SynCoP 2015

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Enhanced Distributed Behavioral Cartography of Parametric Timed Automata

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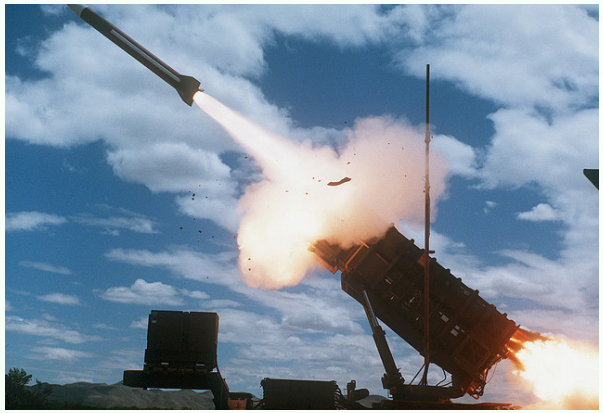
Context: Formal Verification of Timed Systems (1/3)

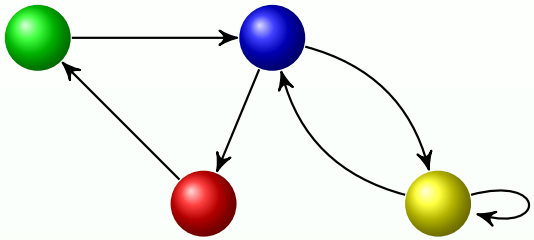
- Need for early bug detection
  - Bugs discovered when final testing: expensive

  ⇝ Need for a thorough modeling and verification phase



Context: Formal Verification of Timed Systems (2/3)

- Use formal methods



A model of the system

A property to be satisfied

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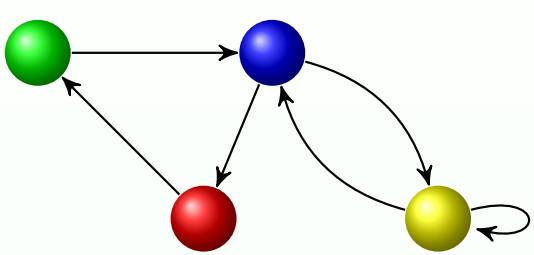

$\stackrel{?}{\models}$

A model of the system

A property to be satisfied

- Question: does the model of the system satisfy the property?

Context: Formal Verification of Timed Systems (2/3)

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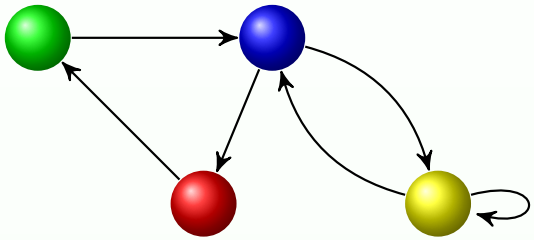


$\models ?$

$AG\neg$ 

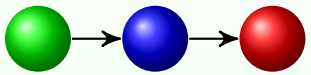
A model of the system

A property to be satisfied

- Question: does the model of the system satisfy the property?

Yes

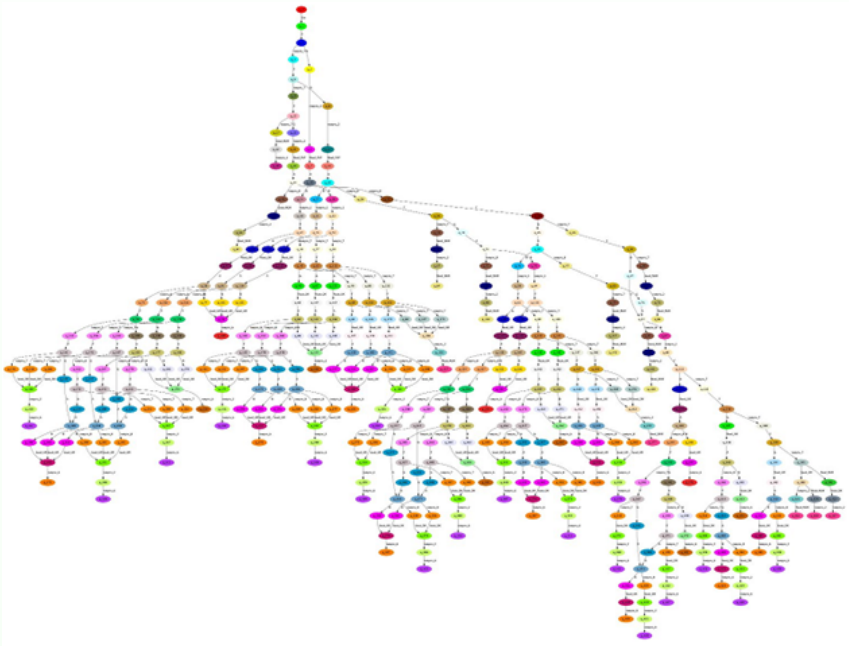
No



Counterexample

Context: Formal Verification of Timed Systems (3/3)

- Problem: But state space explosion is always painful! Especially real-time systems.



Context: Formal Verification of Timed Systems (3/3)

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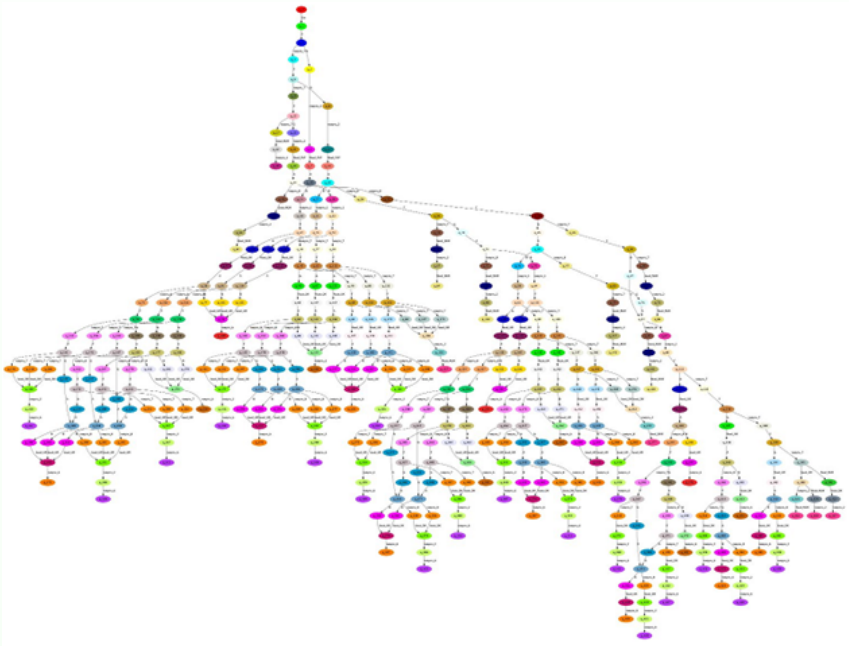

- One solution:
  - Extend to distributed fashion

Outline

1 Behavioral Cartography of Timed Automata

2 Distributing BC

3 State of The Art: Previous Distributed BC Algorithms

4 Enhanced Distributed BC Algorithm

5 Experimental Validation

6 Conclusion and Perspectives

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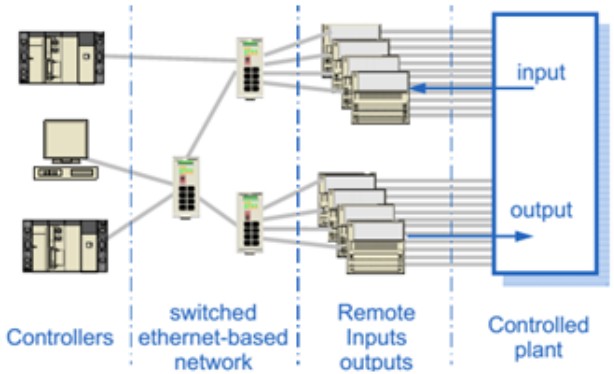
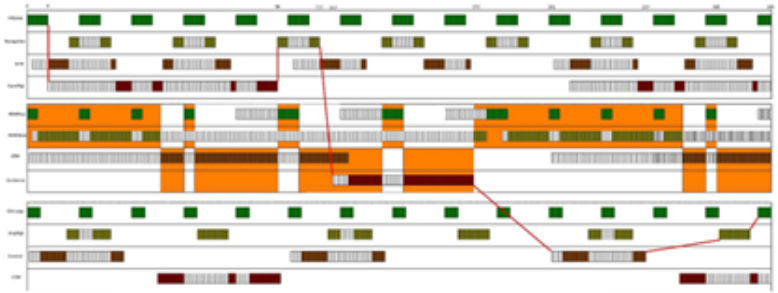
Parametric Timed Automata (PTA)

A formalism to model and verify concurrent real-time systems

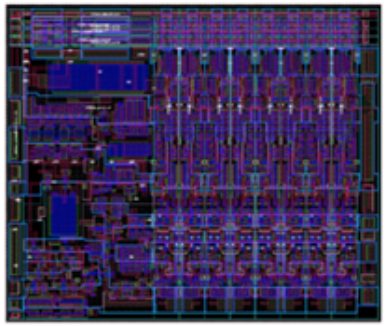
[Alur et al., 1993]



