{ ms}, 145.008 \text{ ms}]$  (for  $n = 1$ )
  - $E2E \in [63 \text{ ms}, 225.016 \text{ ms}]$  (for  $n = 3$ )
- Runtime costs: 7.908 s with  $n = 1$  and 115.247 s with  $n = 3$

## Conclusion

- Solved a problem with **uncertain timing constants** using **parametric analysis**, which turned out to be an efficient option

## References

- Alur, R., Henzinger, T. A., and Vardi, M. Y. (1993). Parametric real-time reasoning. In *STOC*, pages 592–601. ACM.
- André, É., Fribourg, L., Kühne, U., and Soulat, R. (2012). IMITATOR 2.5: A tool for analyzing robustness in scheduling problems. In *FM*, volume 7436 of *Lecture Notes in Computer Science*, pages 33–36. Springer.
- André, É., Lipari, G., and Sun, Y. (2015). Verification of two real-time systems using parametric timed automata. In *WATERS*.