

# École Temps-Réel 2017

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## Timed automata and parametric timed automata

Étienne André

LIPN, Université Paris 13, CNRS, France

Feat. joint work with Giuseppe Lipari and Sun Youcheng



# Context: Verifying complex timed systems

- Need for early bug detection
  - Bugs discovered when final testing: **expensive**  
~ Need for a thorough specification and verification phase



# The Therac-25 radiation therapy machine (1/2)

- Radiation therapy machine used in the 1980s
- Involved in accidents between 1985 and 1987, in which patients were given **massive overdoses of radiation**
  - Approximately **100 times** the intended dose!
  - Numerous causes, including **race condition**

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*“The failure only occurred when a particular nonstandard sequence of keystrokes was entered on the VT-100 terminal which controlled the PDP-11 computer: an X to (erroneously) select 25MV photon mode followed by ↑, E to (correctly) select 25 MeV Electron mode, then Enter, all **within eight seconds.**”*

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## Limits of testing

This case illustrates the difficulty of bug detection without formal methods.

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- health-related devices
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- smart homes and smart cities
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- etc.

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Hence, high need for **formal verification**

# Outline

- 1 Finite-state automata
- 2 Timed automata
- 3 Parametric timed automata
- 4 Modeling and verifying real-time systems with parameters
- 5 A case study: Verifying a real-time system under uncertainty
- 6 Conclusion and perspectives

# Outline: Finite-state automata

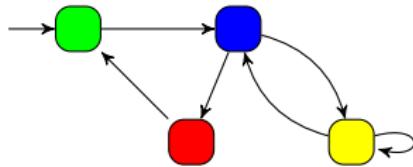
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# Model checking concurrent systems

- Use formal methods [Baier and Katoen, 2008]



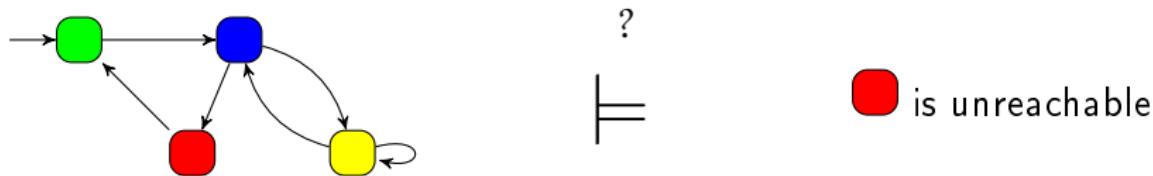
is unreachable

A **model** of the system

A **property** to be satisfied

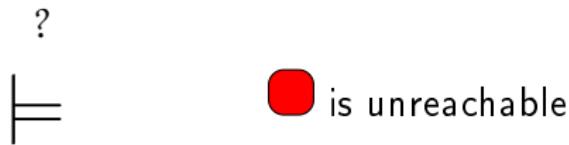
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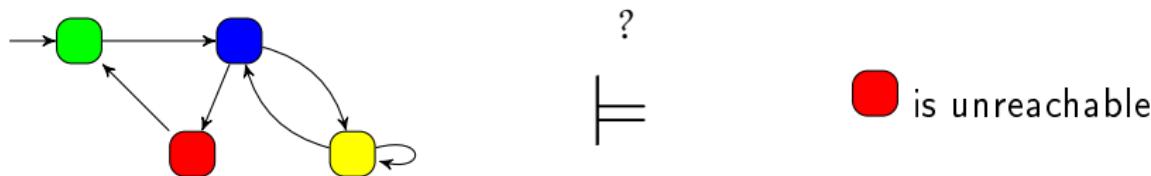
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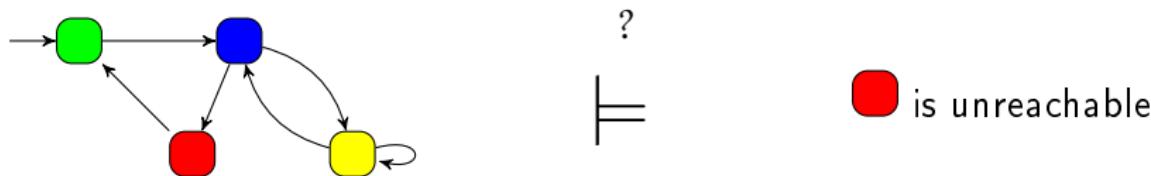
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Counterexample

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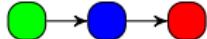
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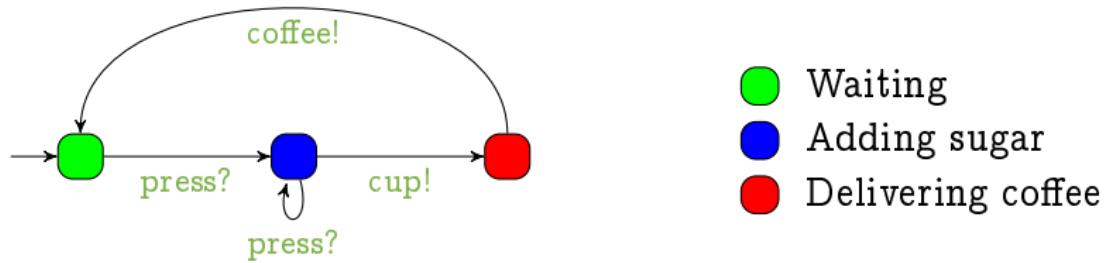
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Counterexample

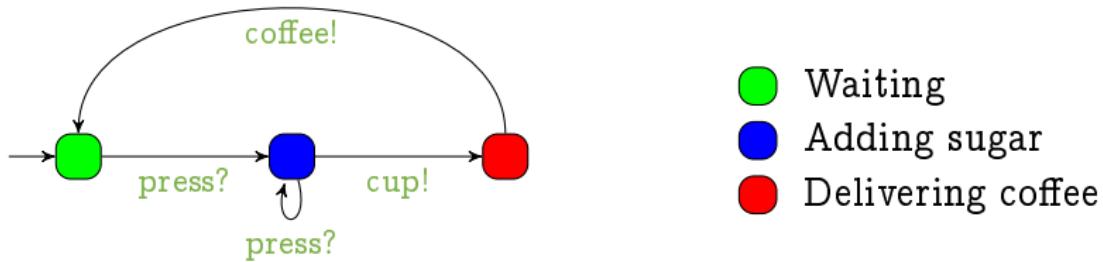
Turing award (2007) to Edmund M. Clarke, Allen Emerson and Joseph Sifakis

# Finite state automata: A coffee machine $\mathcal{A}_C$



- Example of runs
  - Coffee with no sugar

# Finite state automata: A coffee machine $\mathcal{A}_C$



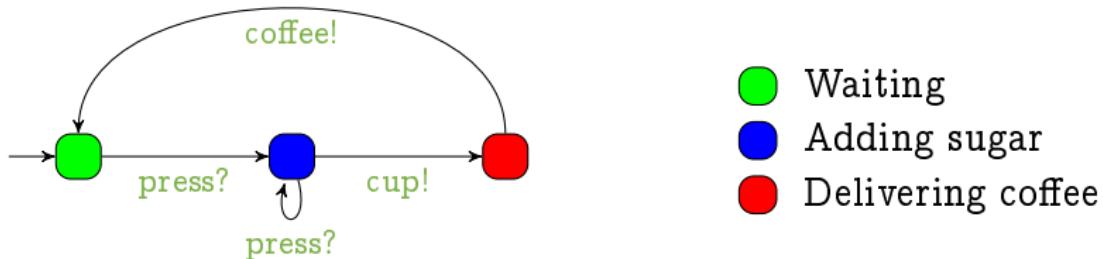
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# Finite state automata: A coffee machine $\mathcal{A}_C$



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- And so on

# Outline: Timed automata

## 1 Finite-state automata

## 2 Timed automata

- Introduction
- Syntax
- Semantics
- Decision problems
- Software

## 3 Parametric timed automata

## 4 Modeling and verifying real-time systems with parameters

## 5 A case study: Verifying a real-time system under uncertainty

# Beyond finite state automata

Finite State Automata give a powerful syntax and semantics to model  
**qualitative** aspects of systems

- Executions, sequence of actions
- Modular definitions (parallelism)
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Finite State Automata give a powerful syntax and semantics to model **qualitative** aspects of systems

- Executions, sequence of actions
- Modular definitions (parallelism)
- Powerful checking (reachability, safety, liveness...)

But what about **quantitative** aspects:

- Time ("the airbag always eventually inflates, but maybe 10 seconds after the crash")
- Temperature ("the alarm always eventually ring, but maybe when the temperature is above 75 degrees")

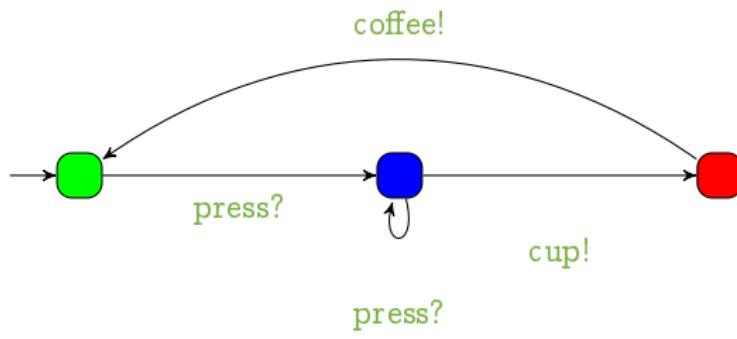
# Timed automaton (TA)

- Finite state automaton (sets of locations)



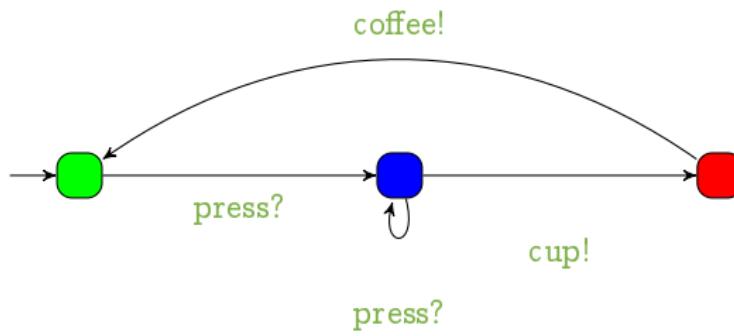
# Timed automaton (TA)

- Finite state automaton (sets of locations and actions)



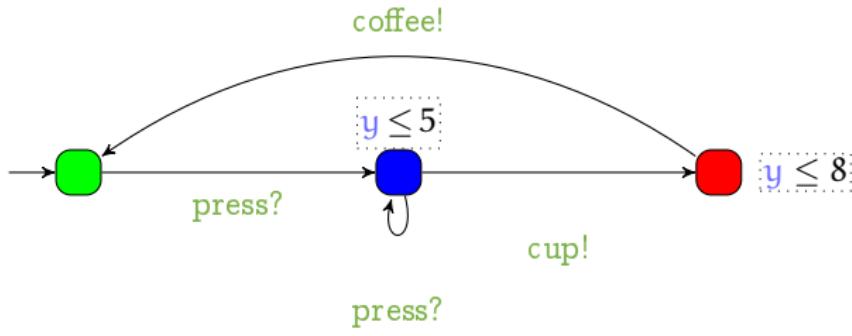
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- Finite state automaton (sets of **locations** and **actions**) augmented with a set  $X$  of **clocks** [Alur and Dill, 1994]
  - Real-valued variables evolving linearly at the same rate



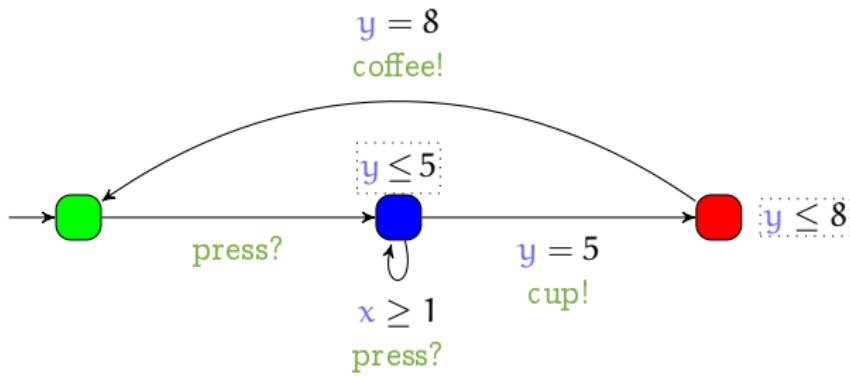
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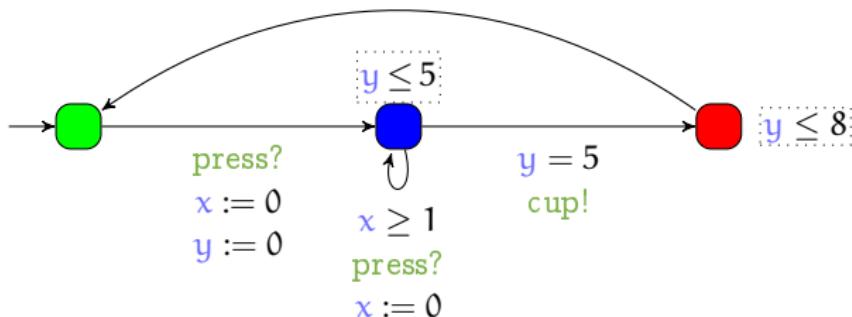
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- Features

- Location **invariant**: property to be verified to stay at a location
- Transition **guard**: property to be verified to enable a transition
- Clock **reset**: some of the clocks can be set to 0 at each transition

$y = 8$

coffee!



# Concrete semantics of timed automata

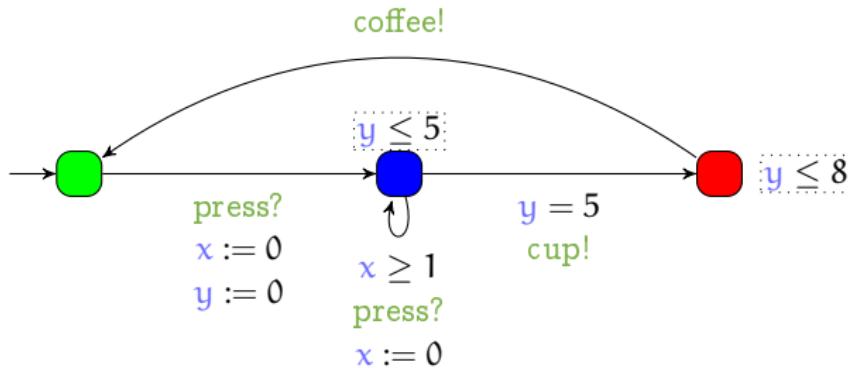
- Concrete state of a TA: pair  $(l, w)$ , where

- $l$  is a location,
- $w$  is a valuation of each clock

Example:  $(\bullet, (x=1.2, y=3.7))$

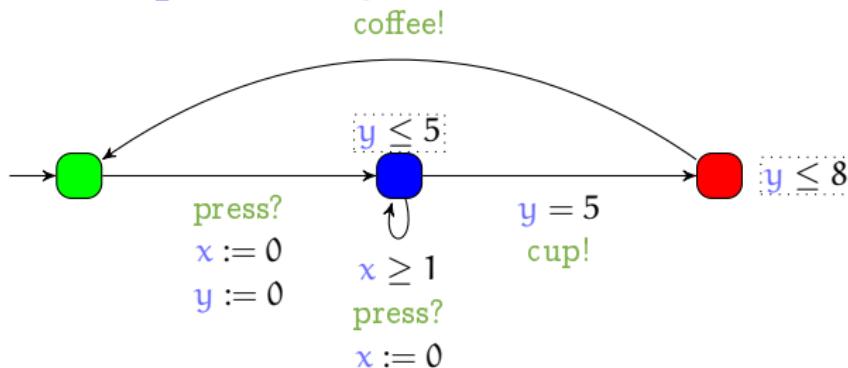
- Concrete run: alternating sequence of concrete states and actions or time elapse

# Example of concrete runs



- Possible concrete runs for the coffee machine

# Example of concrete runs

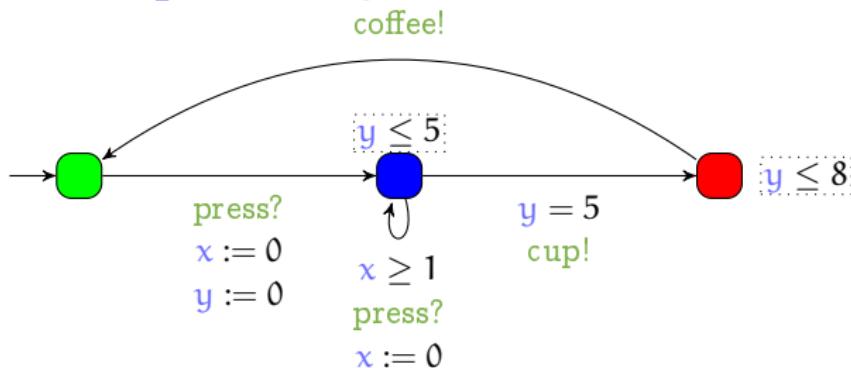


- Possible concrete runs for the coffee machine
  - Coffee with no sugar



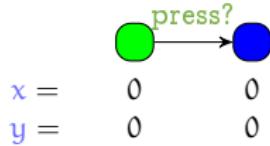
$x = 0$   
 $y = 0$

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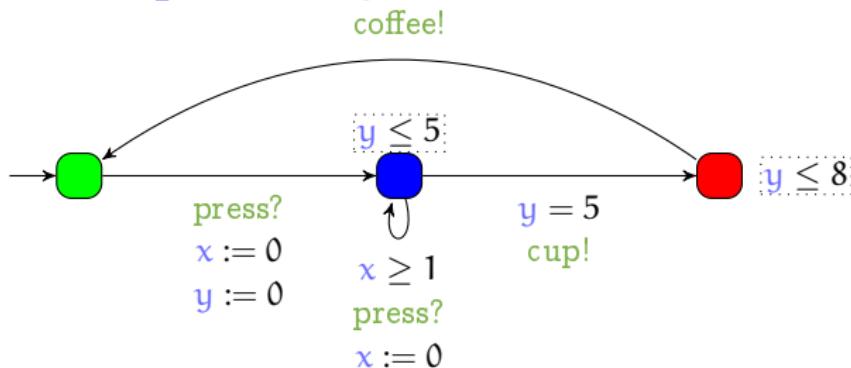