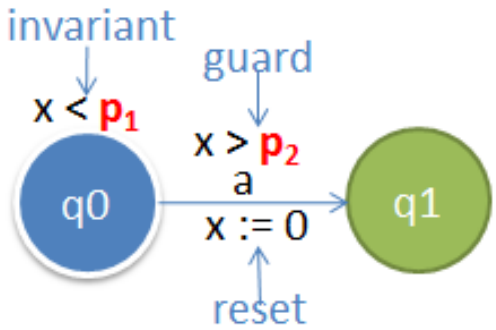
Communication protocols



Processor Scheduling



Asynchronous Circuits

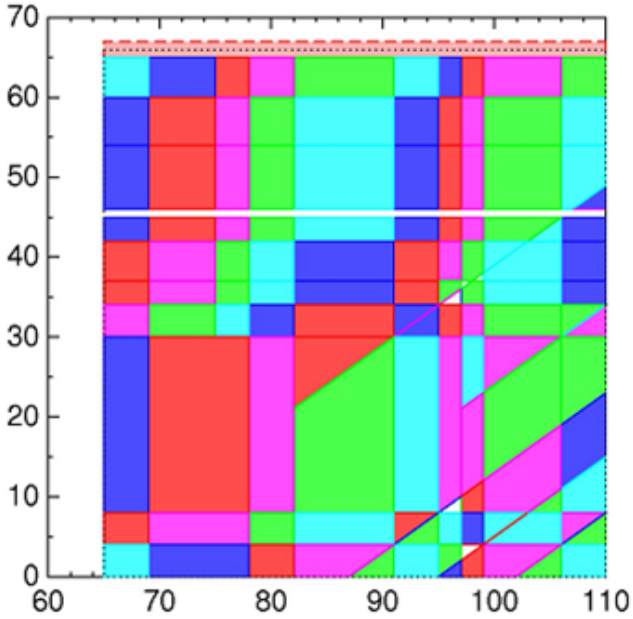


Parametric Timed Automata

x: Clock

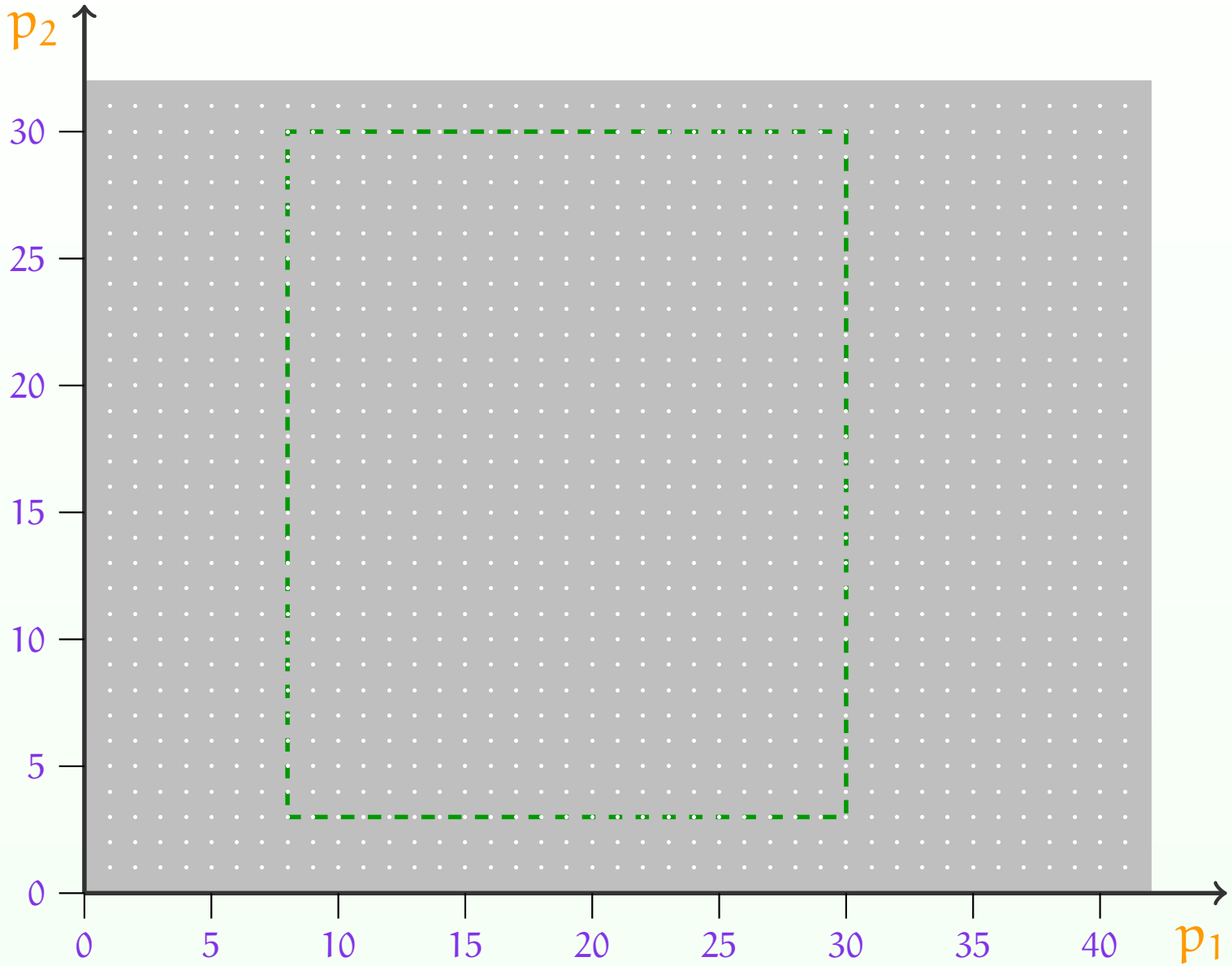
p: Parameters allow to represent unknown values (e.g., a transmission delay or a timeout)

Behavioral Cartography (BC)



- BC: Partitions a parameter domain into tiles, i.e., parametric zones of uniform behavior [André and Fribourg, 2010]
- Method: enumerate integer points and generate a tile using an existing algorithm (the inverse method IM)
- All parameter valuations in a tile have the same possible behaviors (same "trace set"), and verify the same linear-time properties

Behavioral Cartography: Example



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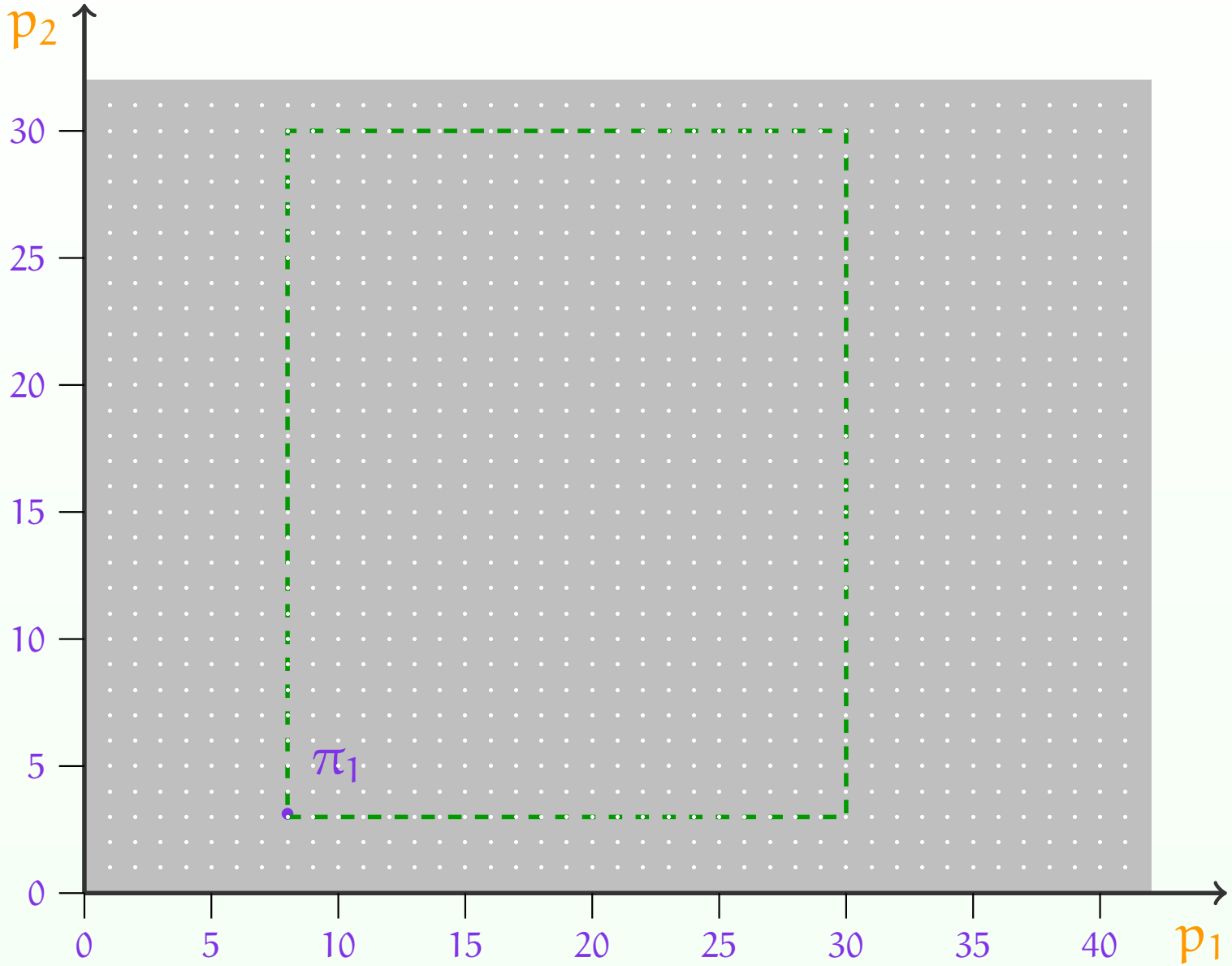

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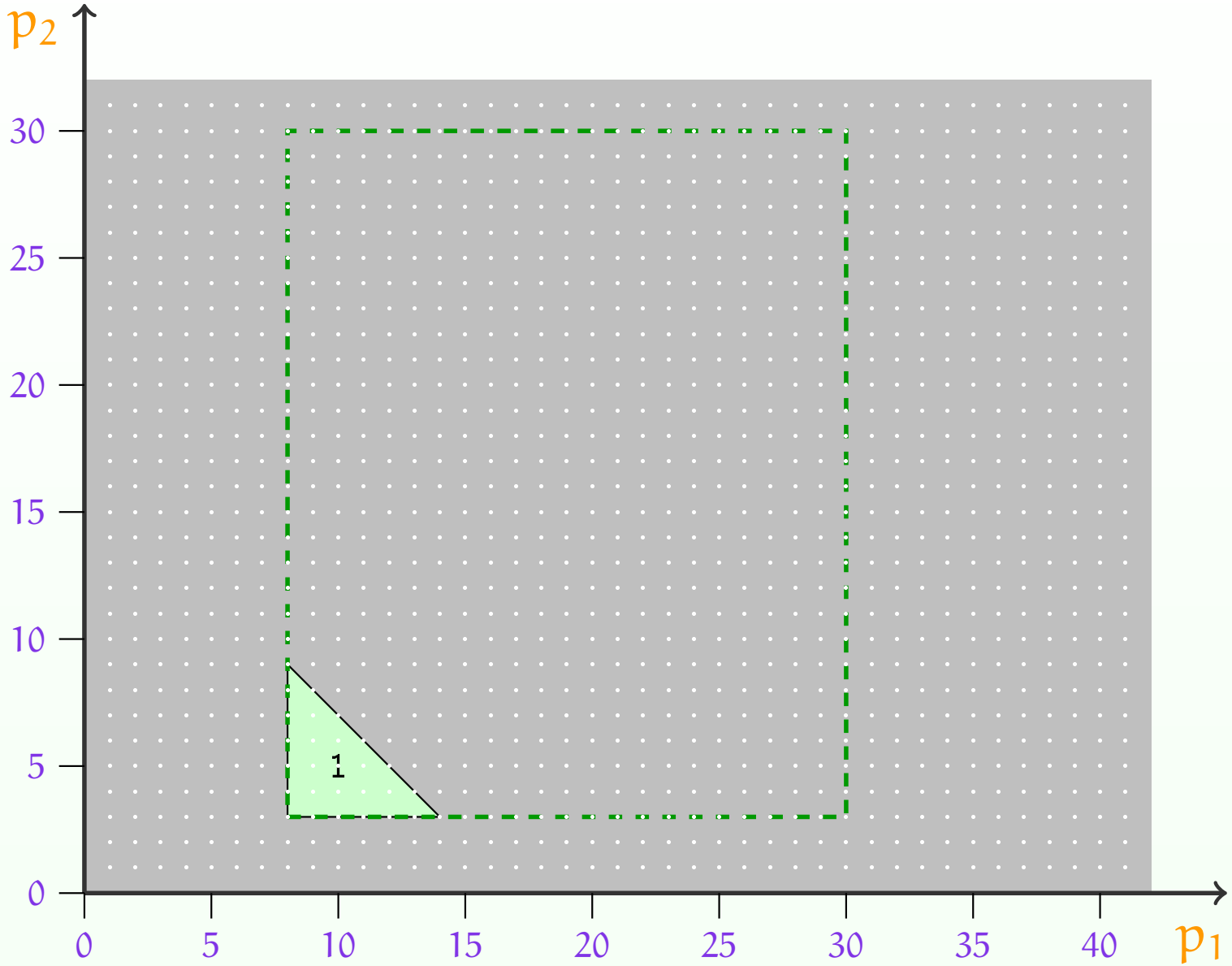

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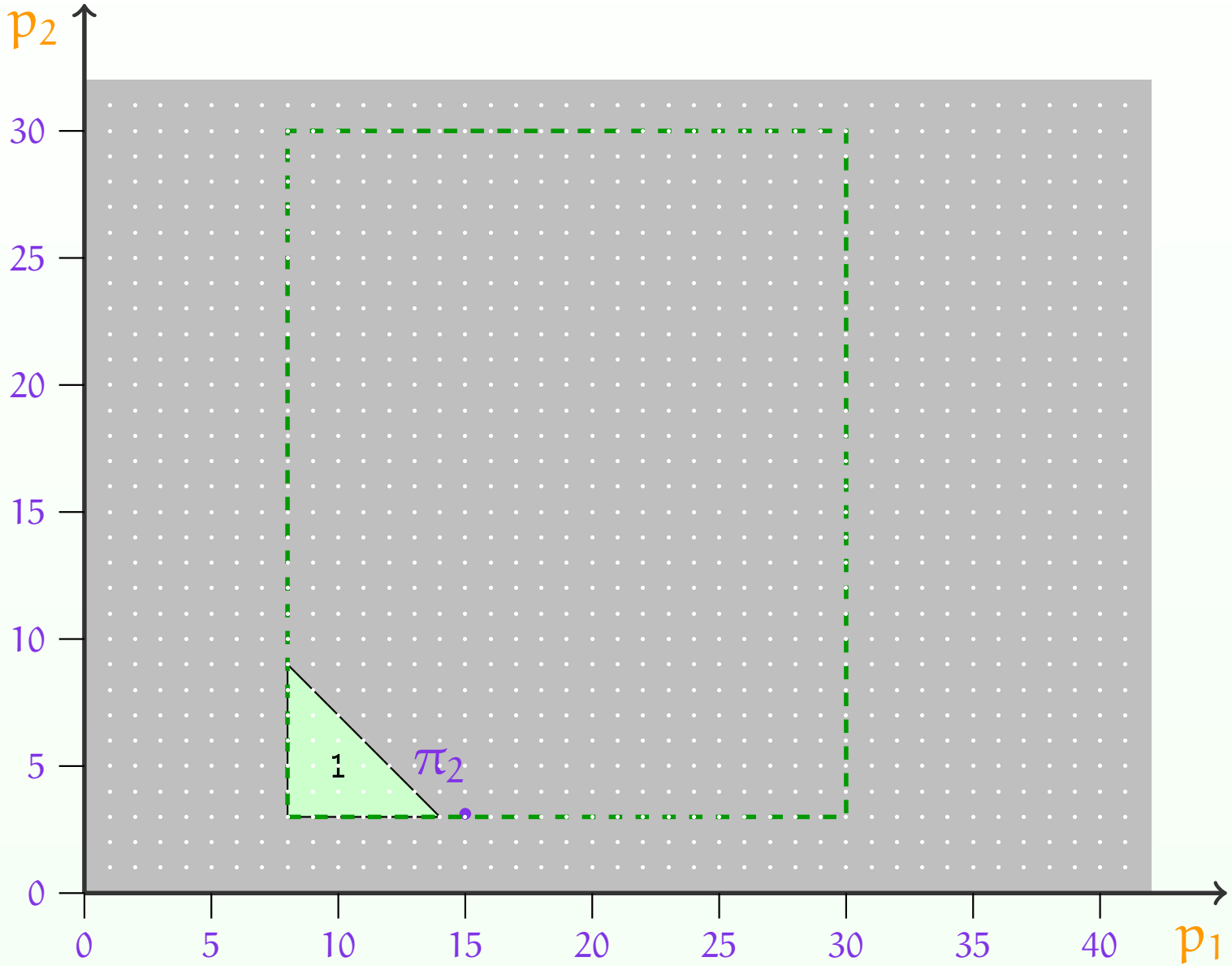

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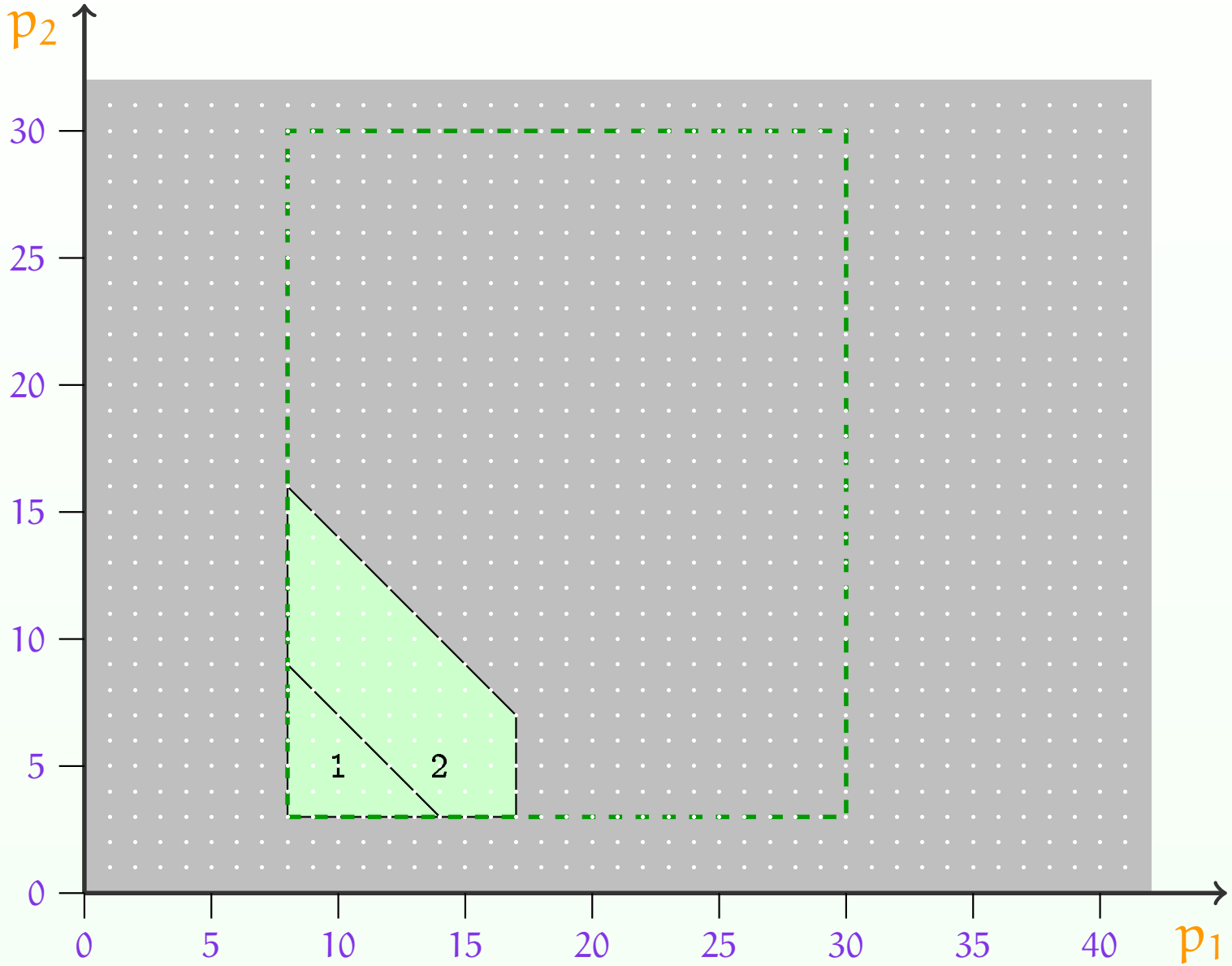

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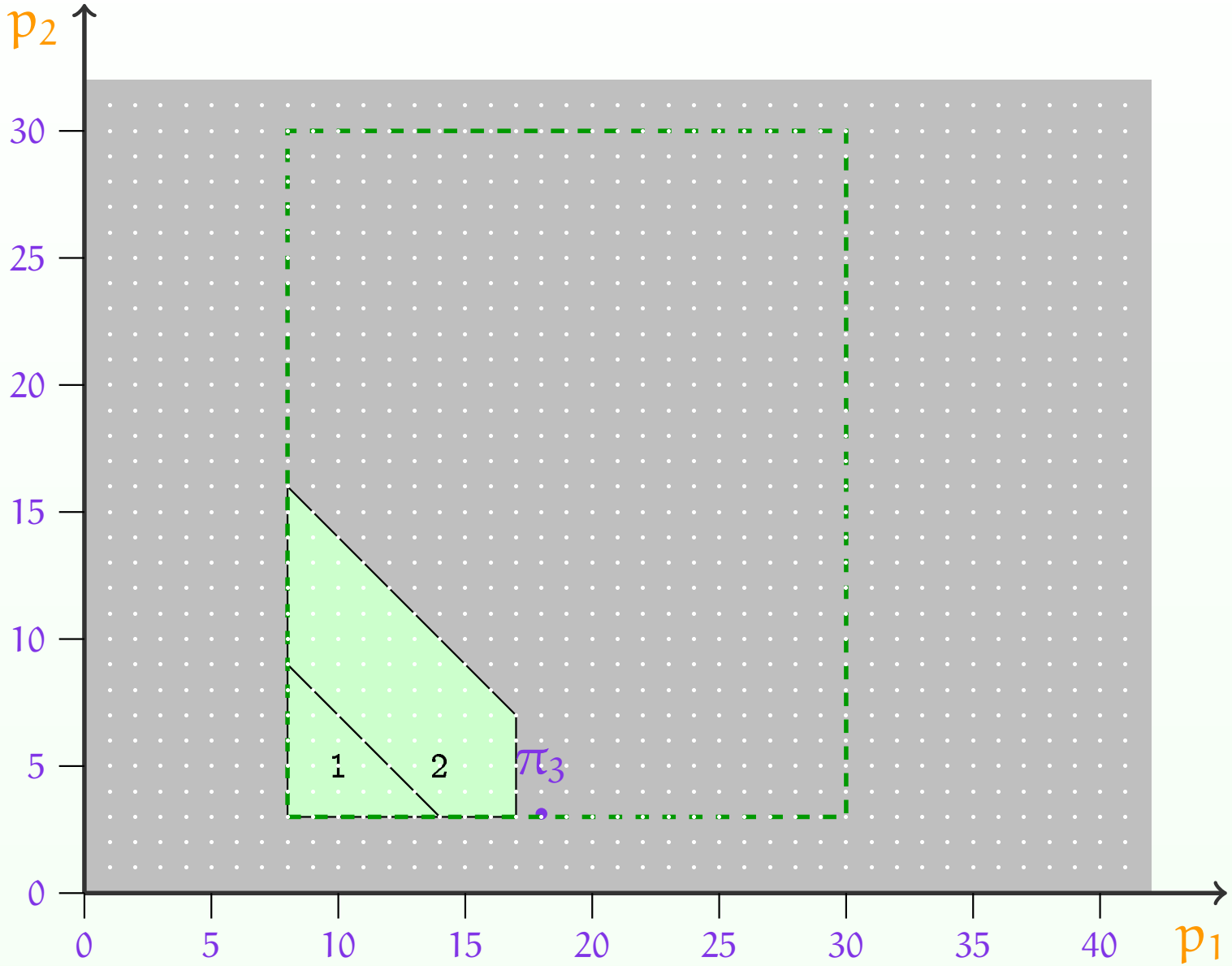