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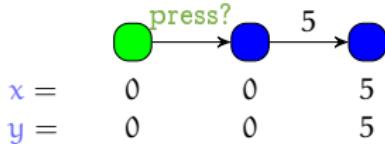


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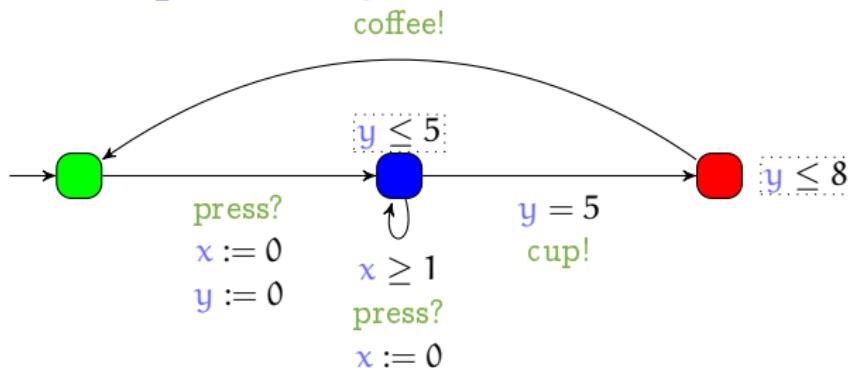


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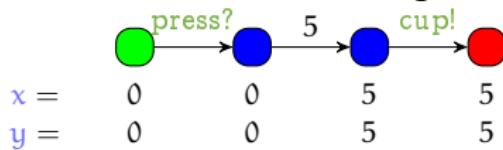


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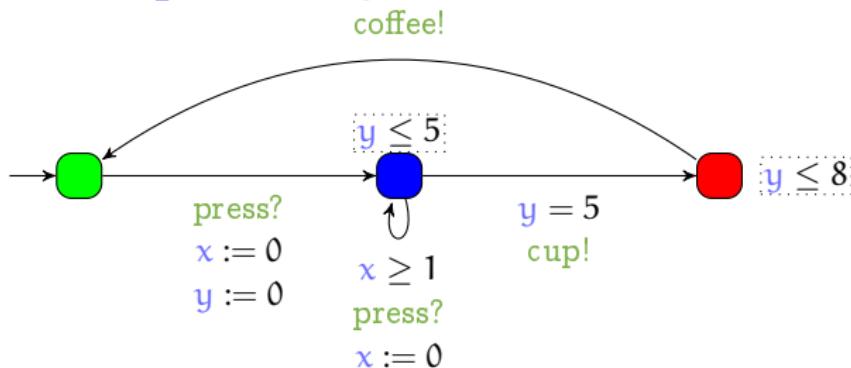


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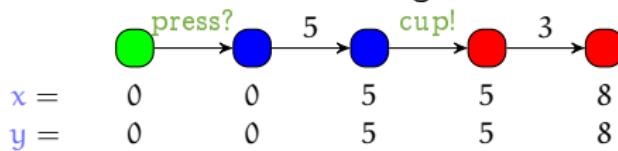


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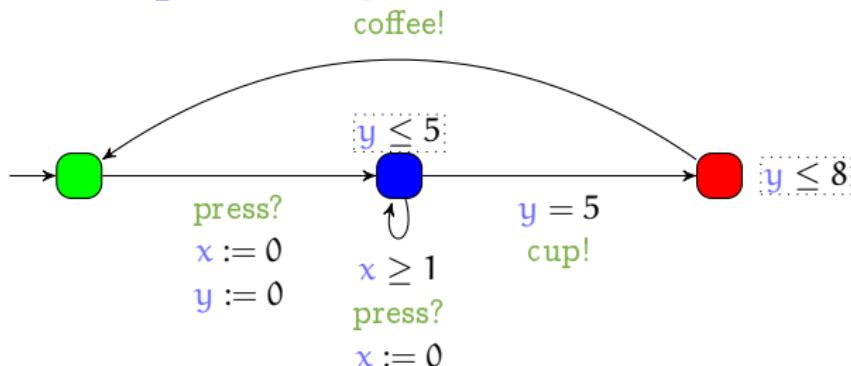


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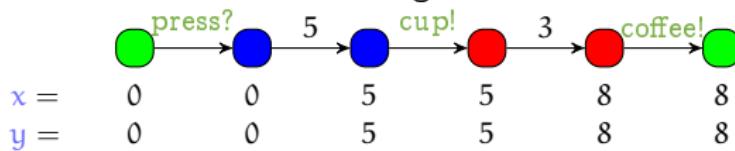


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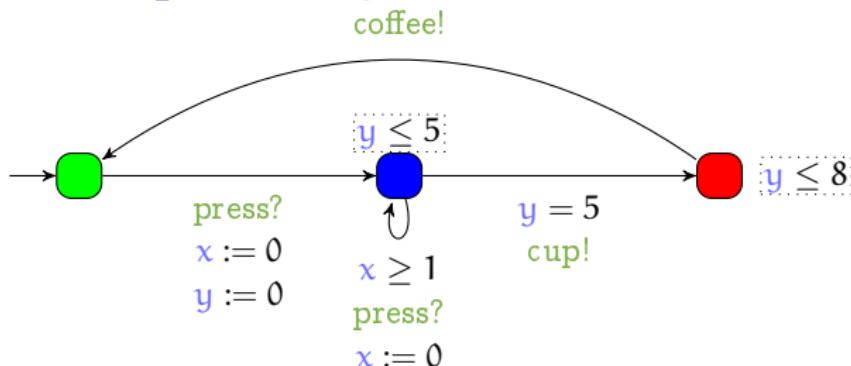


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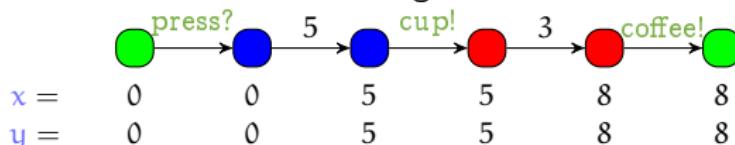


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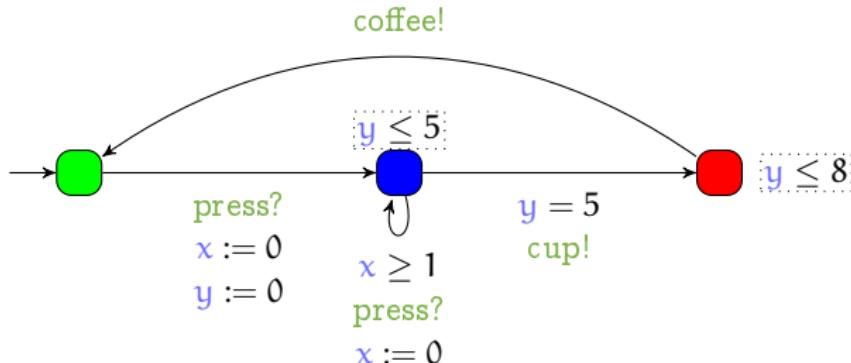


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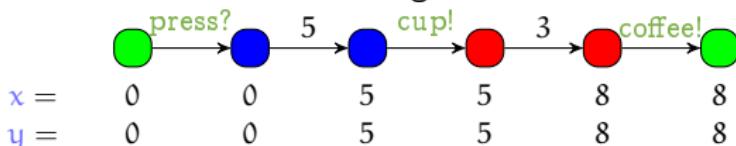
$x =$  0  
 $y =$  0

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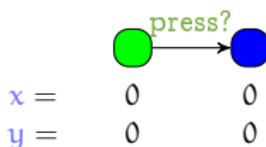


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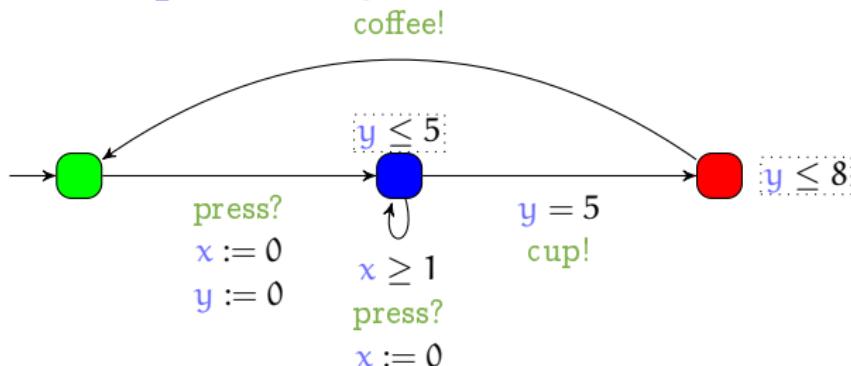
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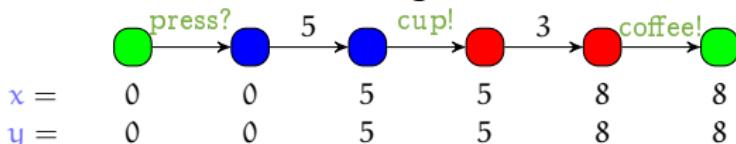


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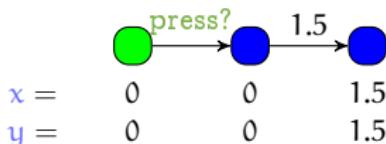


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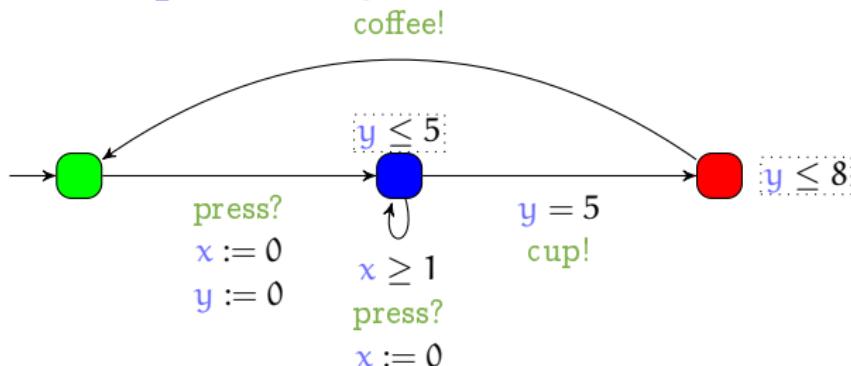
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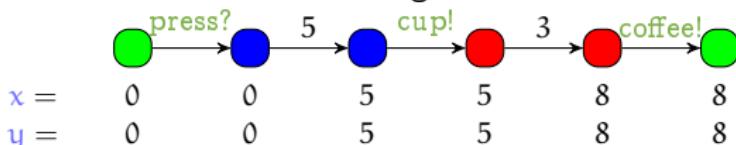


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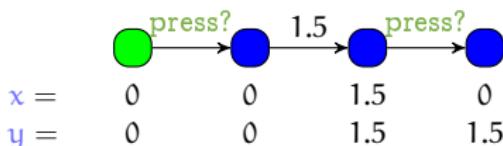


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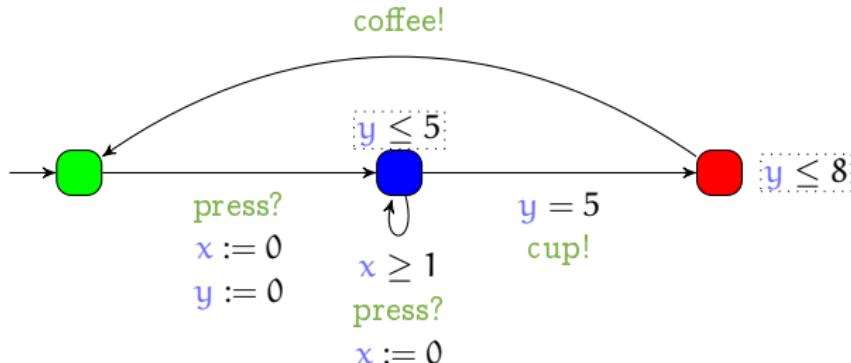
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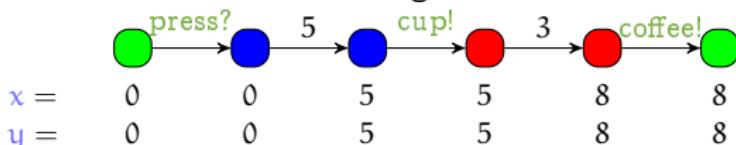


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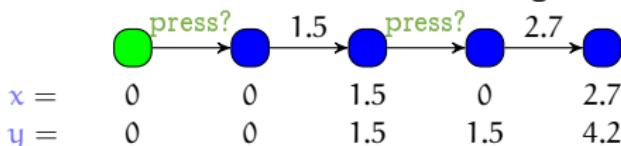


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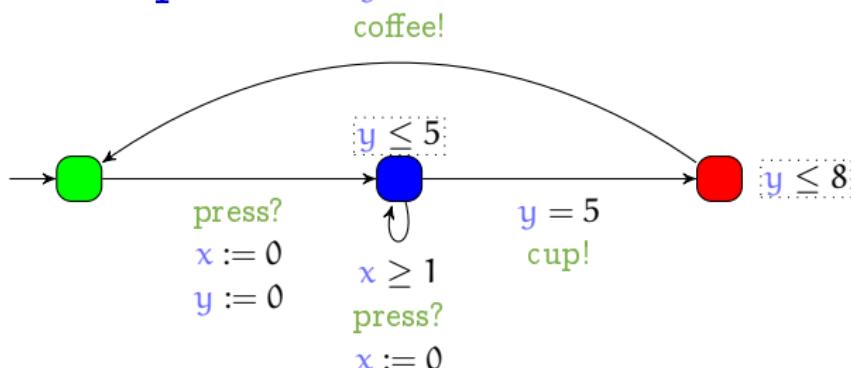
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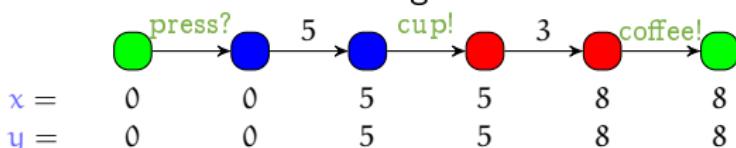


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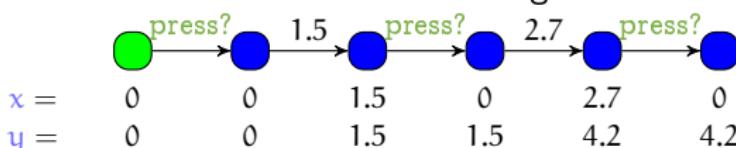


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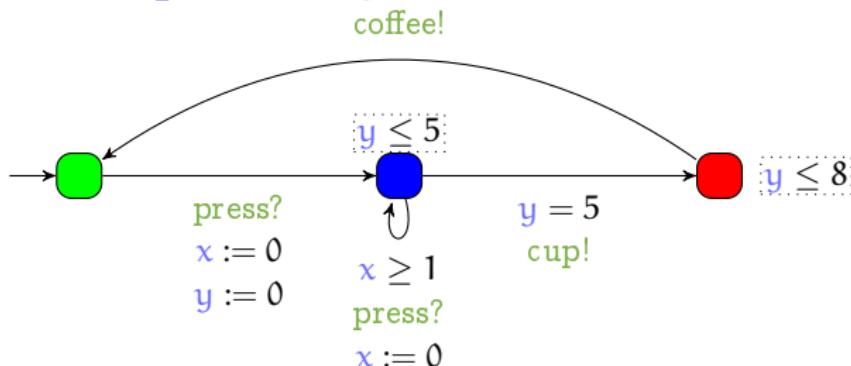
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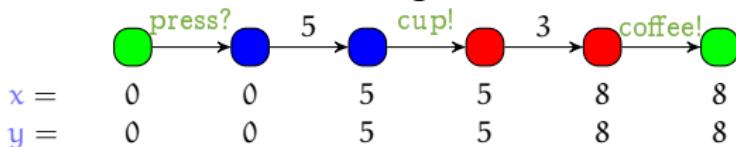