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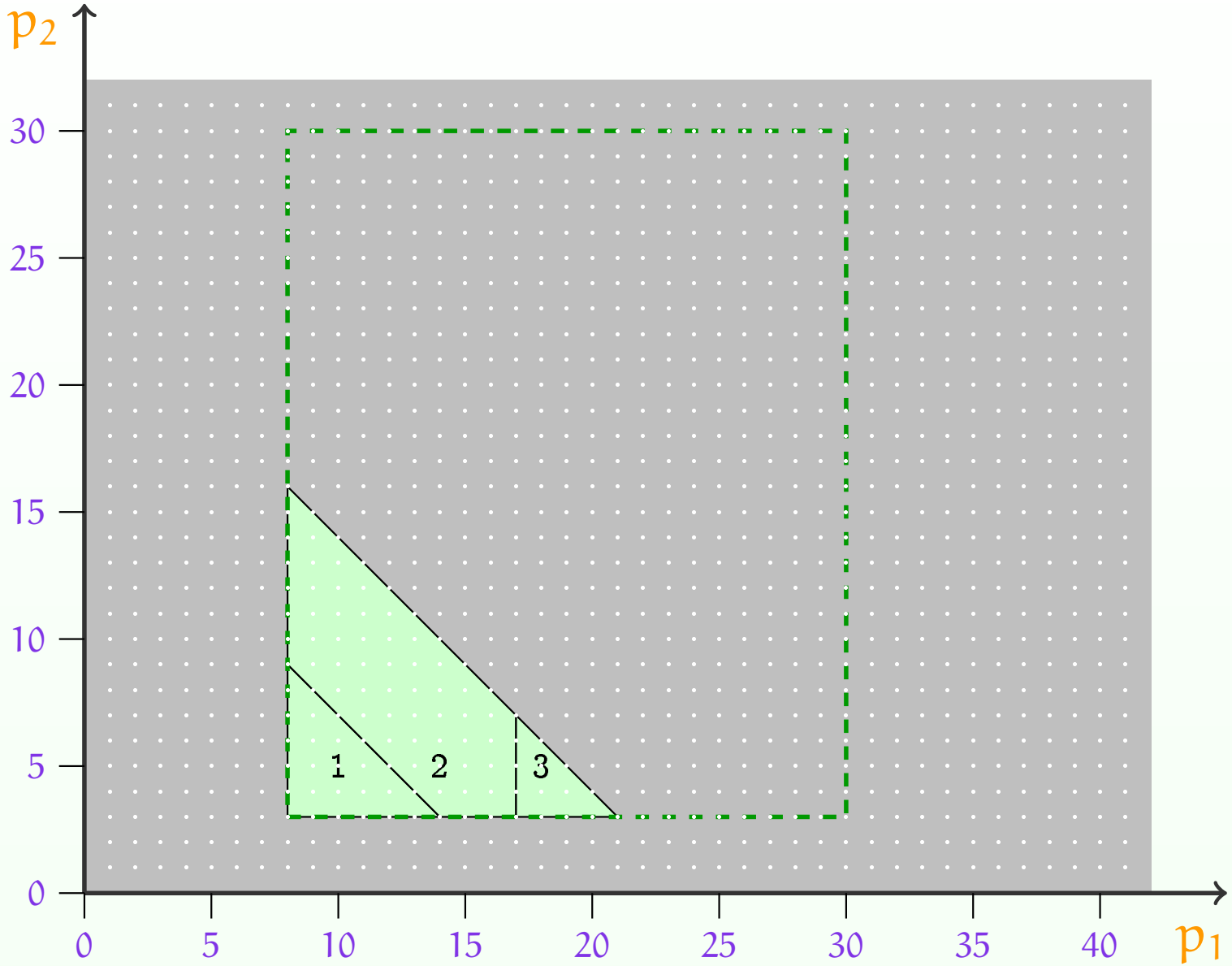

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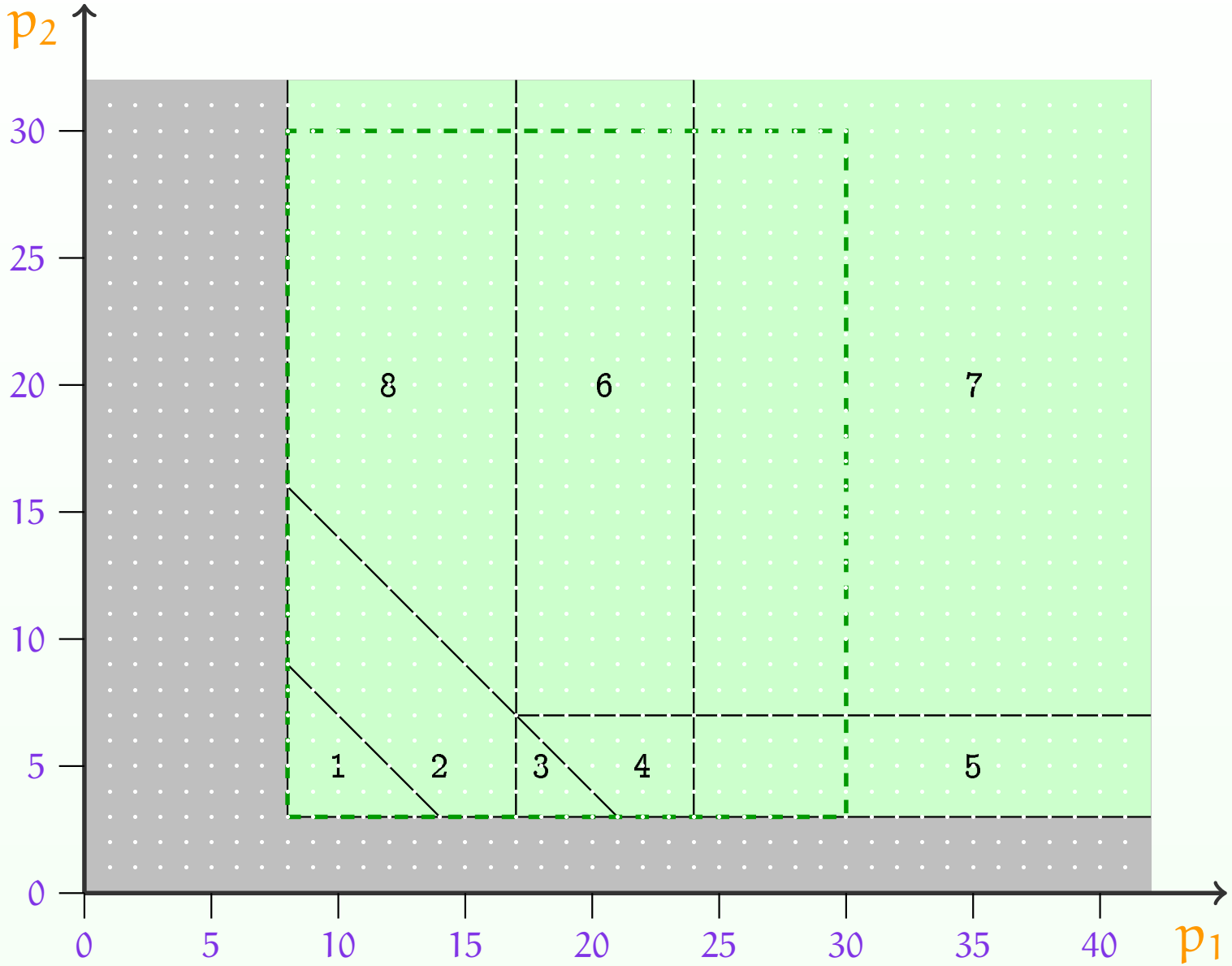
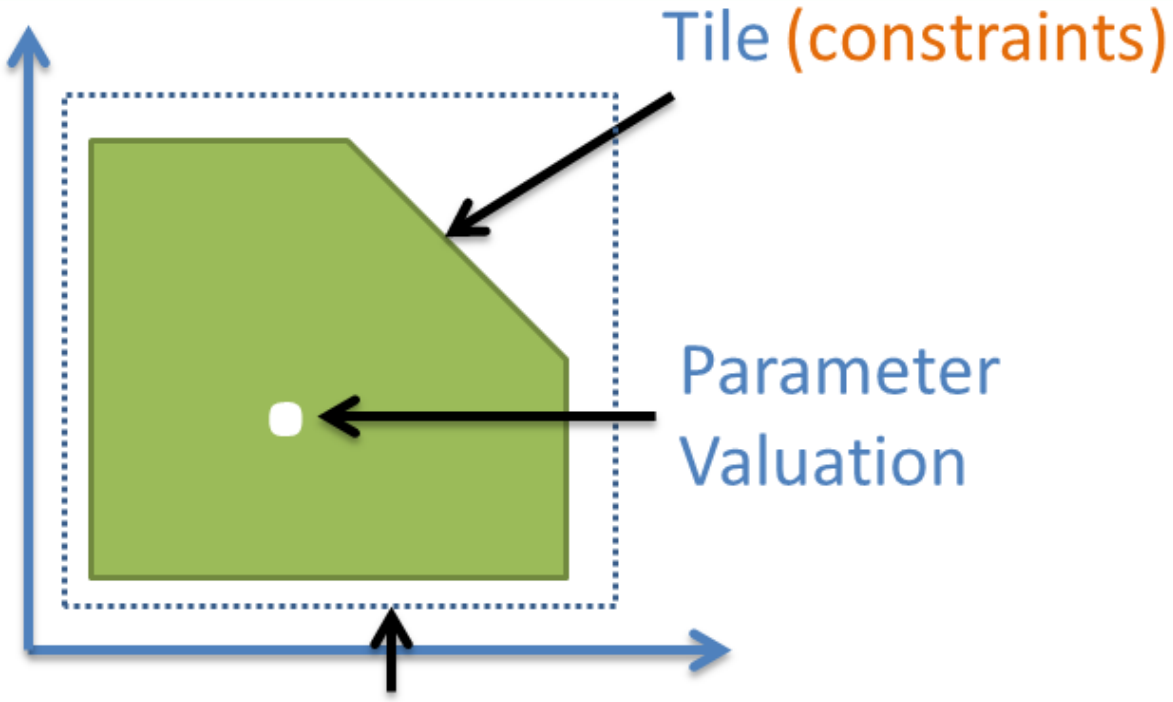
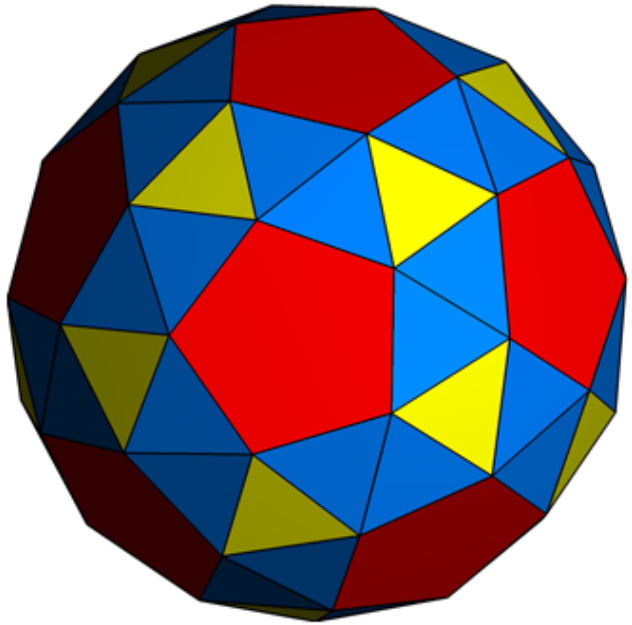


An n-dimension analysis



Tile
(2 dimensions)



Tile
- Polyhedron
(n dimensions)