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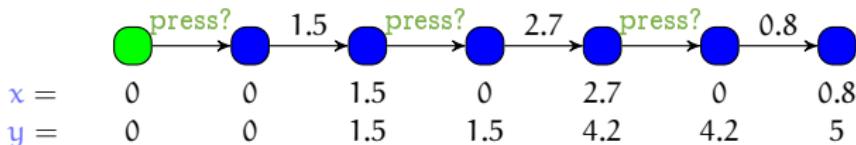


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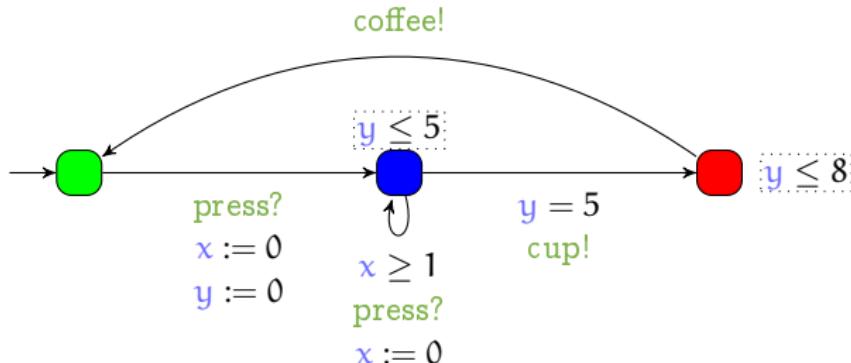
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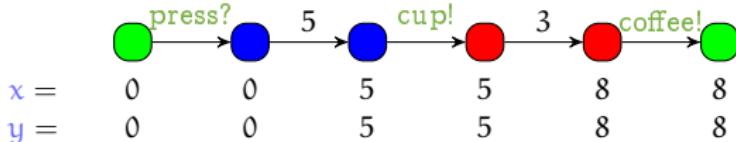


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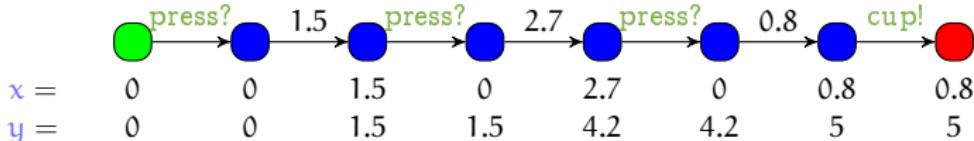


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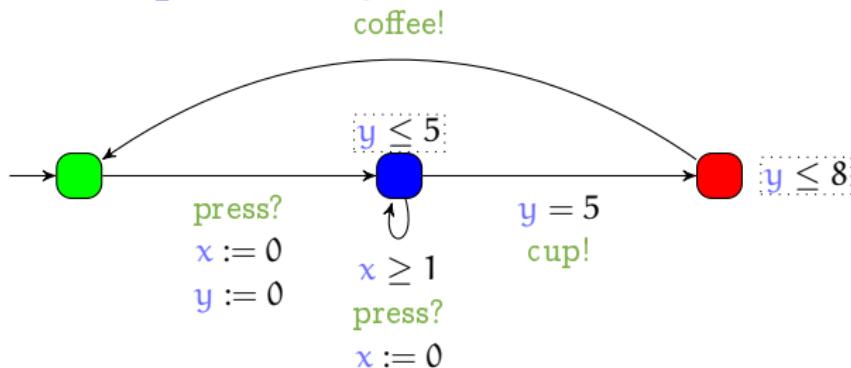
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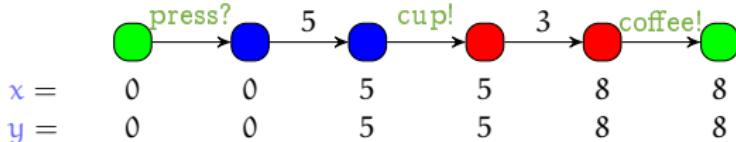


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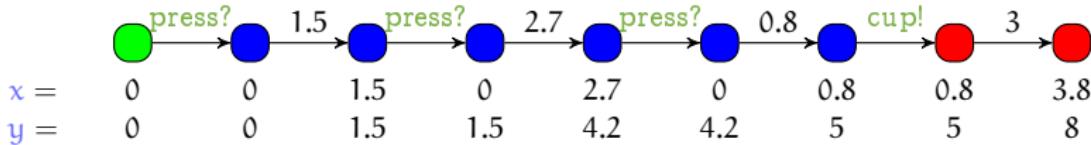


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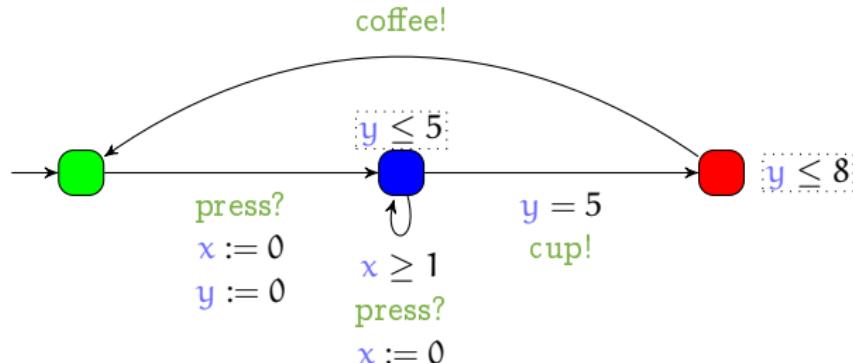
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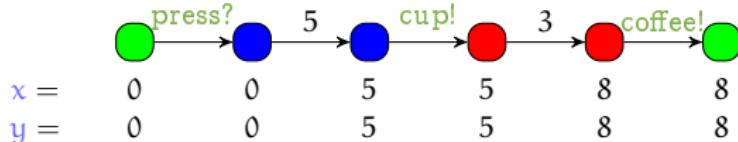


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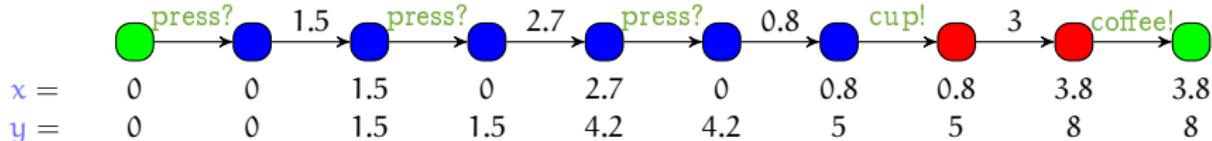


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# Dense time

- Time is **dense**: transitions can be taken anytime
  - **Infinite** number of timed runs
  - Model checking needs a **finite** structure!
- Some runs are **equivalent**
  - Taking the **press?** action at  $t = 1.5$  or  $t = 1.57$  is equivalent w.r.t. the possible actions
- Idea: reason with abstractions
  - **Region automaton** [Alur and Dill, 1994], and **zone automaton**
  - Example: in location , all clock values in the following zone are equivalent
$$y \leq 5 \wedge y - x \geq 4$$
  - This abstraction is **finite**

# Symbolic states for timed automata

- **Objective:** group all concrete states reachable by the same sequence of discrete actions
- **Symbolic state:** a location  $l$  and a (infinite) set of states  $Z$
- For timed automata,  $Z$  can be represented by a **convex polyhedron** with a special form called **zone**, with constraints

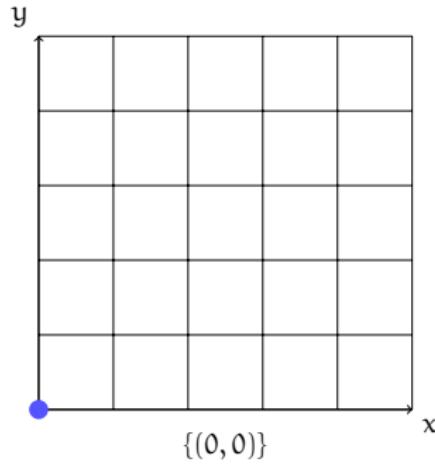
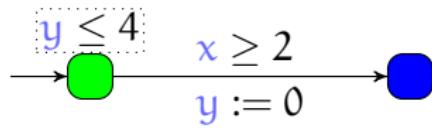
$$-d_{0i} \leq x_i \leq d_{i0} \text{ and } x_i - x_j \leq d_{ij}$$

- Computation of successive reachable symbolic states can be performed **symbolically** with polyhedral operations: for edge  $e = (l, a, g, R, l')$ :

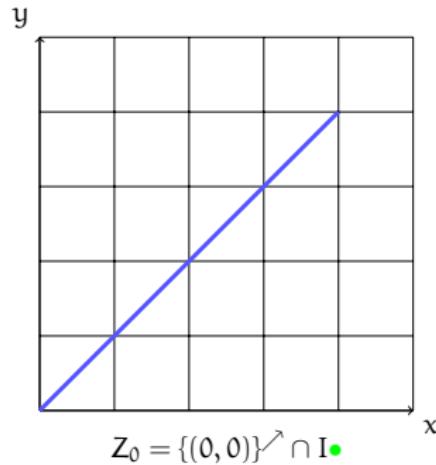
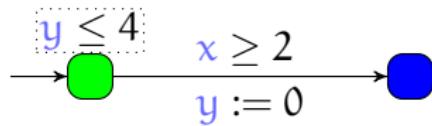
$$\text{Succ}((l, Z), e) = (l', [(Z \cap g)]_R \cap I(l'))^\nearrow \cap I(l')$$

- With an additional technicality, there is a **finite number** of reachable zones in a TA.

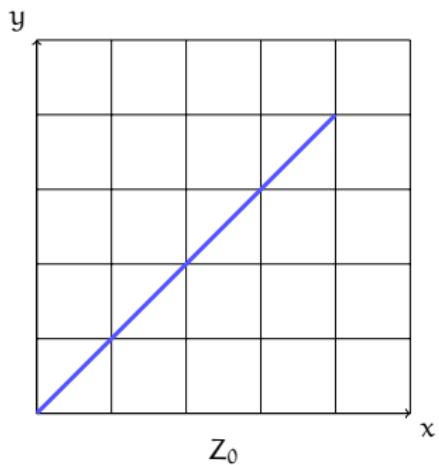
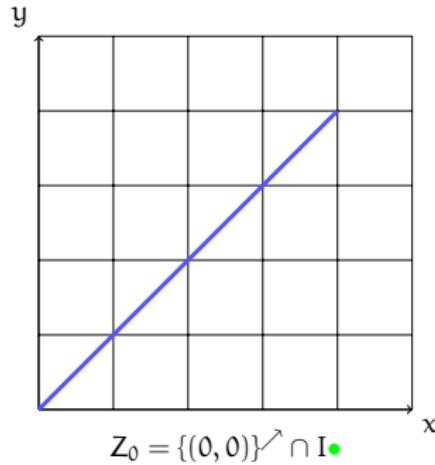
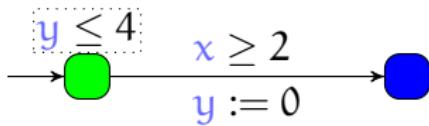
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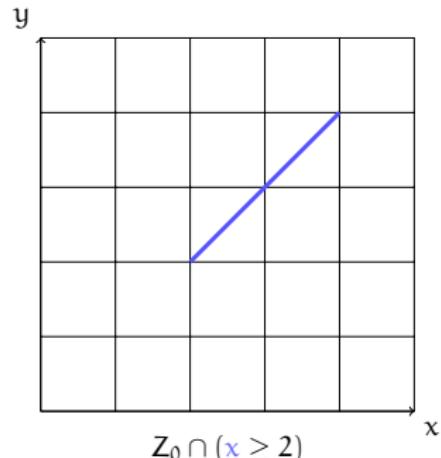
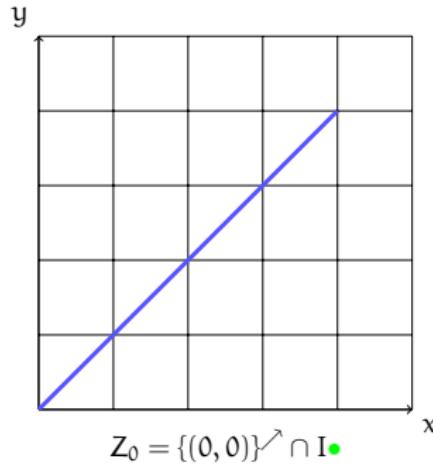
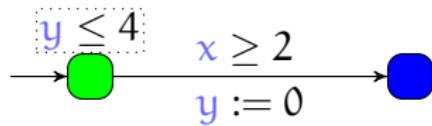
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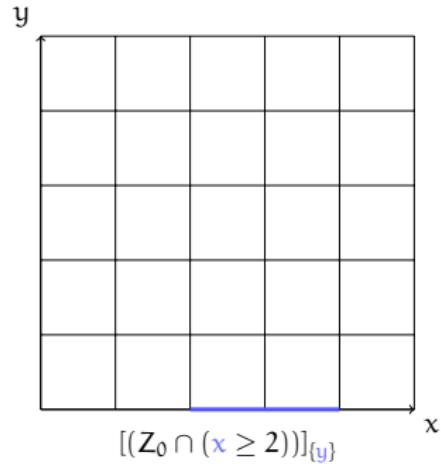
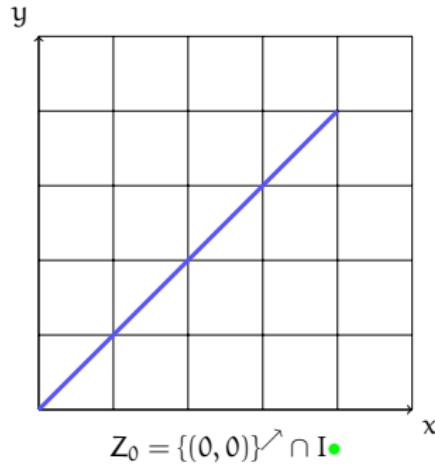
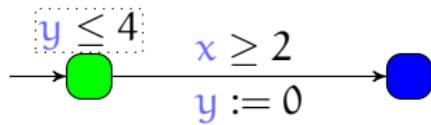
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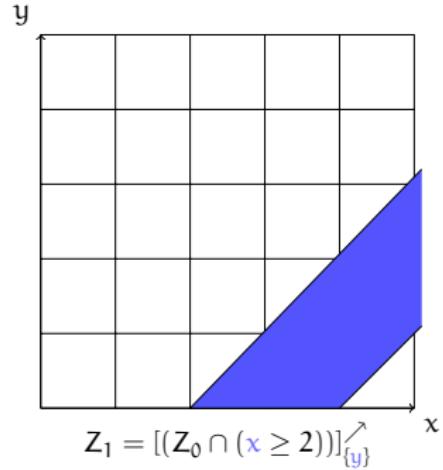
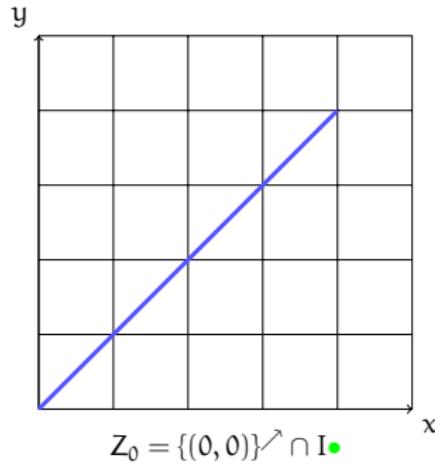
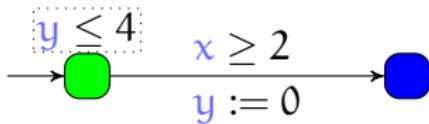
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# Abstract semantics of timed automata

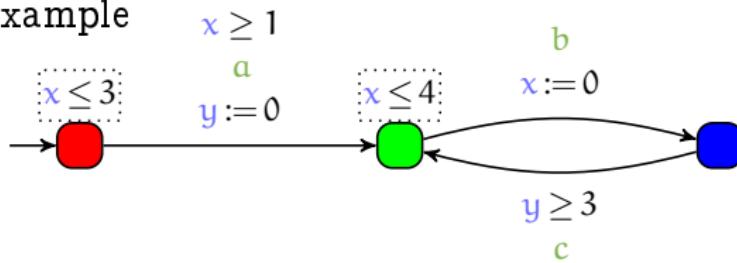
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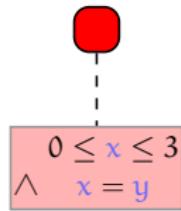
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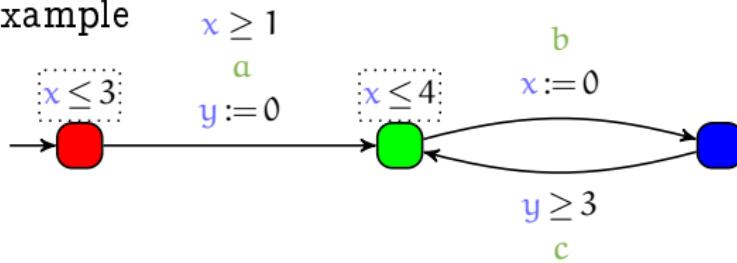