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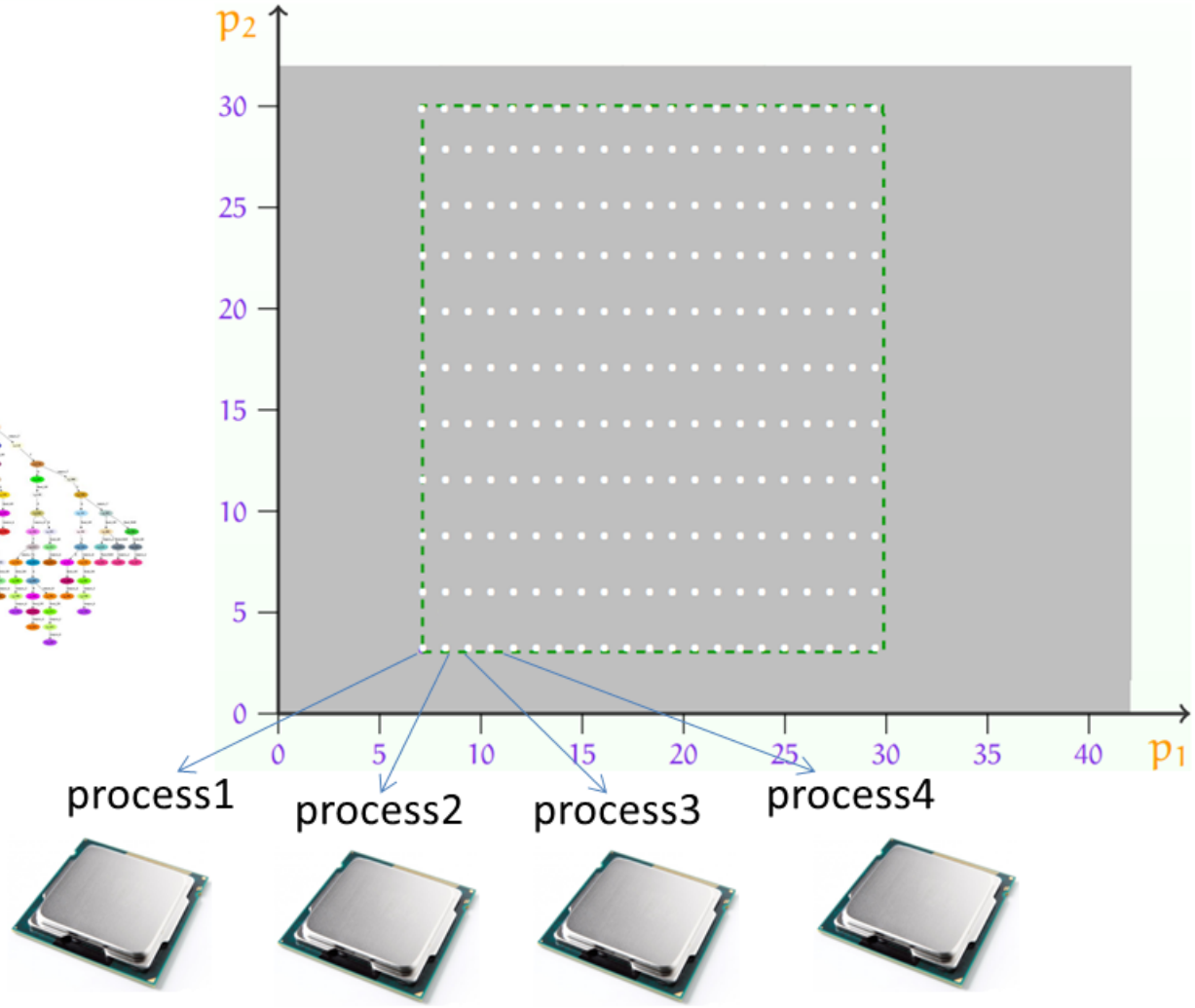
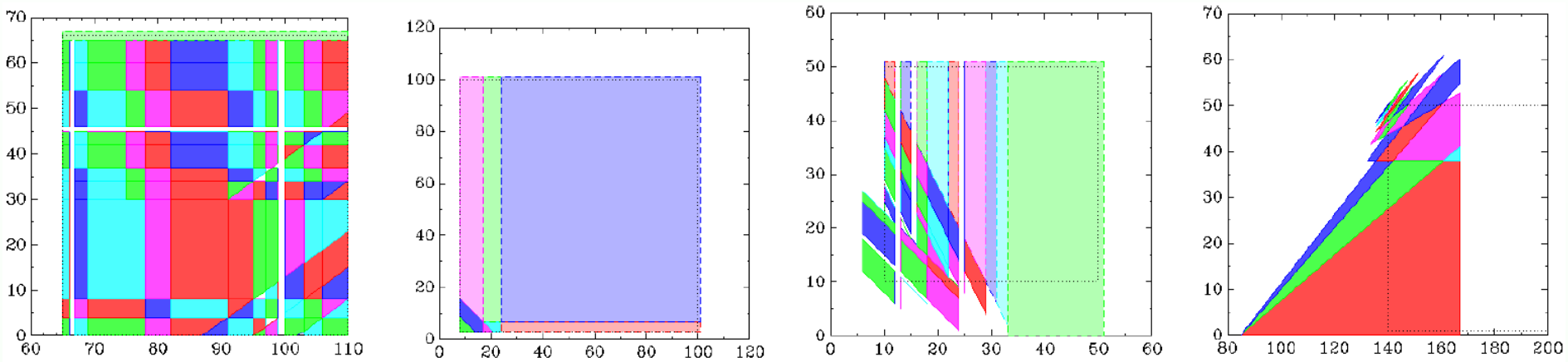
Distributing BC

Example of a trace set output by IMITATOR



- Problem: BC is very slow! (up to several hours)
- Goal: distribute BC on a cluster to increase the computation speed

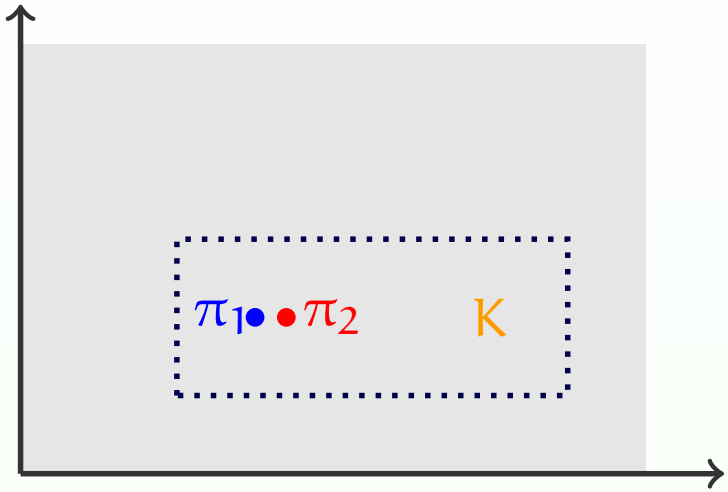
Distributing BC: Problem 1



Problem 1: the general shape of the Cartography is unknown in general

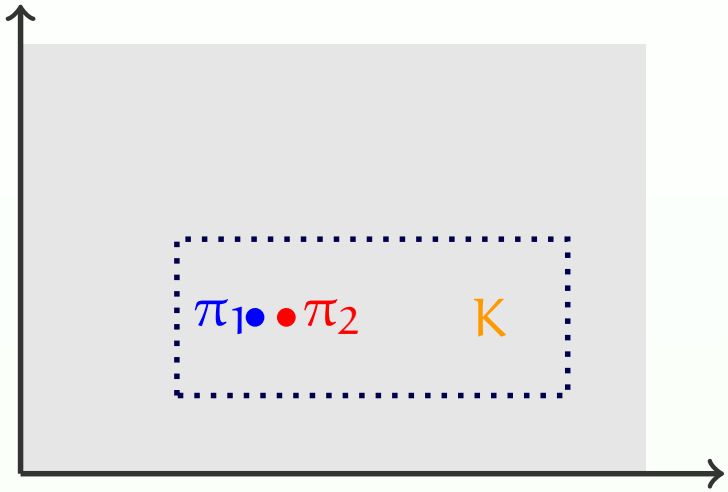
And the time to compute each tile varies a lot (more or less complex trace sets)

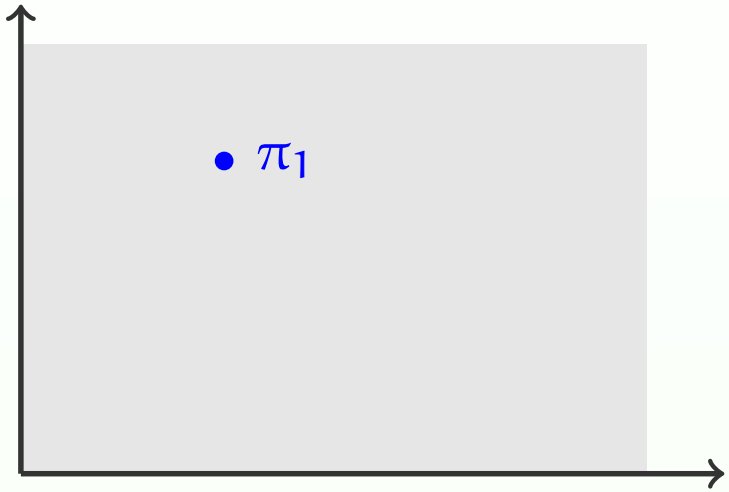
Distributing BC: Problems 2 and 3



Problem 2: two close points will very probably yield the same tile (loss of efficiency)

Distributing BC: Problems 2 and 3





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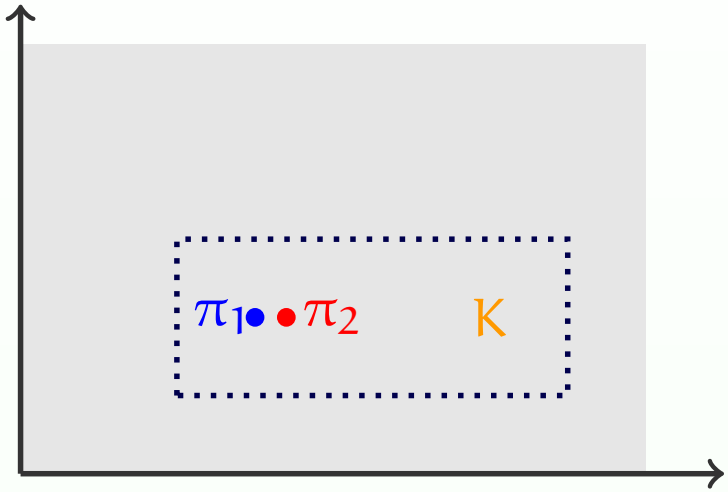

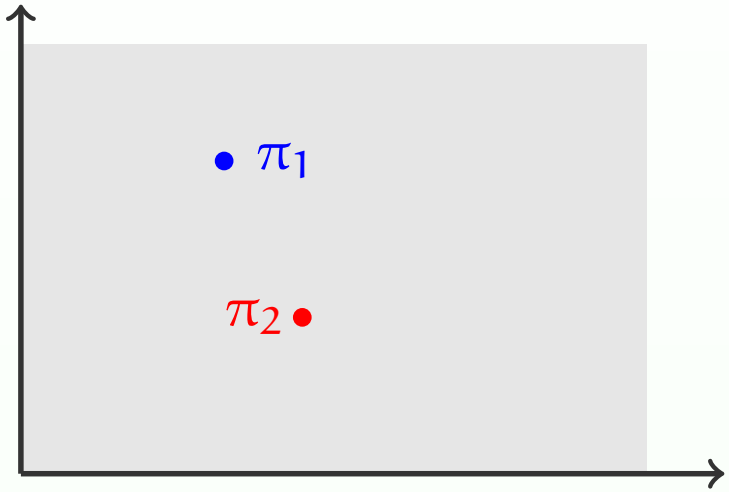

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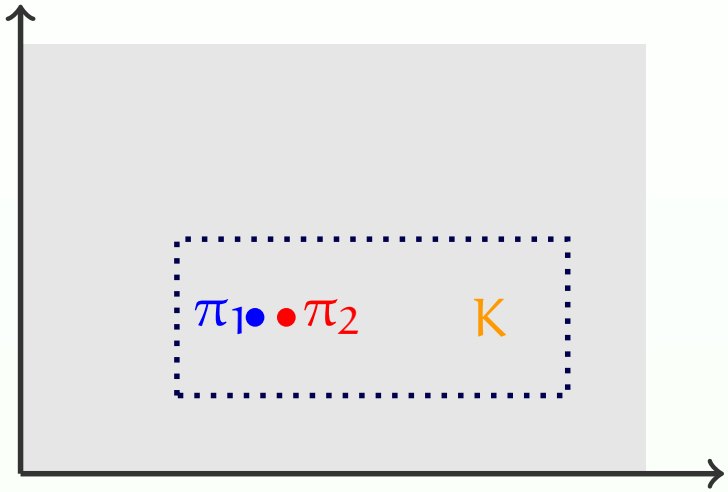

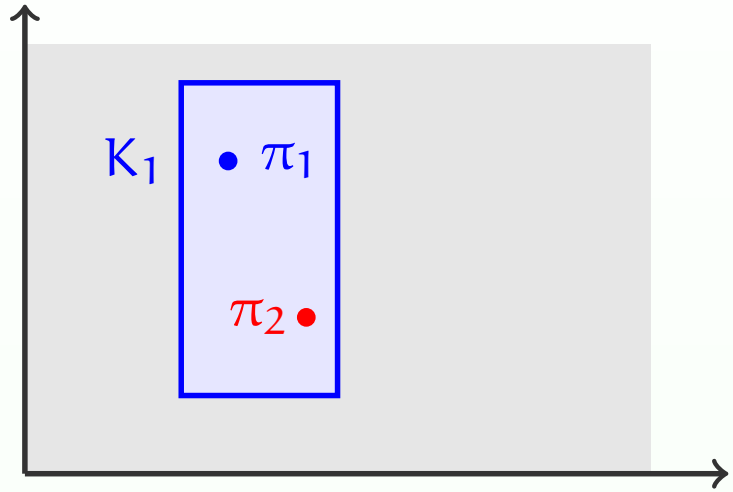

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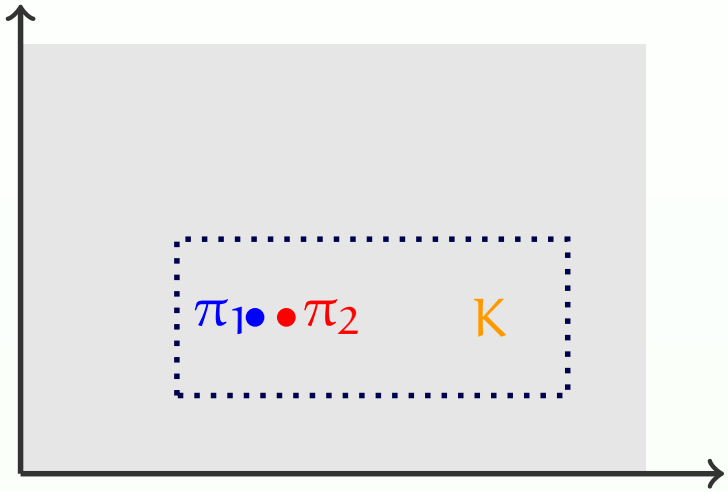

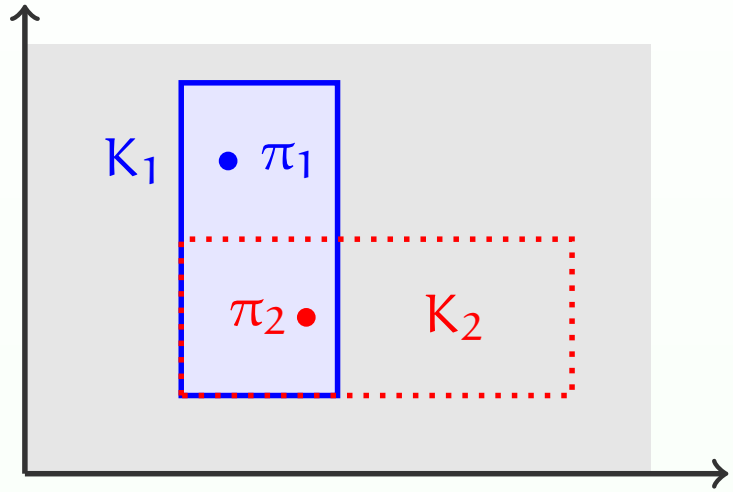

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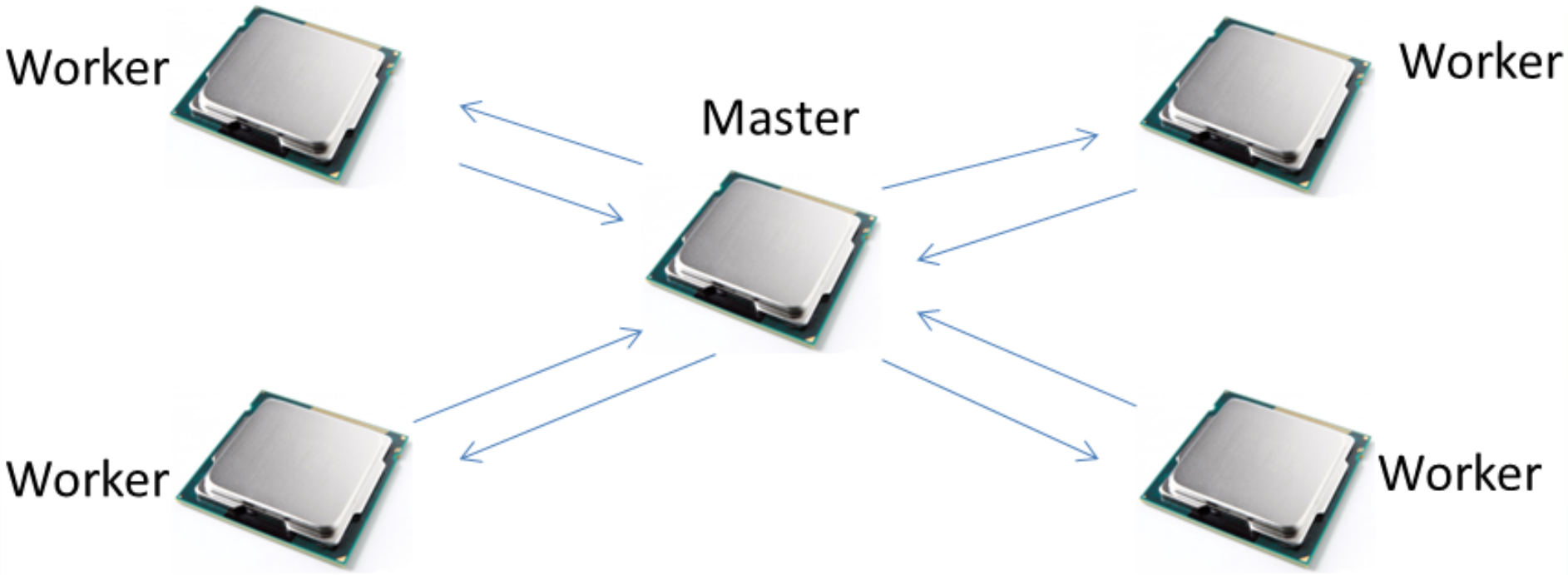
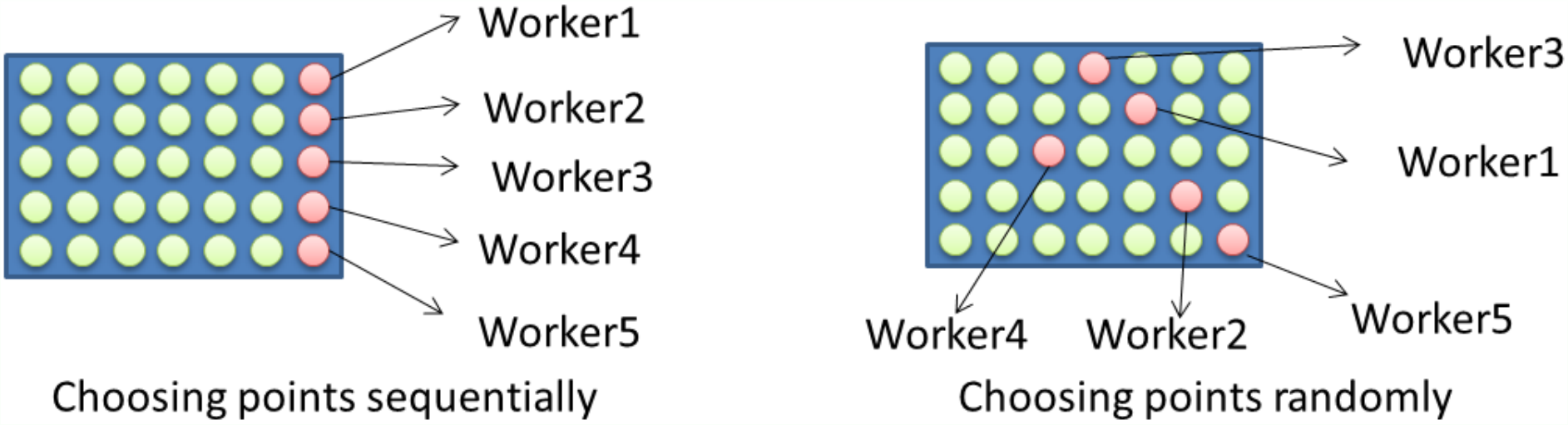
Master Workers Scheme



Traditional Master-Worker communication scheme: [André, Coti, Evangelista, 2014]

- Workers: ask the master for a point, and send the result ("tiles") to the master
- Master: is responsible for smart repartition of data between the workers

Previous Point-based BC Algorithms



Point-based BC algorithms:

- Sequential: each point is sent to a worker sequentially
- Random: points selected randomly, then switches to Sequential
- Shuffle: similar to the Sequential, but the difference is that master must statically compute the list of all points, then shuffle all points, then store them in array (new)

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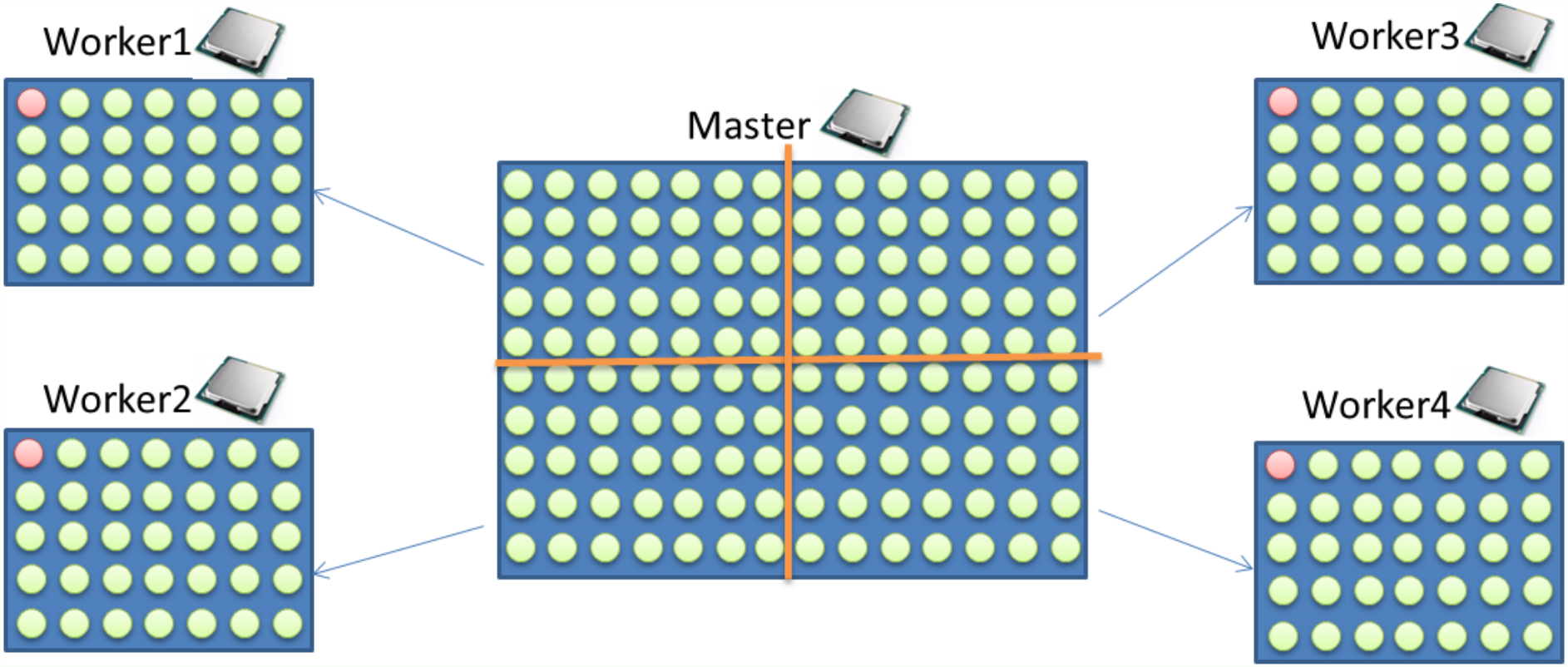
Subpart-based BC Algorithm Scheme