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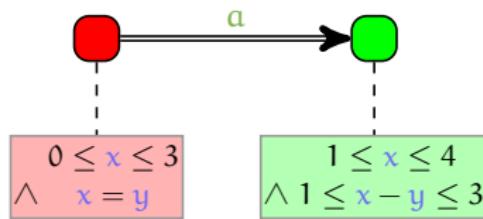


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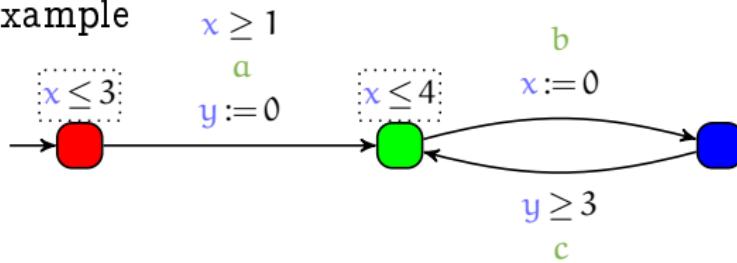


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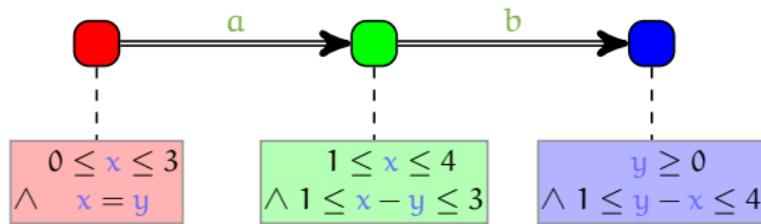


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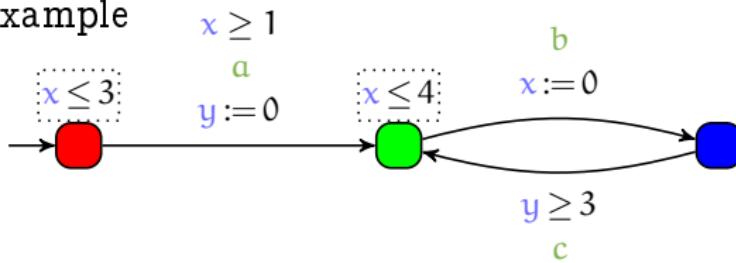


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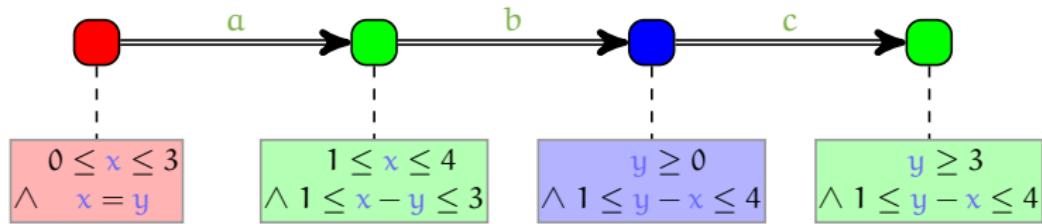


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However, one can:

- design **semi-algorithms**: if the algorithm halts, then its result is correct
- design algorithms yielding over- or under-**approximations**

# Decision problems for timed automata

The finiteness of the region automaton allows us to check properties

- ☺ Reachability of a location [Alur and Dill, 1994]
- ☺ Liveness (Büchi conditions) [Alur and Dill, 1994]

Some problems impossible to check using the region automaton (but still **decidable**)

- ☺ non-Zenoness emptiness check [Wang et al., 2015]

Some **undecidable** problems (and hence impossible to check in general)

- ☹ universality of the timed language [Alur and Dill, 1994]
- ☹ timed language inclusion [Alur and Dill, 1994]

# Software supporting timed automata

Timed automata have been successfully used since the 1990s

Tools for modeling and verifying models specified using TA

- HYTECH (also hybrid, parametric timed automata) [Henzinger et al., 1997]
- KRONOS [Yovine, 1997]
- TREX (also parametric timed automata) [Annichini et al., 2001]
- UPPAAL [Larsen et al., 1997]
- ROMÉO (parametric time Petri nets) [Lime et al., 2009]
- PAT (also other formalisms) [Sun et al., 2009]
- IMITATOR (also parametric timed automata) [André et al., 2012]

# Outline: Parametric timed automata

1 Finite-state automata

2 Timed automata

3 Parametric timed automata

- Syntax
- Semantics
- Decidability results
- L/U-PTAs

4 Modeling and verifying real-time systems with parameters

5 A case study: Verifying a real-time system under uncertainty

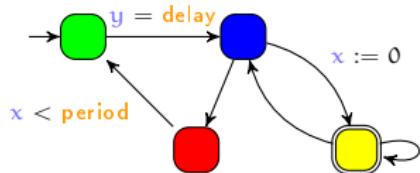
# Beyond timed model checking: parameter synthesis

- Verification for **one** set of constants does not usually guarantee the correctness for other values
- Challenges
  - **Numerous verifications:** is the system correct for any value within [40; 60]?
  - **Optimization:** until what value can we increase 10?
  - **Robustness** [Markey, 2011]: What happens if 50 is implemented with 49.99?
  - **System incompletely specified:** Can I verify my system even if I don't know the period value with full certainty?

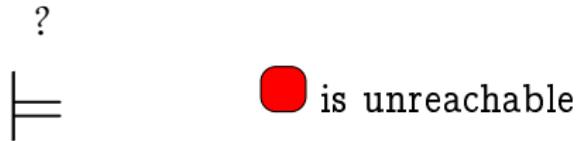
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- Parameter synthesis
  - Consider that timing constants are unknown constants (**parameters**)

# timed model checking



A **model** of the system



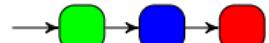
A **property** to be satisfied

- Question: does the model of the system satisfy the property?

Yes

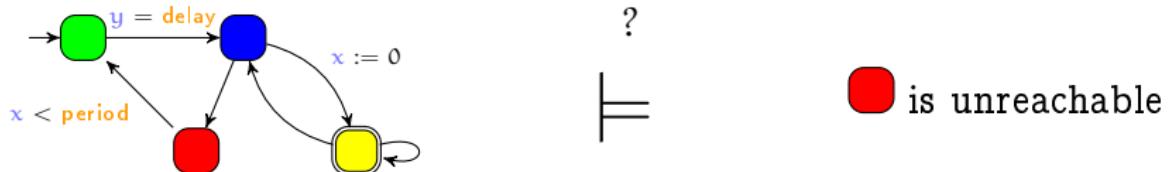


No



Counterexample

# Parametric timed model checking



A **model** of the system

A **property** to be satisfied

- Question: for what values of the parameters does the model of the system satisfy the property?

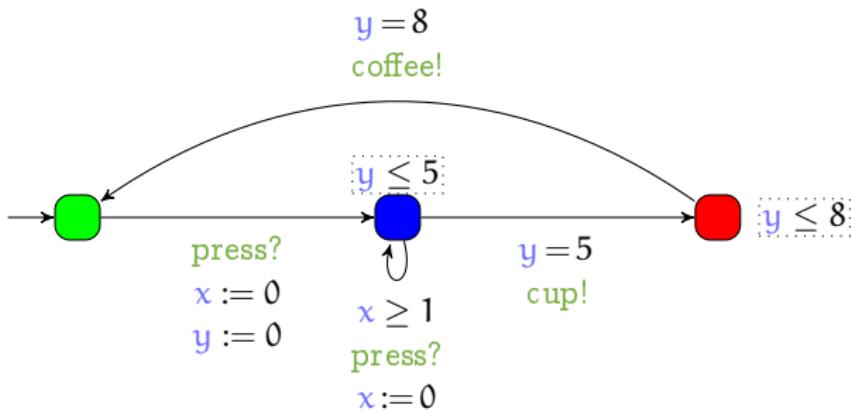
Yes if...



$$\begin{aligned} 2\text{delay} &> \text{period} \\ \wedge \text{period} &< 20.46 \end{aligned}$$

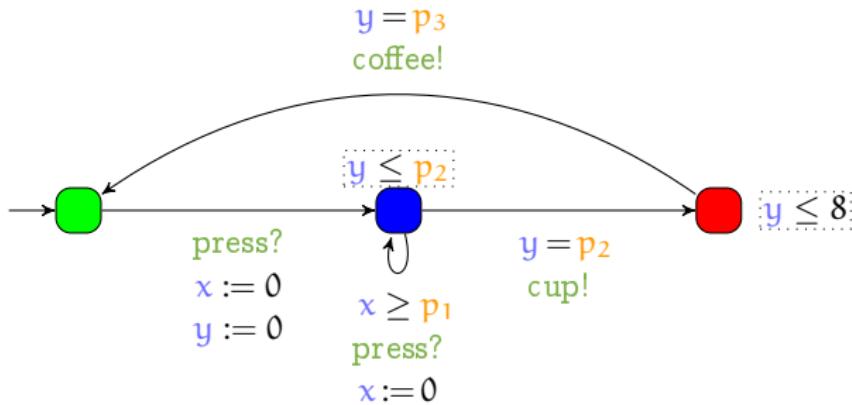
# Parametric Timed Automaton (PTA)

- Timed automaton (sets of locations, actions and clocks)



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- Timed automaton (sets of locations, actions and clocks)  
augmented with a set  $P$  of parameters [Alur et al., 1993b]
- Unknown constants compared to a clock in guards and invariants

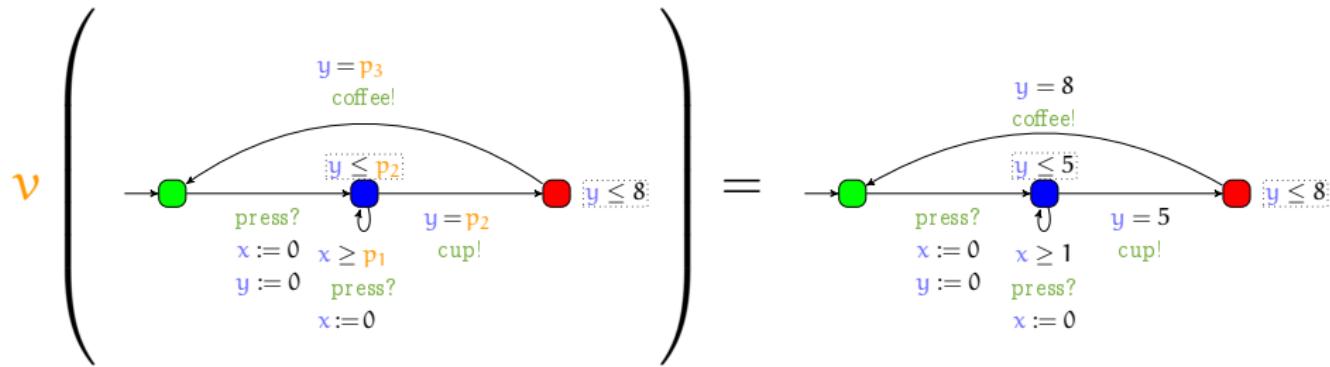


## Valuation of a PTA

- Given a PTA  $\mathcal{A}$  and a parameter valuation  $v$ , we denote by  $v(\mathcal{A})$  the (non-parametric) timed automaton where each parameter  $p$  is valued by  $v(p)$

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with  $v$  :  $\begin{cases} p_1 \rightarrow 1 \\ p_2 \rightarrow 5 \\ p_3 \rightarrow 8 \end{cases}$

# Symbolic semantics of parametric timed automata

- **Symbolic state** of a PTA: pair  $(l, C)$ , where
    - $l$  is a **location**,
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- [Hune et al., 2002]

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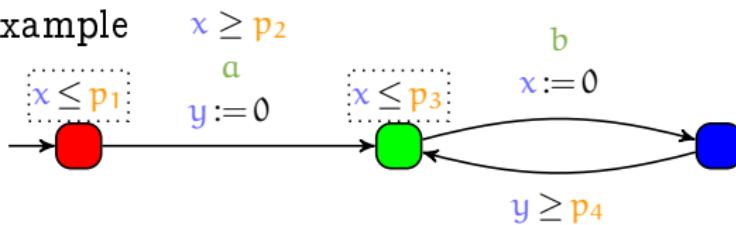
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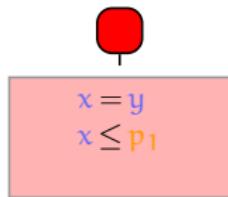
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- Possible symbolic run for this PTA

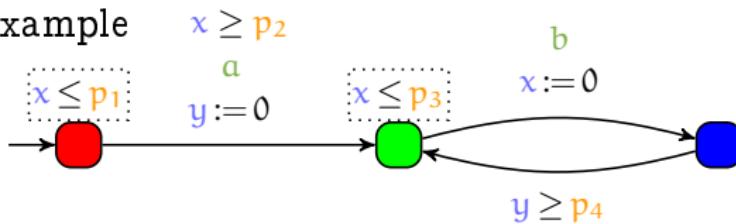


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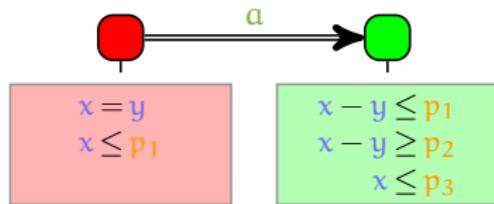
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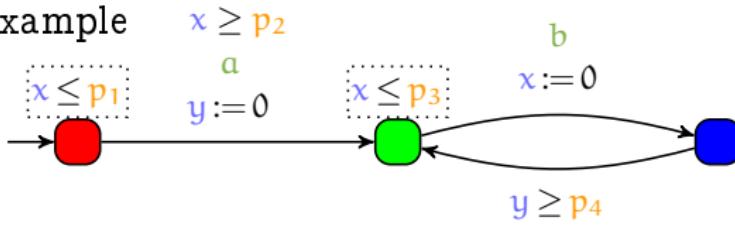


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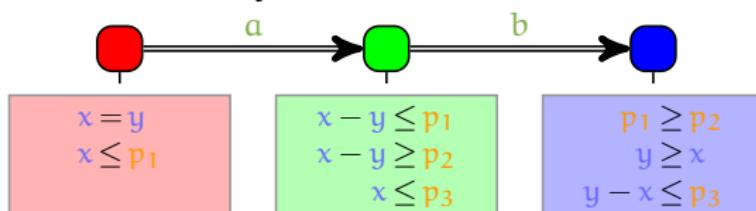


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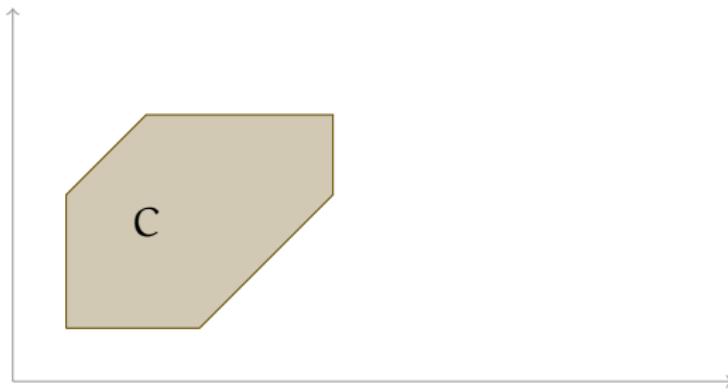