"Domain decomposition" scheme

- Master
  1. initially splits the parameter domain into subparts and send them to the workers
     - Subpart: a subdomain of the parameter domain
  2. when a worker has completed its subpart, the master splits another subpart, and sends it to the idle worker

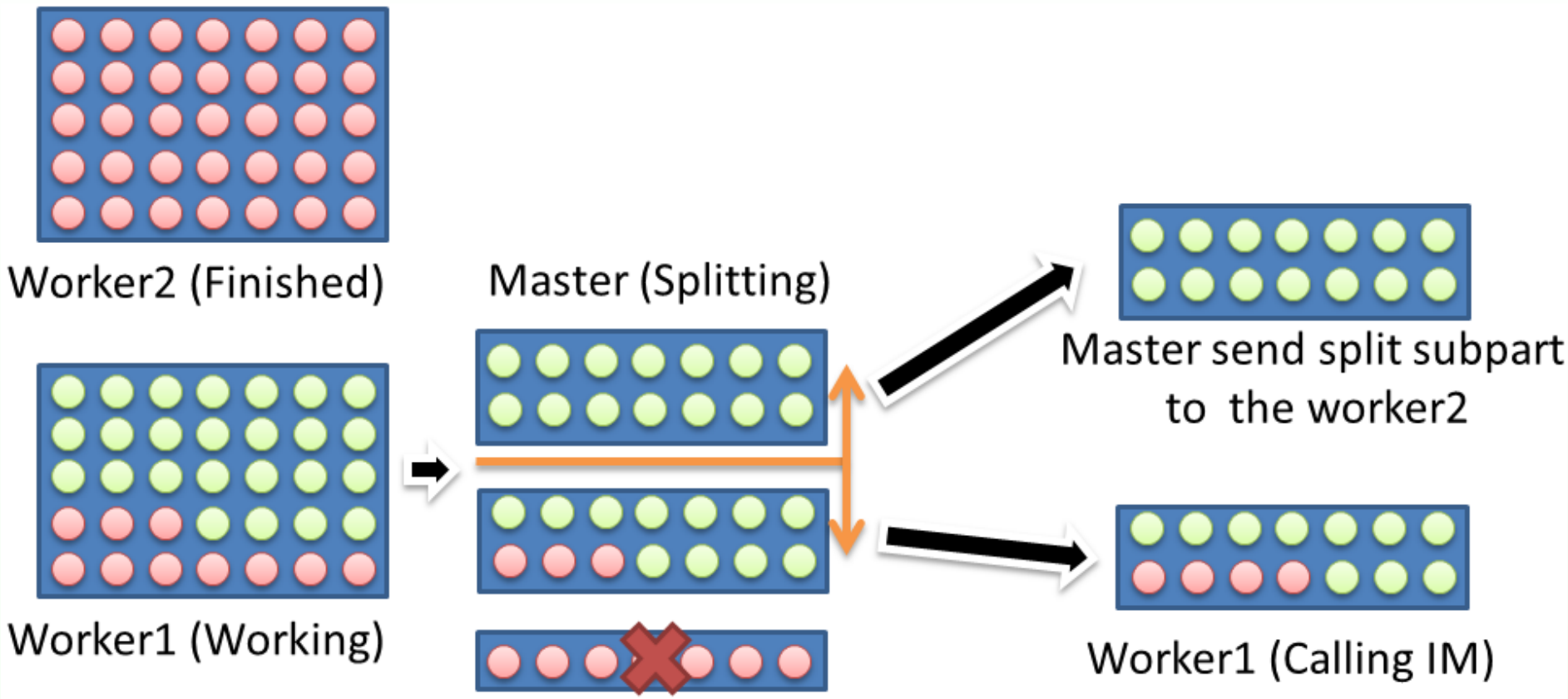
- Workers
  1. receives the subpart from the master
  2. calls IM on the points of this subpart
  3. sends the results (tiles) back to the master
  4. asks for more work

Subpart-based Distribution Scheme: Initial Splitting



- Solved Problem 2! (prevent to choose close points)
- Prevent bottleneck phenomenon at the master side
  - Master only responsible for gathering tiles and splitting subparts

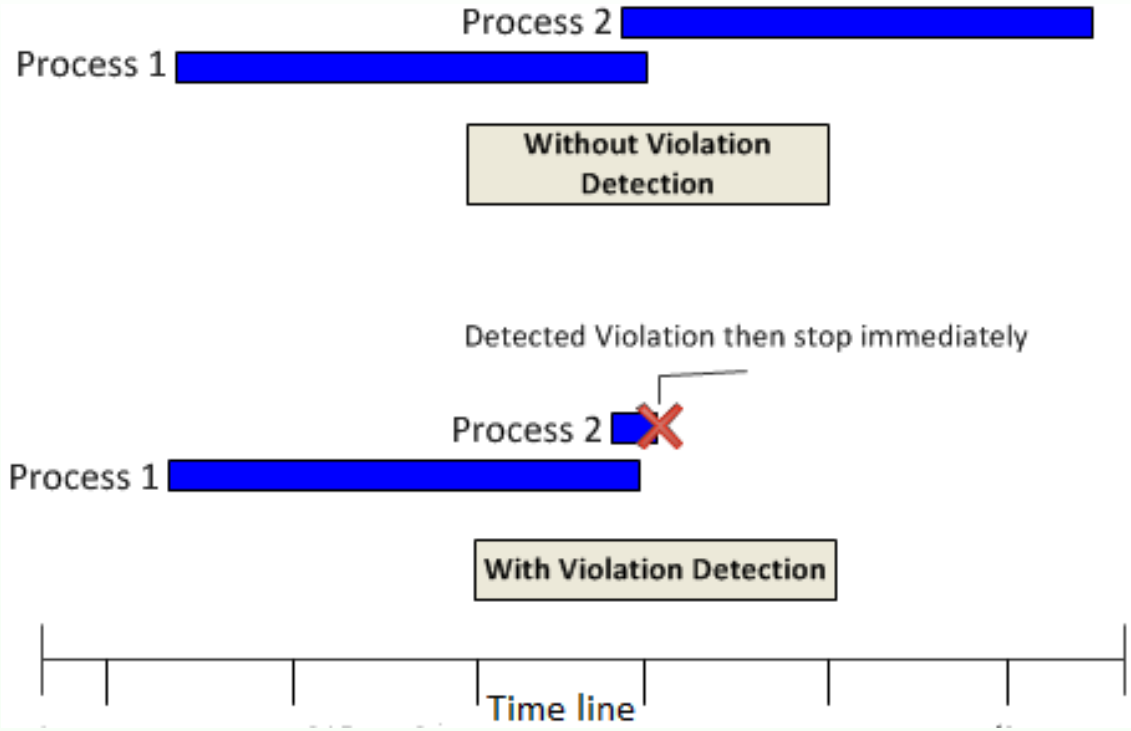
Subpart-based Distribution Scheme: Dynamic Splitting

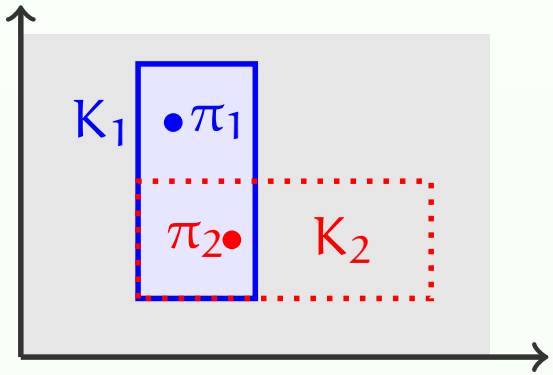


- Master can balance workload between workers

Violation Detection – Heuristic (1/2)

Violation detection: a mechanism to detect and stop process which is calling point in the covered tile.





Violation Detection – Heuristic (2/2)

- Solution proposed: stop immediately when the reference point ("π_2") is covered by another tile ("C_1")
- Workers have ability to self-detects violation
- Is an answer to the previous Problem 3 ("what to do when a point is covered by another tile?")
- Can be used for all previous algorithms

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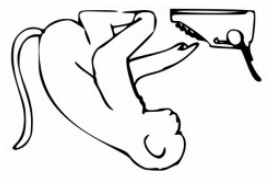

- IMITATOR [André, Fribourg, Kühne, Soulat, 2012]
  - 26,000 lines of OCaml code
    - Including $> 3,000$ lines for the distribution algorithms
  - Relies on the PPL library for operations on polyhedra [Bagnara et al., 2008]
  - Available under the GNU-GPL license at `www.imitator.fr`
  - Stable version (2.6.2) integrated in *CosyVerif* [AHHKLLP13]

- Distributed version of IMITATOR relying on MPI
  - Using the OcamlMPI library for passing messages between Master and Workers

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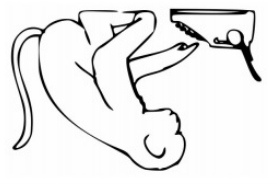

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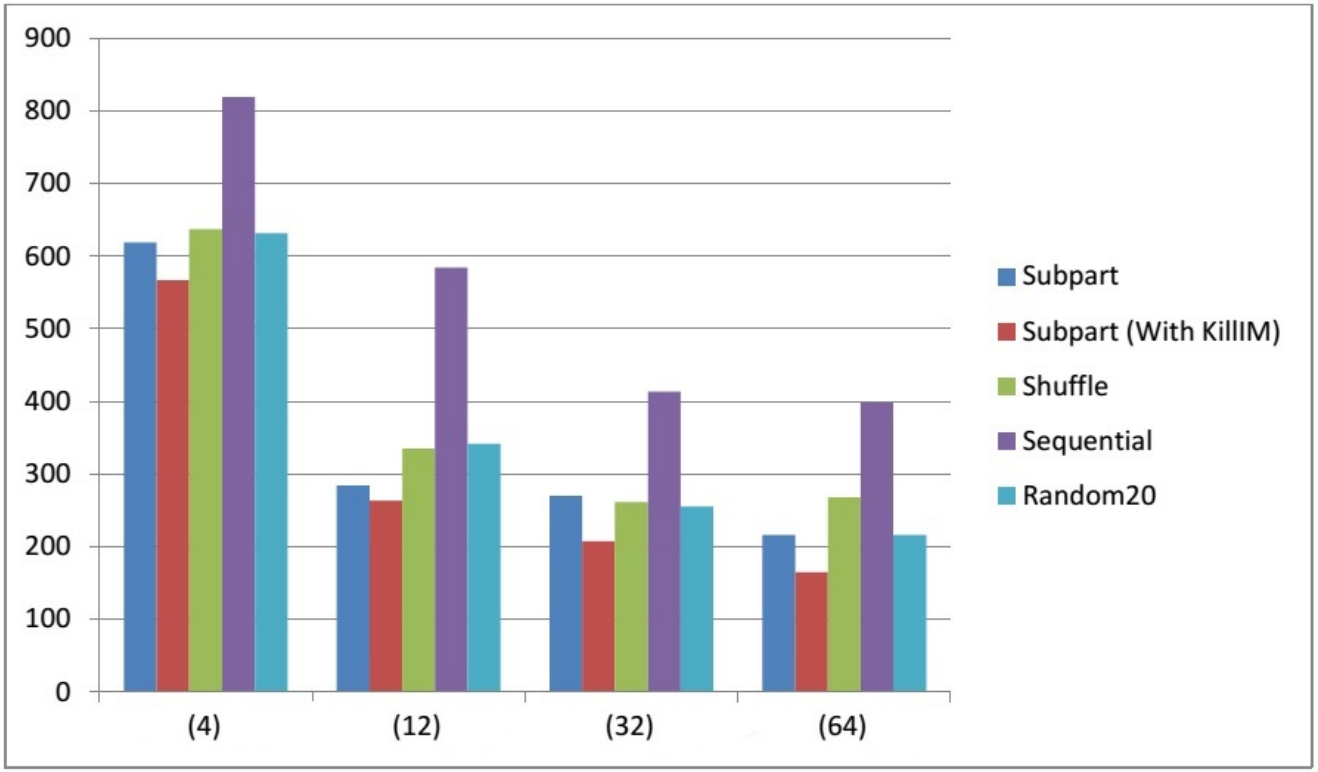
    ...in which we found a bug!