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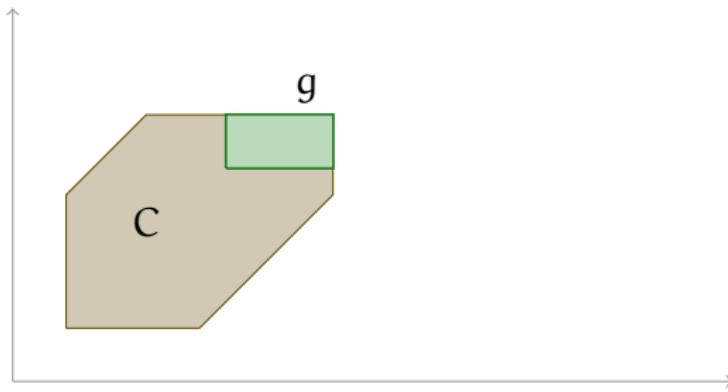
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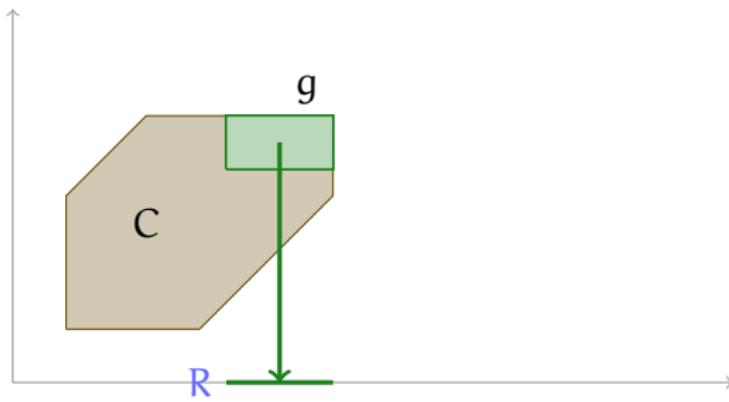
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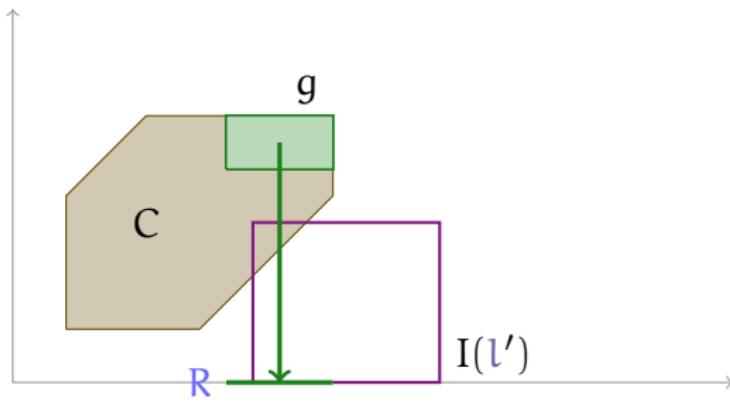
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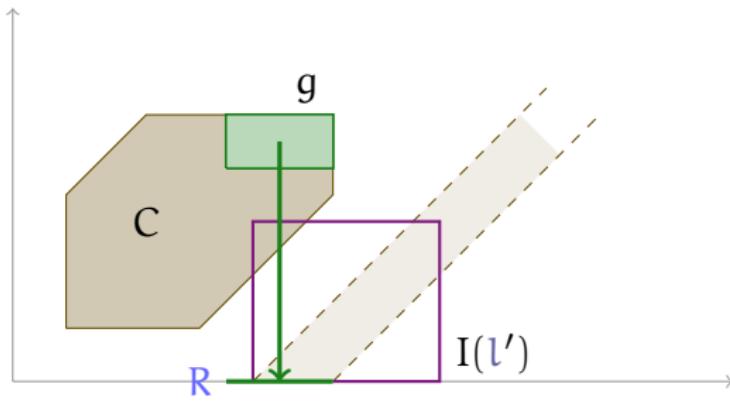
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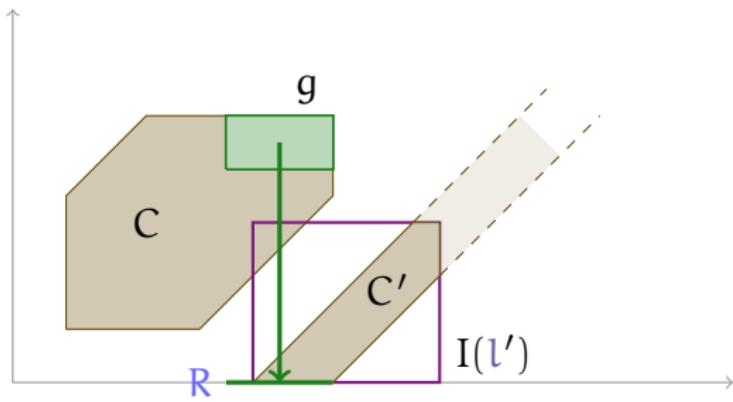
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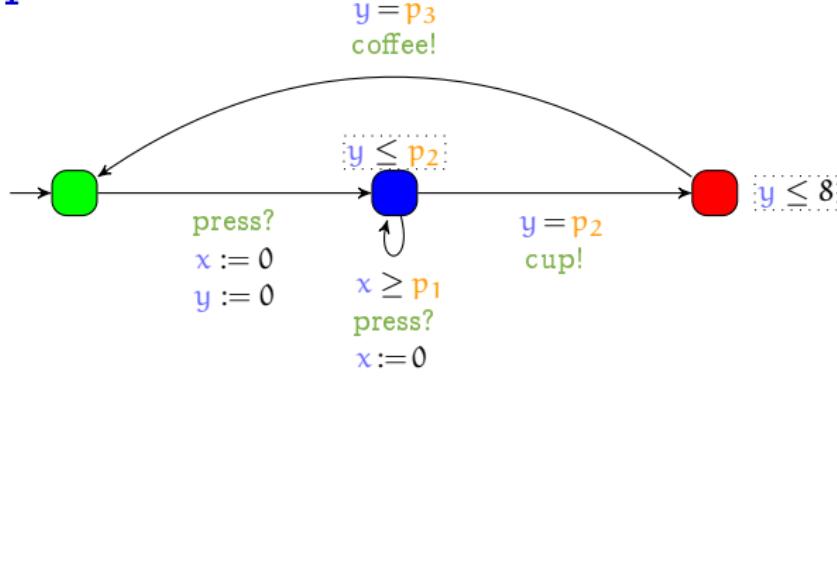


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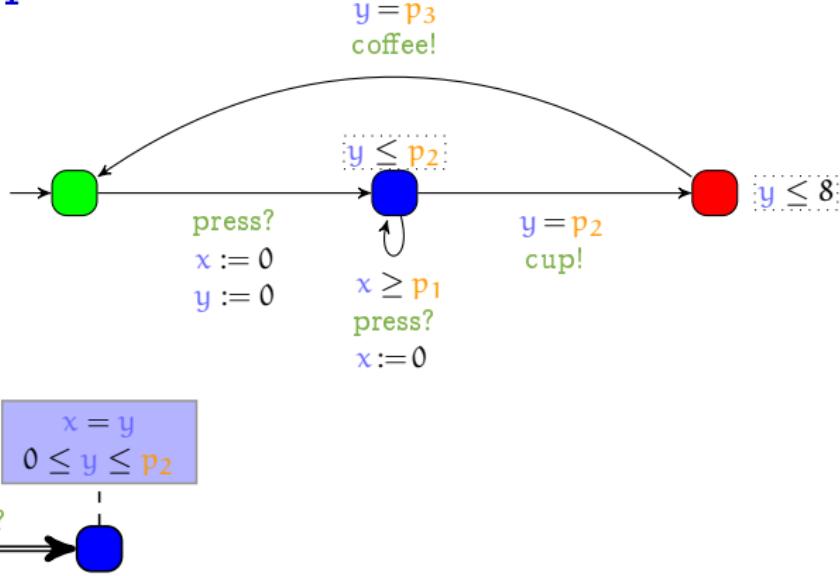
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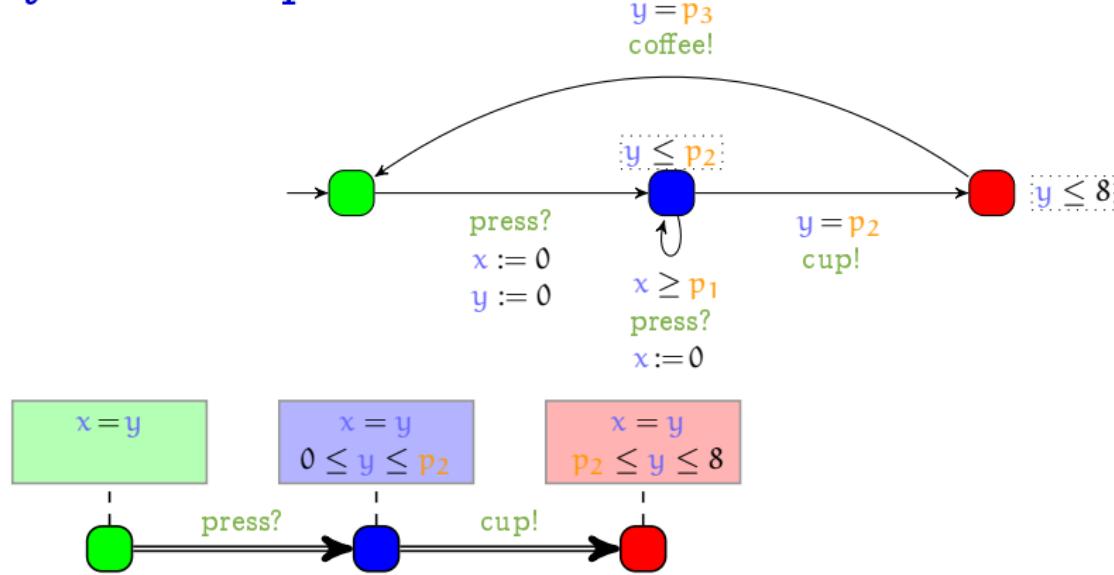
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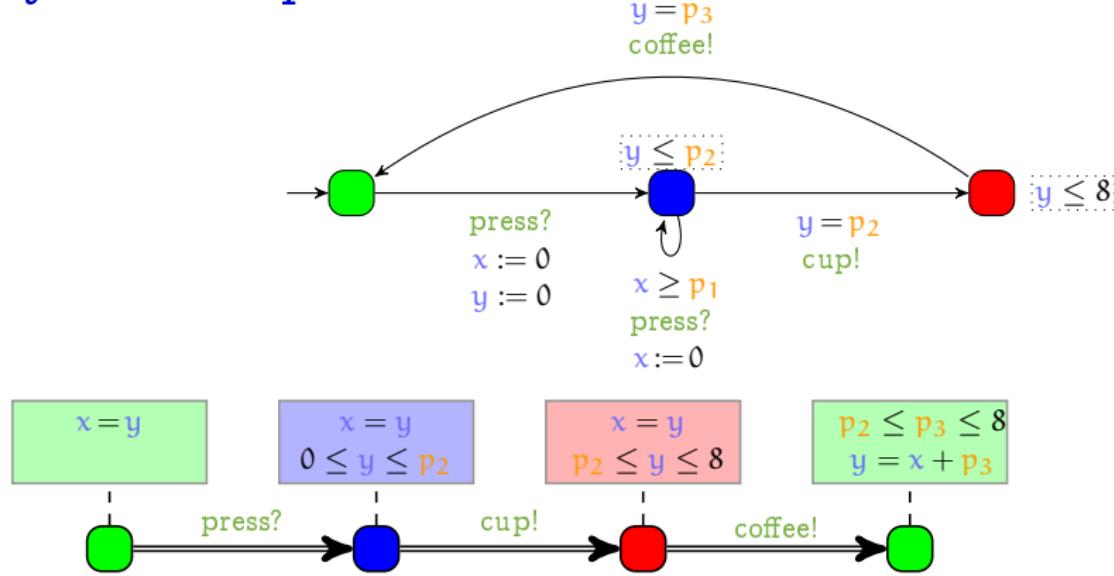
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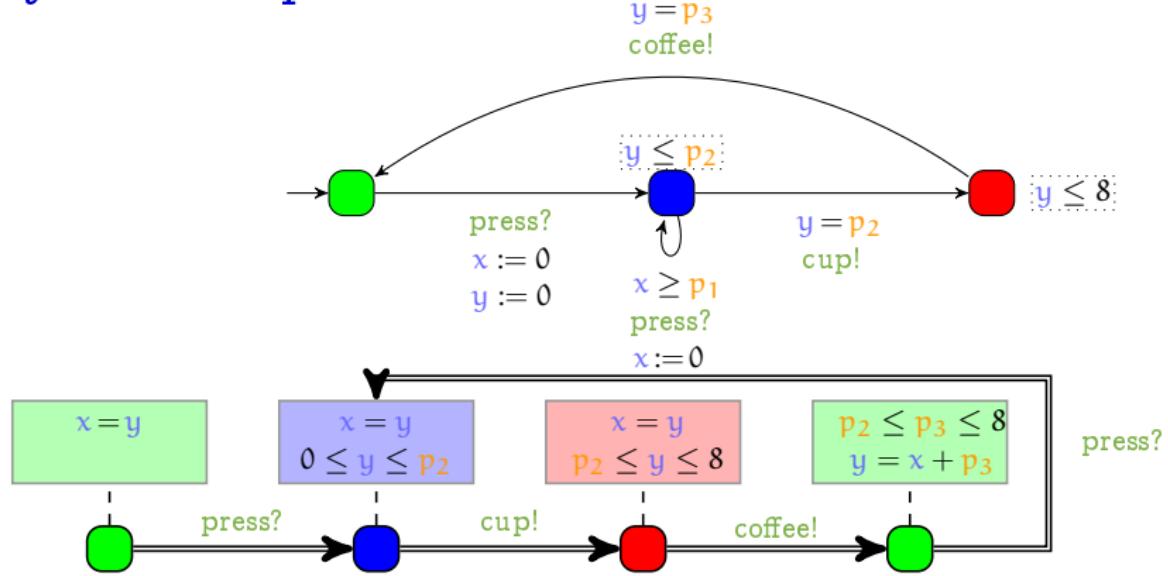
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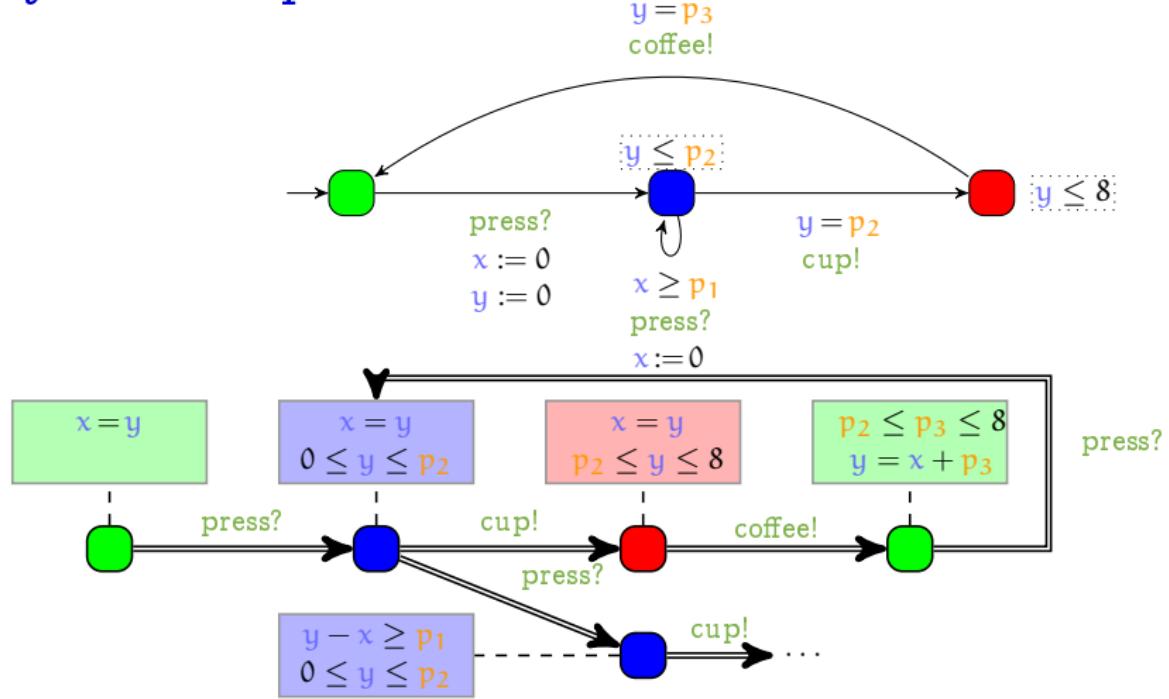
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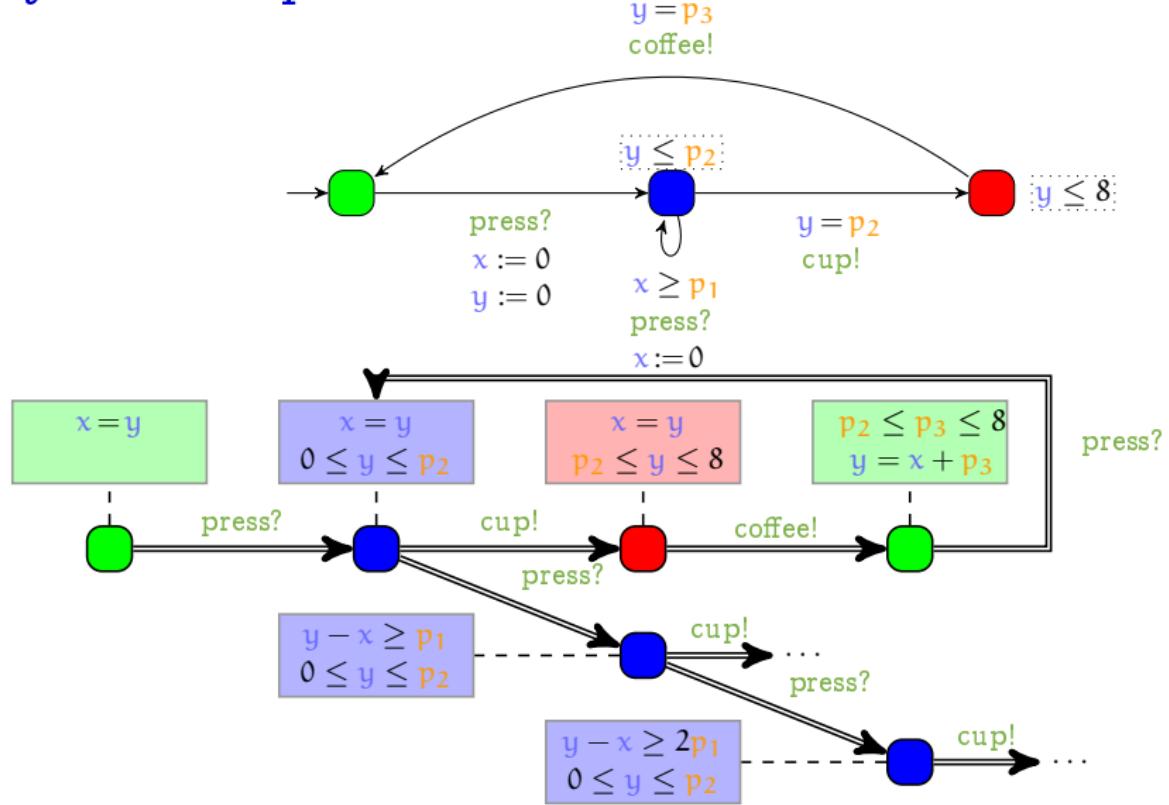
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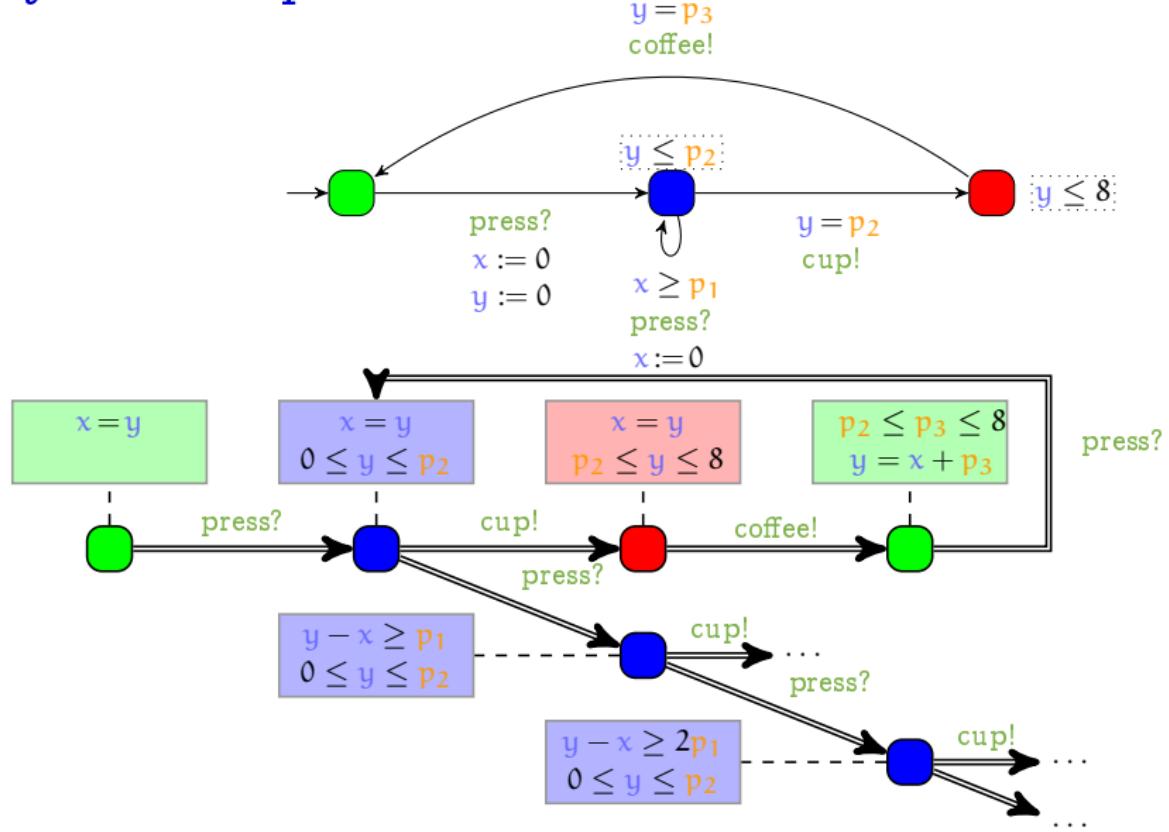
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# Decision and computation problems for PTA