Experimental Validation

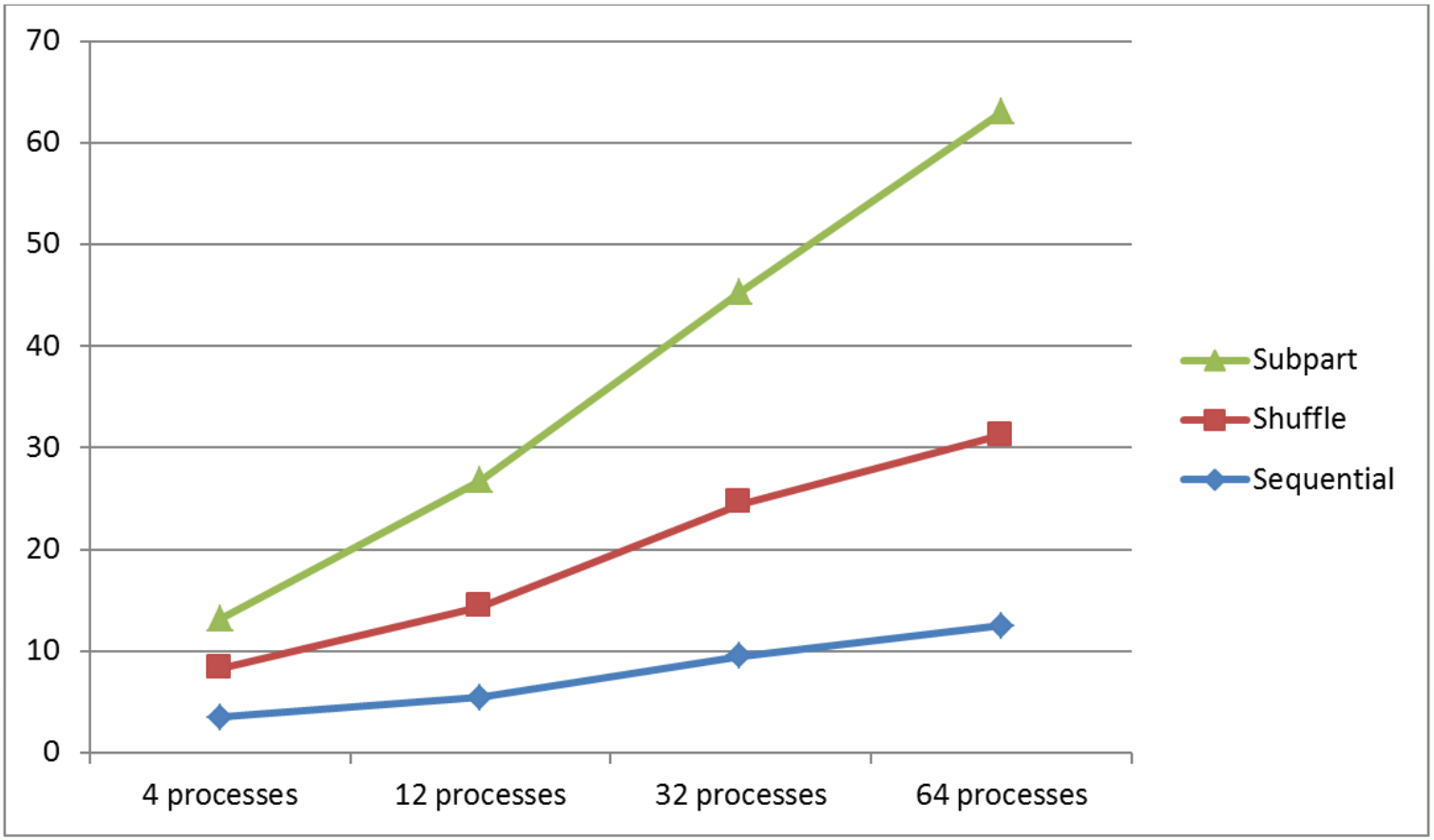
Experimental conducted on a real cluster ("Magi") in the Paris 13 University

Average computation time for a set of case studies, for 4/12/32/64 nodes:



Our new algorithm always outperforms existing algorithms

SpeedUp Chart Diagram

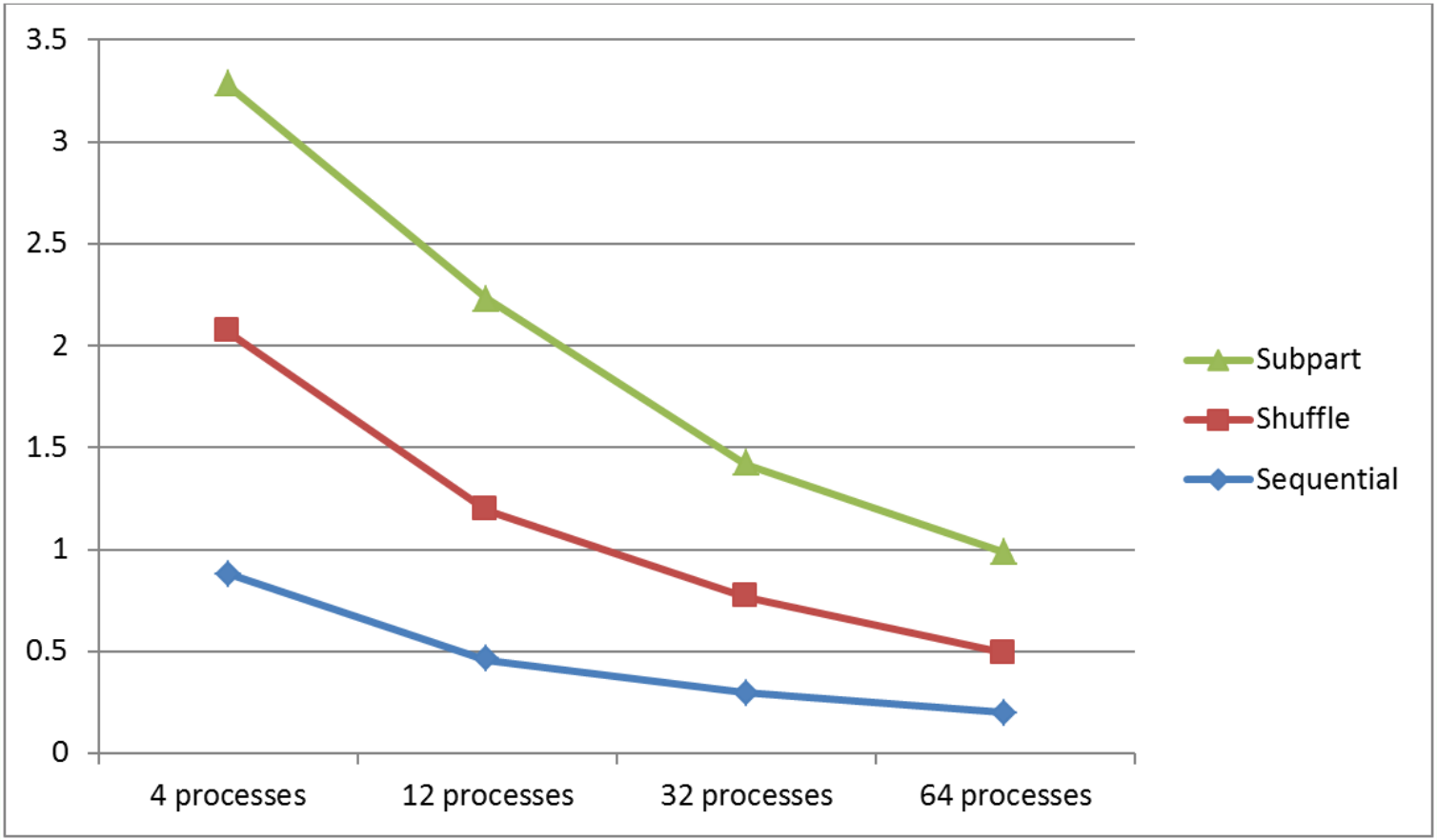


From Amdahl's law, we have $SpeedUp = \frac{T_s}{T_d}$ (Higher is better)

T_s: is run time with single process (sequential)

T_d: is run time with multi-processes (distributed)

Efficiency Chart Diagram



$Efficiency = \frac{T_s}{N \times T_d} = \frac{SpeedUp}{N}$ (Higher is better)

N: is number of processes ("nodes")

Efficiency decreases while number of processes increase

=> loss of efficiency

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Conclusion and Perspectives

- Conclusion:
  - Proposed a new efficient distributed algorithm (Subpart) for Behavioral Cartography
  - Proposed a new heuristic approach improving all BC distribution algorithms
  - Proposed solutions to our three problems
  - Implemented the new algorithm in IMITATOR

- Future works:
  - We will attempt to achieve a more efficient algorithm
  - Design an autonomous distribution scheme for BC
  - Improve heuristics
  - Try BC in GPU's or CPU+GPU's environment
  - . . . and prove the deadlock-freeness of our master-worker communication scheme!

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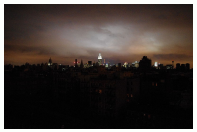
Additional explanation

Explanation for the 4 pictures in the beginning



Allusion to the Northeast blackout (USA, 2003)
Computer bug
Consequences: 11 fatalities, huge cost
(Picture actually from the Sandy Hurricane, 2012)

Error screen on the earliest versions of Macintosh

Allusion to the sinking of the Sleipner A offshore platform (Norway, 1991)
No fatalities
Computer bug: inaccurate finite element analysis modeling
(Picture actually from the Deepwater Horizon Offshore Drilling Platform)

Allusion to the MIM-104 Patriot Missile Failure (Iraq, 1991)
28 fatalities, hundreds of injured
Computer bug: software error (clock drift)
(Picture of an actual MIM-104 Patriot Missile, though not the one of 1991)

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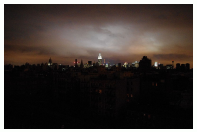
Source of the graphics used I



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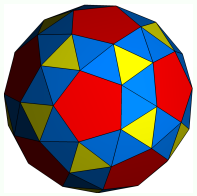

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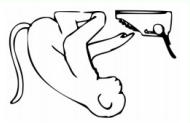

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