- **EF-Emptiness** “Is the set of parameter valuations for which a given location  $l$  is reachable empty?”

**Example:** “Does there exist at least one parameter valuation for which I can get a coffee with 2 sugars?”

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**Example:** “Are all parameter valuations such that I may eventually get a coffee?”

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✗, e. g.,  $p_1 = 1, p_2 = 5, p_3 = 2$

- **Preservation of the untimed language** “Given a parameter valuation, does there exist another valuation with the same untimed language? ”

**Example:** “Given the valuation  $p_1 = 1, p_2 = 5, p_3 = 8$ , do there exist other valuations with the same possible untimed behaviours?”

✓

# Computation problems for PTA

- EF-Synthesis “Find all parameter valuations for which a given location  $l$  is reachable”

**Example:** “What are all parameter valuations such that one may eventually get a coffee?”

- and so on

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$$0 \leq p_2 \leq p_3 \leq 8$$

- and so on

# Undecidability

- The symbolic state space is **infinite** in general
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## Bad news

All interesting problems are undecidable for (general) parametric timed automata.

# Decidability results for PTA (1/2)

## ■ EF-emptiness problem

“Is the set of parameter valuations for which a given location  $l$  is  
reachable empty?”

undecidable

[Alur et al., 1993b]

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## ■ AF-emptiness problem

“Is the set of parameter valuations for which all runs eventually reach a given location  $l$  empty? ”

undecidable

[Jovanović et al., 2015]

# Decidability results for PTA (2/2)

## ■ AF-universality problem

“Do all parameter valuations allow to reach a given location  $\textcolor{blue}{l}$  for all runs?”

undecidable

[André et al., 2016]

## Decidability results for PTA (2/2)

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In fact most interesting problems for PTAs are undecidable

[André, 2017]

# Limiting the number of clocks

Undecidability of EF-emptiness is achieved **for a single parameter**

[Miller, 2000, Beneš et al., 2015]

However, reducing the number of clocks yields decidability of the EF-emptiness problem:

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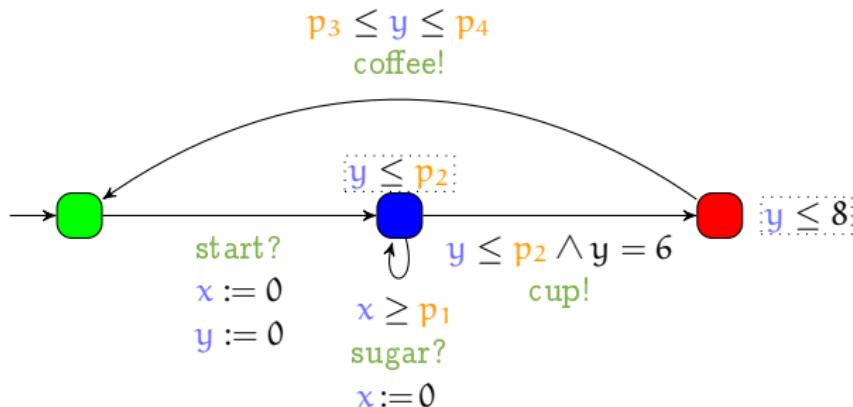
However, reducing the number of clocks yields decidability of the EF-emptiness problem:

- ✓ 1 parametric clock and arbitrarily many non-parametric clocks and integer-valued parameters [Beneš et al., 2015]
- ✓ 1 parametric clock and arbitrarily many rational-valued parameters [Miller, 2000]
- ✓ 2 parametric clocks and 1 integer-valued parameter [Bundala and Ouaknine, 2014]

# L/U-PTAs

## Definition

A lower/upper bound PTA (L/U-PTA) is a PTA in which each parameter  $p$  is always compared with clocks as an **upper bound** or always as a **lower bound**.



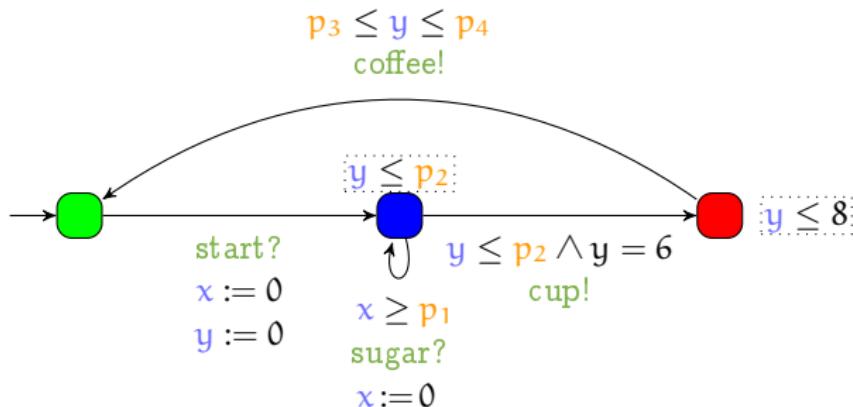
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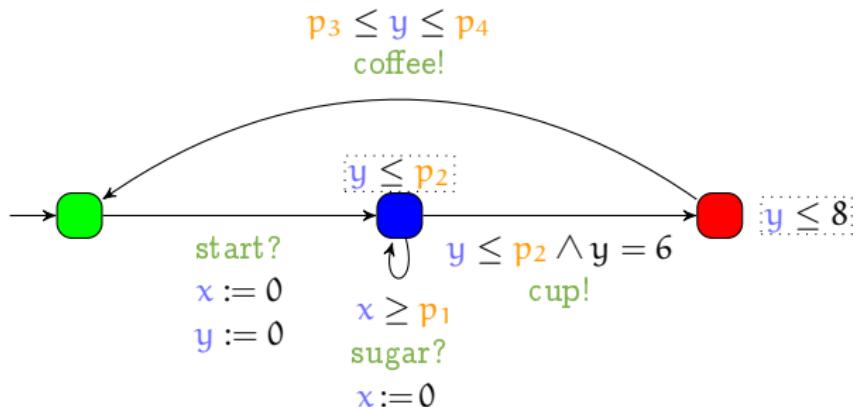
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Lower-bound parameters:  $p_1, p_3$

Upped-bound parameters:  $p_2, p_4$

# Decidable problems for L/U-PTA

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“Does there exist a parameter valuation for which a given location  $l$  is reachable?”

decidable

[Hune et al., 2002]

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## ■ EF-finiteness problem

“Is the set of parameter valuations allowing to reach a given location  $l$  finite? ”

decidable (for integer valuations)

[Bozzelli and La Torre, 2009]

# Undecidable problems for L/U-PTA

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# Outline: Modeling and verifying real-time systems with parameters

- 1 Finite-state automata
- 2 Timed automata
- 3 Parametric timed automata
- 4 Modeling and verifying real-time systems with parameters
  - Real-time systems
  - Modeling real-time systems under uncertainty
  - Verification
  - IMITATOR in a nutshell
- 5 A case study: Verifying a real-time system under uncertainty

## Context: Hard real-time embedded systems

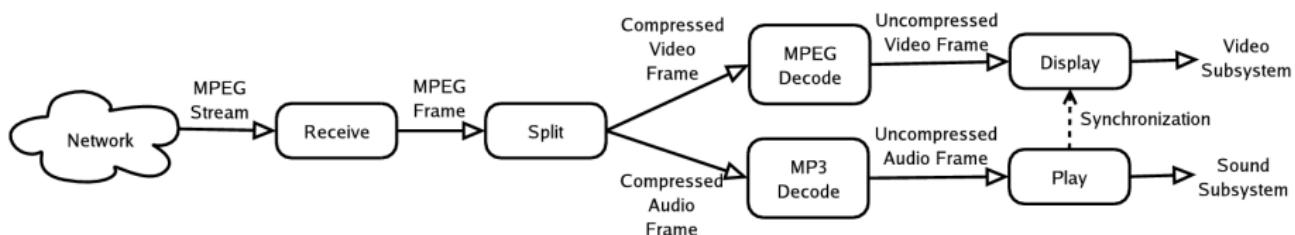
- Modern hard real-time embedded systems are **distributed** in nature
- Many of them have **critical timing requirements**:
  - **automotive systems** (modern cars have 10-20 embedded boards connected by one or more CAN bus)
  - **avionics systems** (several distributed control boards connected by one or more dedicated networks)



- To analyze the schedulability of such systems, it is very important to estimate the **(worst-case) computation times** of the tasks
- **Estimating WCET** is very difficult in modern architectures

# Real-time pipelines

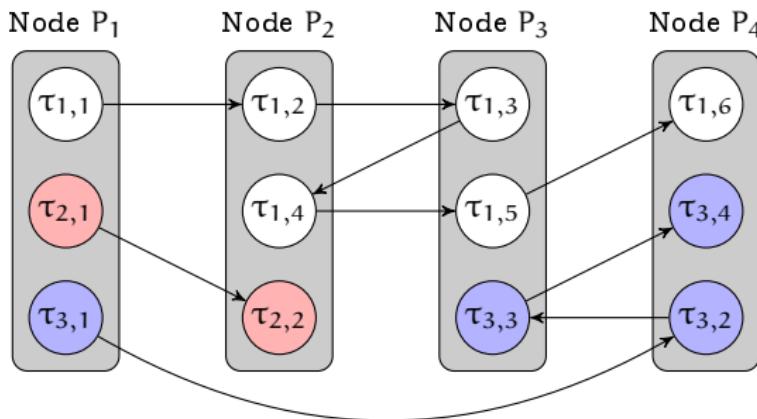
- Many real-time applications can be modeled as **pipelines** (also called **transactions**) of tasks



- Executed on a distributed (or multicore) system
- Activated cyclically (periodic or sporadic)
- Using preemption
  - Lower-priority tasks can be temporarily interrupted by a higher-priority task

# Model

- A set of pipelines  $\{\mathcal{P}^{(1)}, \dots, \mathcal{P}^{(p)}\}$  distributed over  $m$  nodes
- Each pipeline  $\mathcal{P}^{(i)}$  is a chain of  $n_i$  tasks  $\{\tau_{i,1}, \dots, \tau_{i,n_i}\}$
- Pipeline  $\mathcal{P}^{(i)}$  has an end-to-end (E2E) deadline  $D_i$  and period  $T_i$

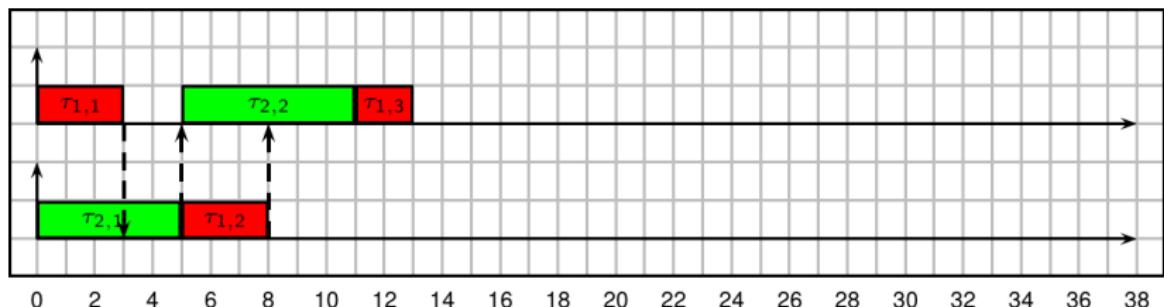
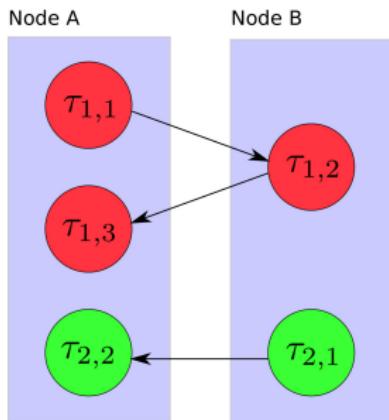


- Scheduling Problem: Guarantee that all pipelines complete before their E2E deadlines

# Activations, jitter, deadline

## ■ An example

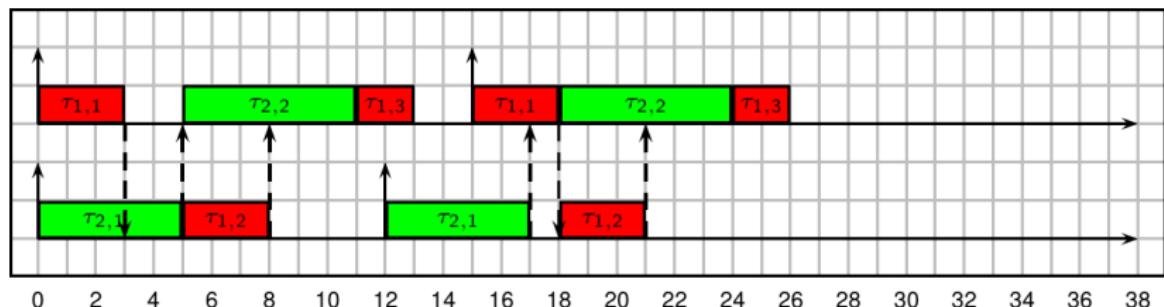
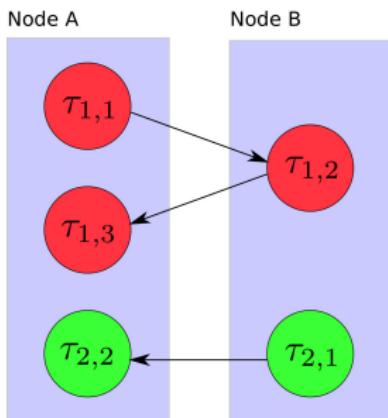
Task	Per.	E2E	Comp.	Resp.	Jitter	prio
$\tau_{1,1}$	15		3	3	0	HI
$\tau_{1,2}$	-		3	8	0-2	LO
$\tau_{1,3}$	-	15	2	13	3	LO
$\tau_{2,1}$	12		5	6	0	HI
$\tau_{2,2}$	-	12	6	?	0-1	ME



# Activations, jitter, deadline

## ■ An example

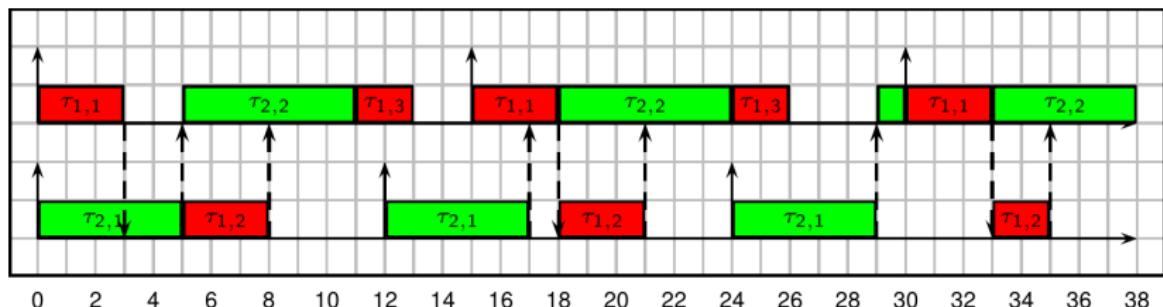
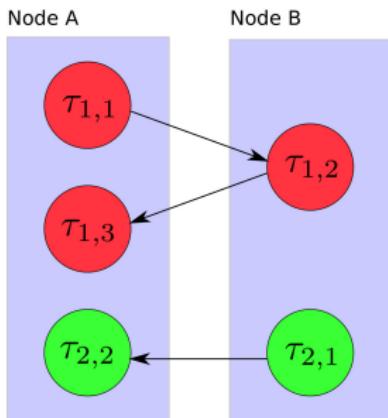
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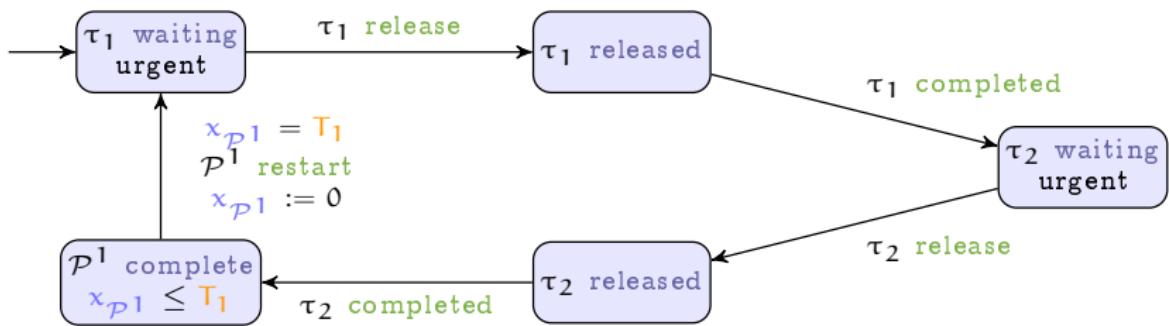
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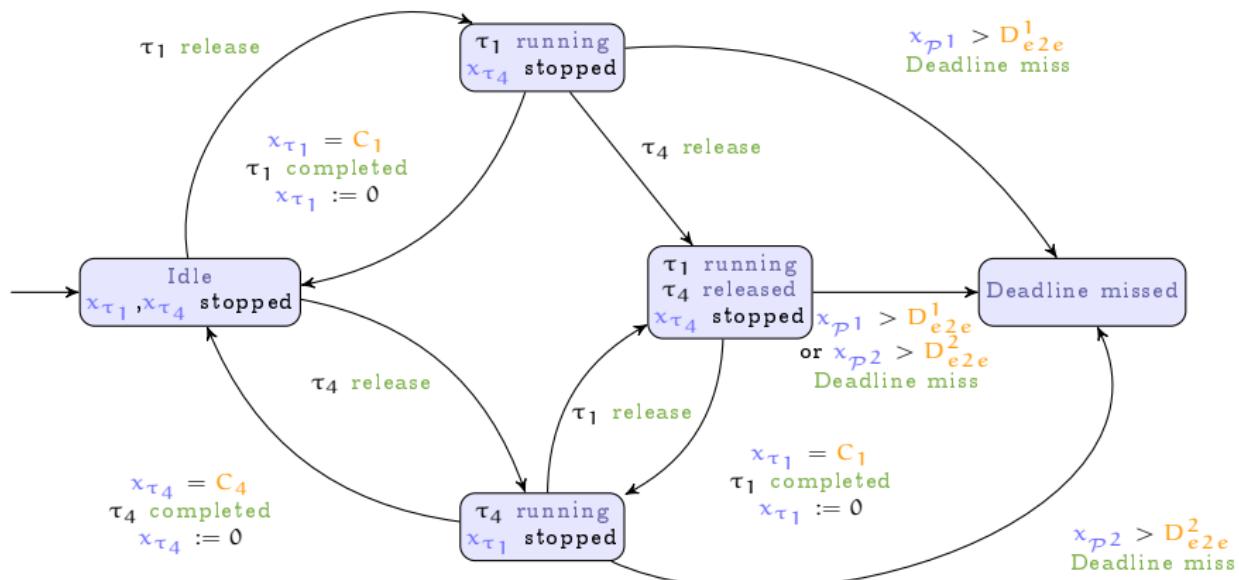
# Enriching the model with parameters

- A task is identified by three parameters:
  - $C_i$  is the **worst-case computation time** (or worst-case transmission time, in case it models a message)
  - $R_i$  is the **task worst-case response time**, i.e., the worst case finishing time of any task instance relative to the activation of its pipeline.
  - $J_i$  is the task **worst-case activation jitter**, i.e., the greatest time since its activation that a task must wait for all preceding tasks to complete their execution
- A parameter of major interest is the **computation time**

# Modeling a task / pipeline



# Modeling the fixed priority scheduler (preemptive)



Actually a PTA extended with **stopwatches** [Sun et al., 2013]

an extension of stopwatch automata [Adbeddaïm and Maler, 2002]

# Parametric verification of real-time systems

Many problems can be reduced to parametric reachability (EFsynth):  
find parameter valuations for which a given state is (un)reachable

- ⌚ This problem is undecidable for PTAs and many subclasses

[A., STTT 2017]

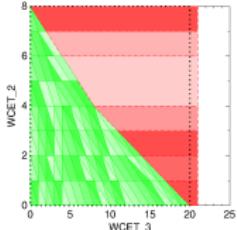
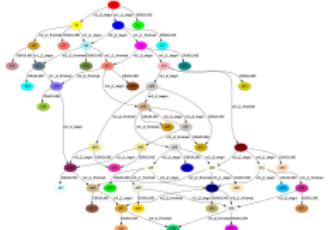
- ⌚ But we can still compute part (and often all) of the solution

Interesting problems:

- Find parameter valuations for which no deadline violation occurs (i. e., for which the system is **schedulable**)
- Compute the worst-case computation time
- Find the parametric WCET when the jitter is unknown

# IMITATOR

- A tool for modeling and verifying **real-time systems** with unknown constants modeled with **parametric timed automata**
  - Communication through (strong) broadcast synchronization
  - Rational-valued shared discrete variables
  - **Stopwatches**, to model schedulability problems with preemption
  
- Verification
  - Computation of the symbolic state space
  - (non-Zeno) parametric model checking (using a subset of **TCTL**)
  - Language and trace preservation, and robustness analysis
  - Parametric deadlock-freeness checking
  - Behavioral cartography



# IMITATOR

Under continuous development since 2008

[André et al., 2012]

A library of benchmarks

- Communication protocols
- Schedulability problems
- Asynchronous circuits
- ... and more

Free and open source software: Available under the GNU-GPL license



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Try it!

[www.imitator.fr](http://www.imitator.fr)

## Some success stories

- Modeled and verified an asynchronous memory circuit by ST-Microelectronics
  - Project ANR Valmem
- Parametric schedulability analysis of a prospective architecture for the flight control system of the next generation of spacecrafts designed at ASTRIUM Space Transportation [Fribourg et al., 2012]
- Formal timing analysis of music scores [Fanchon and Jacquemard, 2013]
- Solution to a challenge related to a distributed video processing system by Thales

# Outline

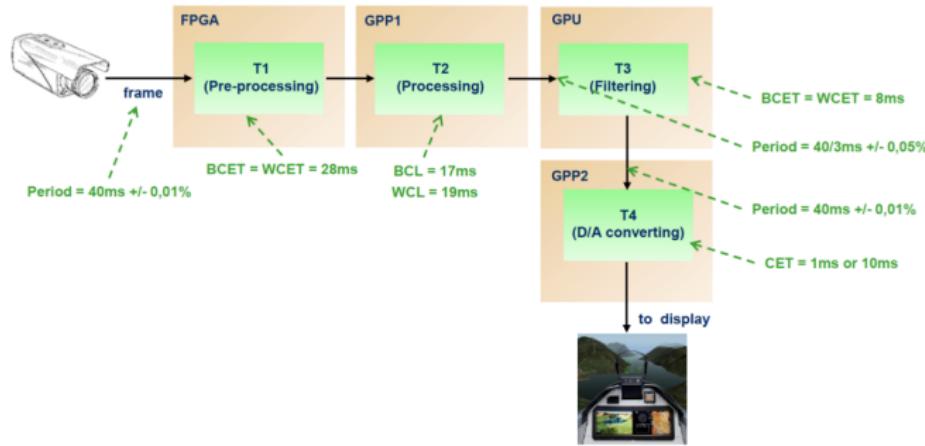
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- 5 A case study: Verifying a real-time system under uncertainty
- 6 Conclusion and perspectives

# The FMTV 2015 Challenge (1/2)

Challenge by Thales proposed during the WATERS 2014 workshop  
Solutions presented at WATERS 2015

System: an unmanned aerial video system with **uncertain periods**

- Period constant but with a small uncertainty (typically 0.01 %)
- Not a jitter!



# The FMTV 2015 Challenge (2/2)

## Goal

Compute the end-to-end BCET and WCET times for a buffer size of  $n = 1$  and  $n = 3$

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⌚ Not a typical parameter synthesis problem?

- No parameters in the specification

😊 A typical parameter synthesis problem

- The end-to-end time can be set as a **parameter**... to be synthesized
- The uncertain period is typically a **parameter** (with some constraint, e. g.,  $P1 \in [40 - 0.004, 40 + 0.004]$ )

# Methodology

- 1 Propose a PTA model with **parameters** for uncertain periods and the end-to-end time

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Note: not eliminating parameters allows one to know for **which values of the periods** the best / worst case execution times are obtained.

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- 6 Exhibit the minimum and the maximum

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# To build the PTA model

- Uncertainties in the system:

- $P1 \in [40 - 0.004, 40 + 0.004]$
- $P3 \in [\frac{40}{3} - \frac{1}{150}, \frac{40}{3} + \frac{1}{150}]$
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- Parameters:
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- The end-to-end latency (another parameter):  $E2E$
- Others:
  - the register between task 2 and task 3: discrete variable  $reg_{2,3}$
  - the buffer between task 3 and task 4:  $n = 1$  or  $n = 3$

# Simplification

- T1 and T2 are synchronised; T1, T3 and T4 are asynchronised
  - (exact modeling of the system behaviour is too heavy)

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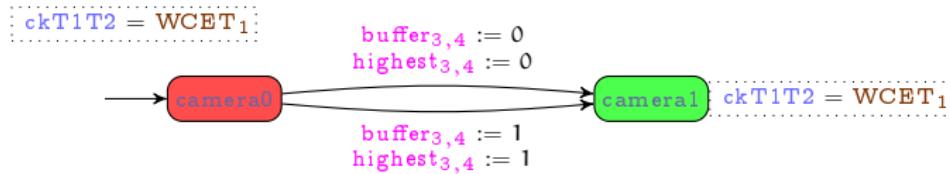
- T1 and T2 are synchronised; T1, T3 and T4 are asynchronised
  - (exact modeling of the system behaviour is too heavy)
- We choose a single arbitrary frame, called the **target** one
- We assume the system is initially in an arbitrary status
  - This is our only uncertain assumption (in other words, can the periods deviate from each other so as to yield any arbitrary deviation?)

# The initialization automaton

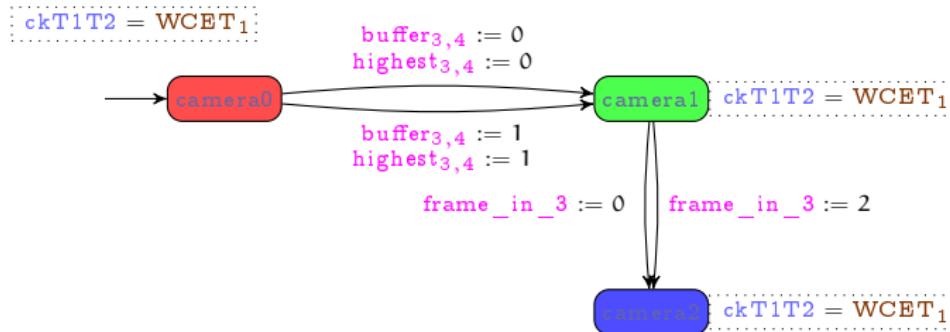
$\text{ckT1T2} = \text{WCET}_1$



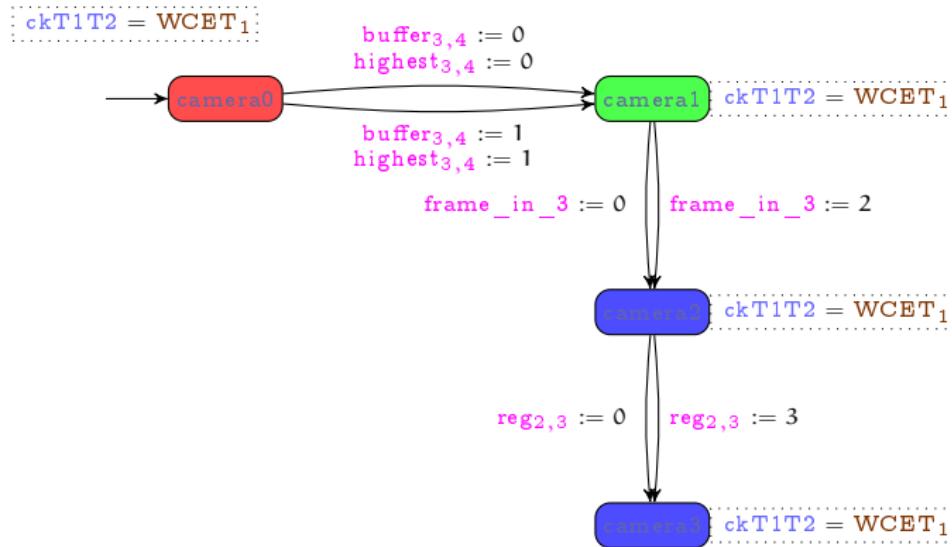
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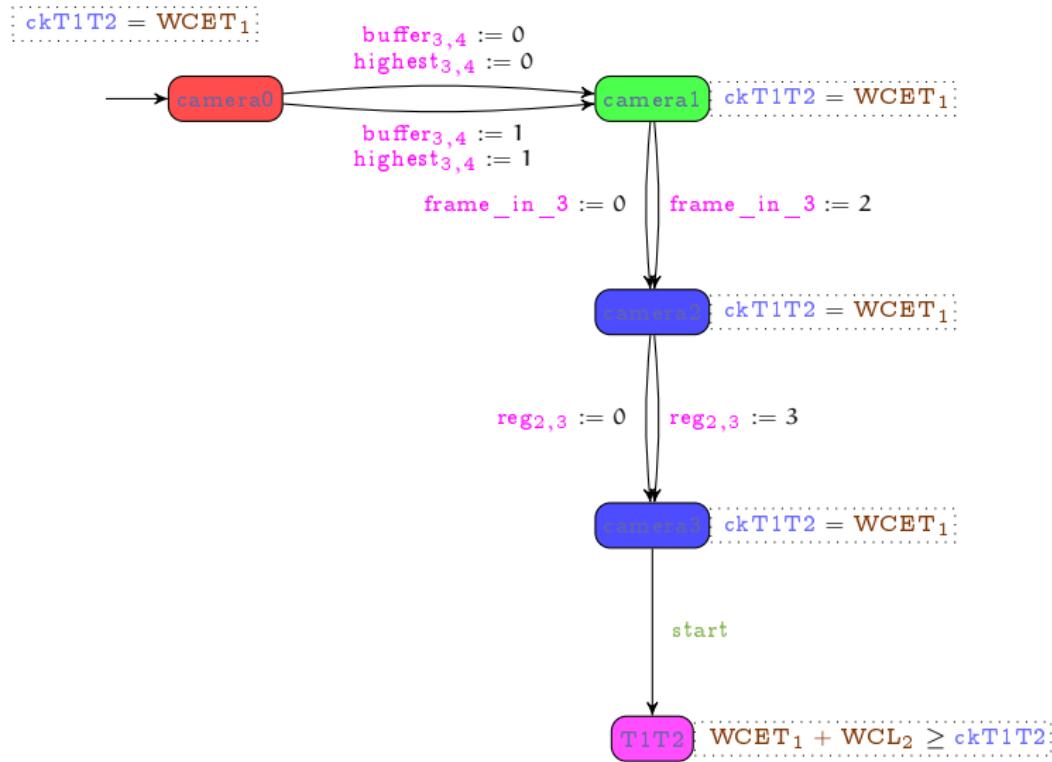
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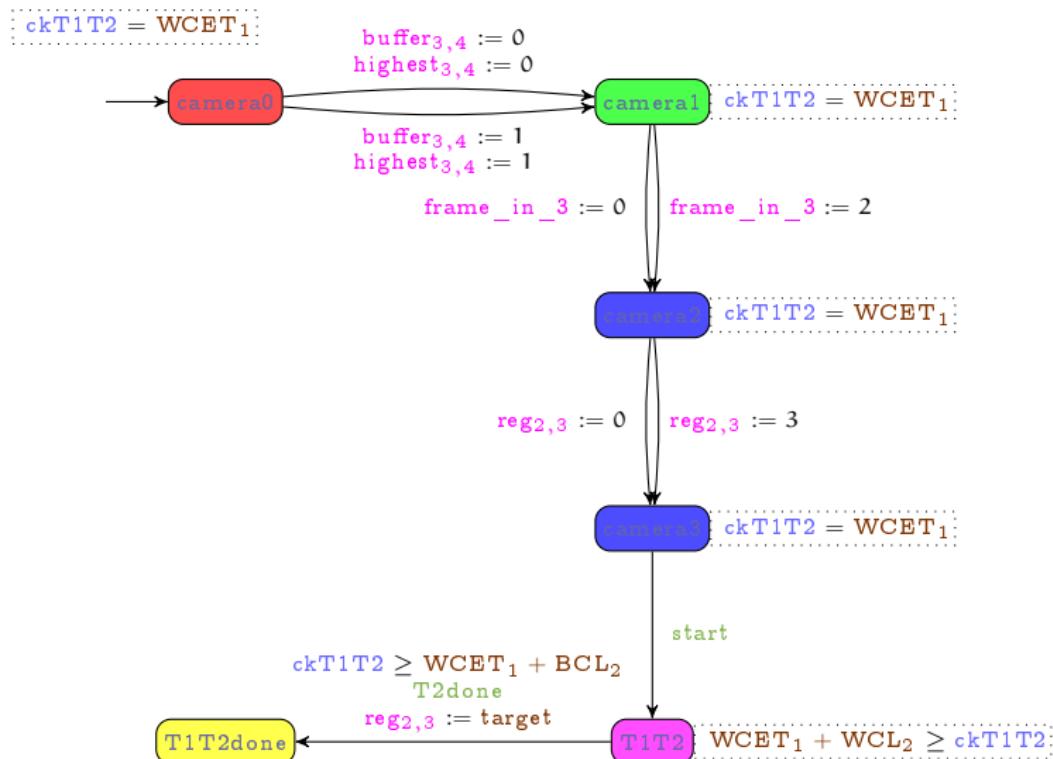
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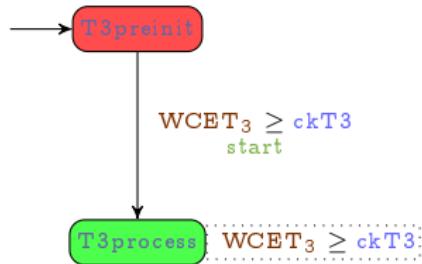
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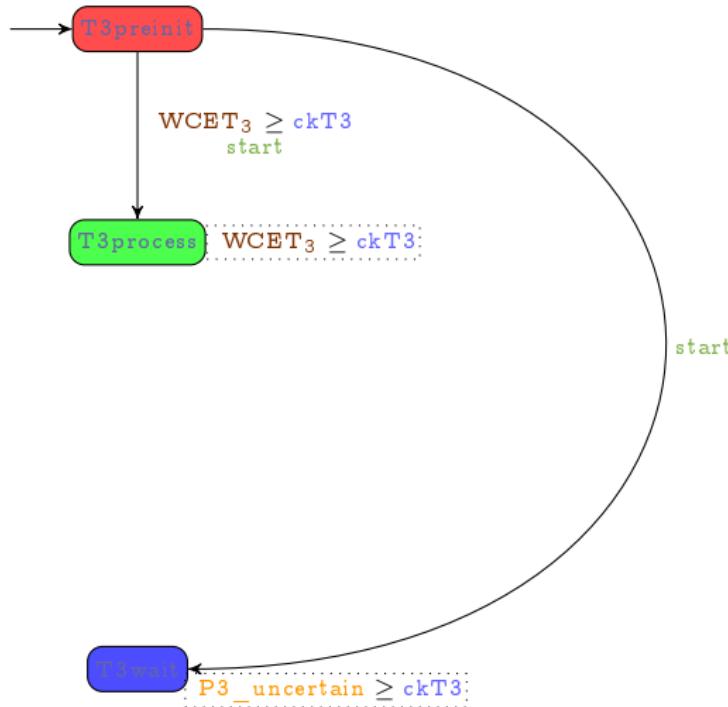
# Task T3



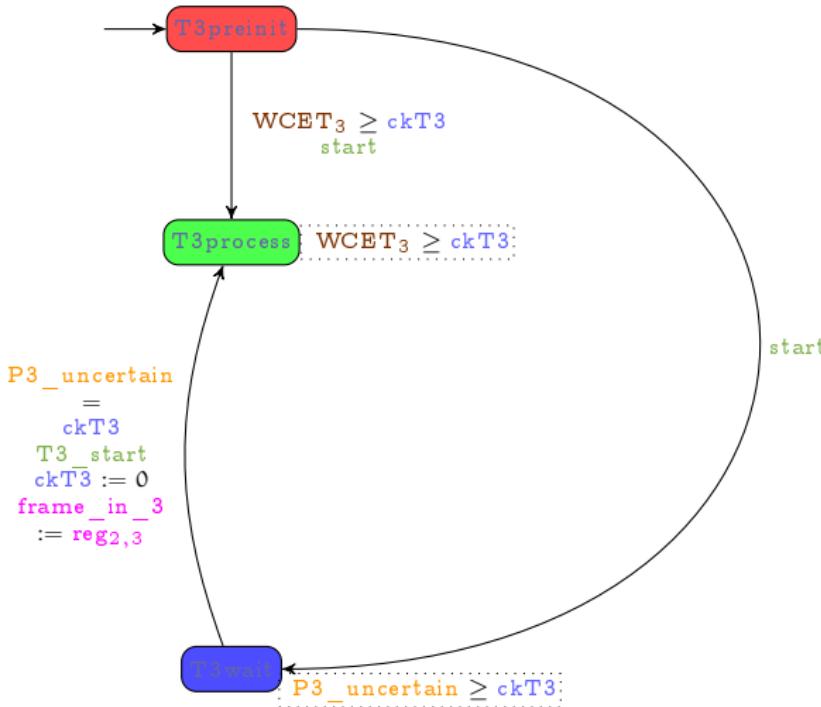
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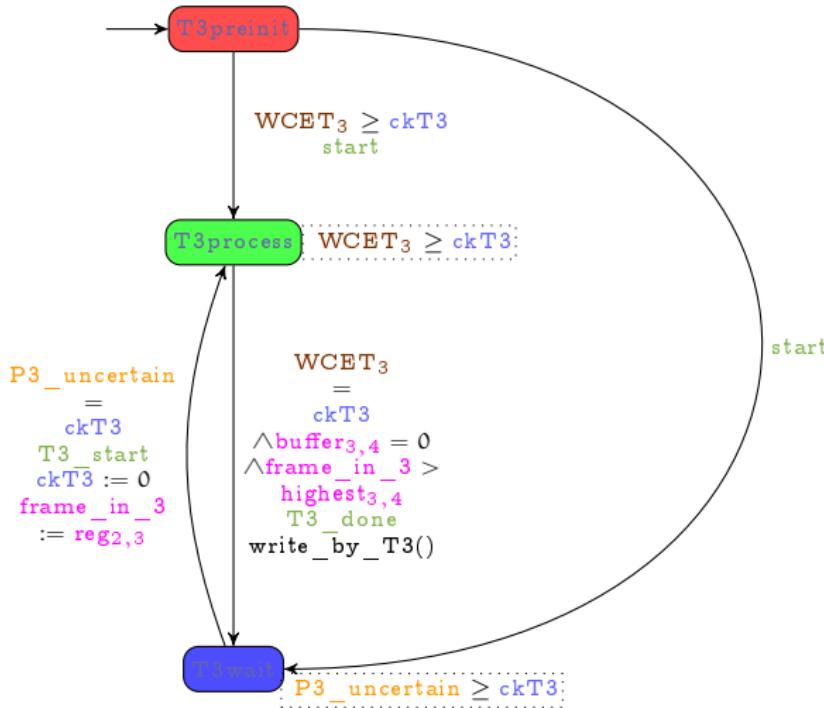
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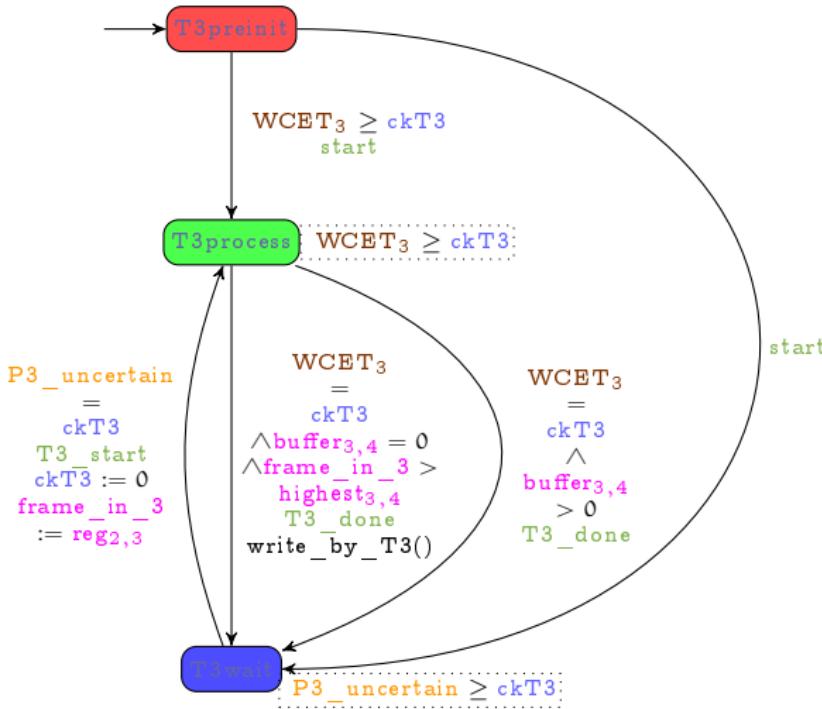
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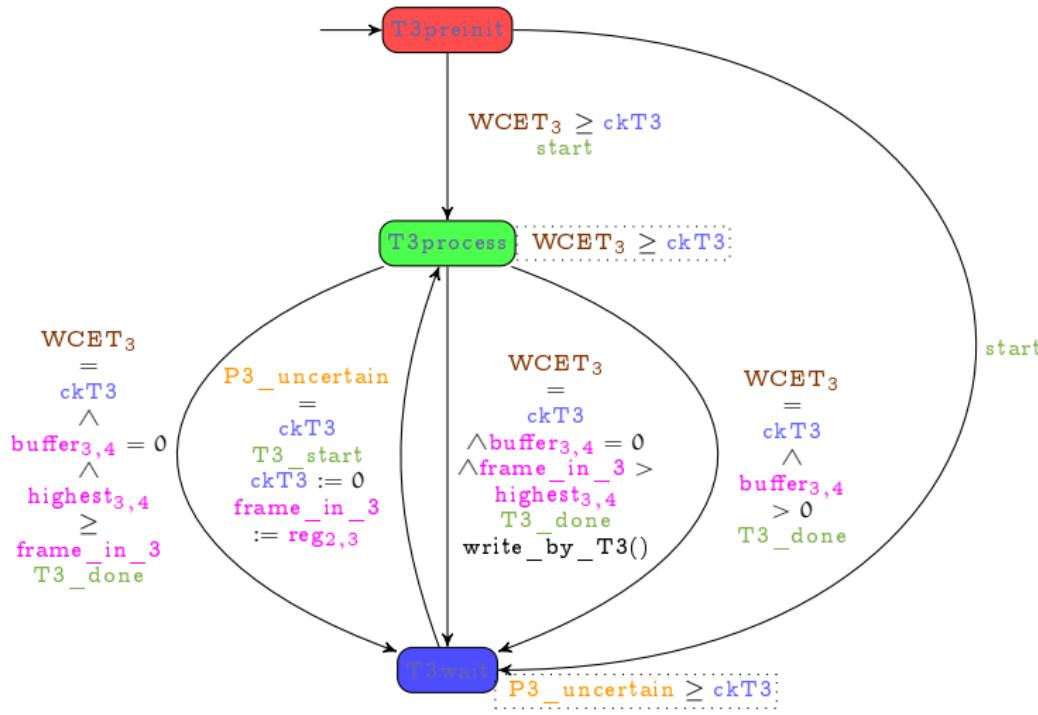
## Task T3



## Task T3



## Task T3



# Task T4



P4\_uncertain  $\geq$  ckT4;

## Task T4

P4\_uncertain = ckT4  
   $\wedge$  buffer3,4 > 0  
    ckT4 := 0  
    read\_by\_T4()

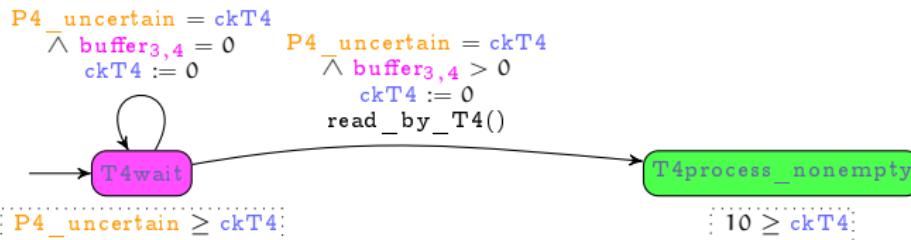
T4wait

T4process\_nonempty

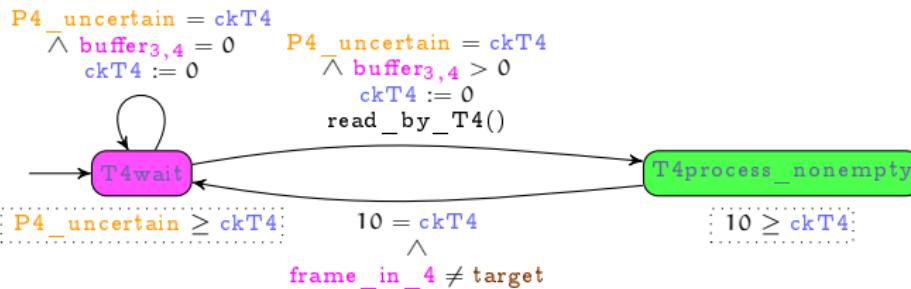
[ P4\_uncertain  $\geq$  ckT4 ]

[ 10  $\geq$  ckT4 ]

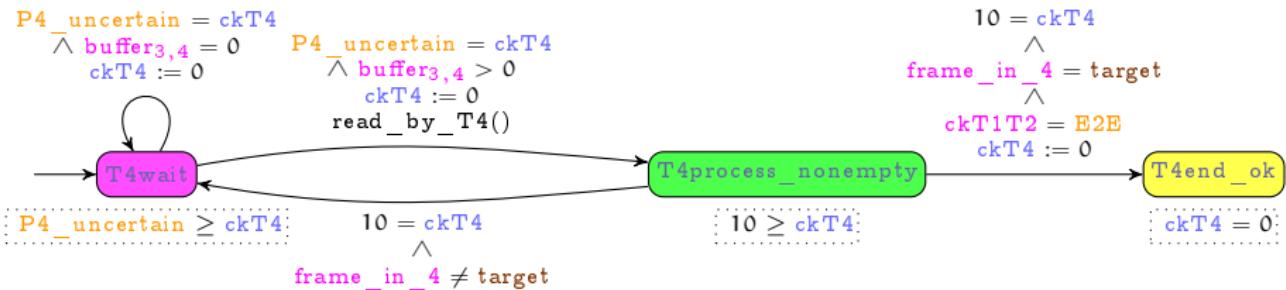
## Task T4



## Task T4



## Task T4



# Results

E2E latency results for  $n = 1$  and  $n = 3$

	$n = 1$	$n = 3$
min E2E	63 ms	63 ms
max E2E	145.008 ms	225.016 ms

Results obtained using MITATOR in a few seconds

# Outline

- 1 Finite-state automata
- 2 Timed automata
- 3 Parametric timed automata
- 4 Modeling and verifying real-time systems with parameters
- 5 A case study: Verifying a real-time system under uncertainty
- 6 Conclusion and perspectives

# Summary

## ■ Finite-state automata

- ☺ Mostly decidable results
- ☺ Efficient model checking algorithms
- ☹ Miss the quantitative aspects
- ☺ Many powerful tools

## ■ Timed automata

- ☺ Finite abstract semantics
- ☺ Some decidable results
- ☹ Some undecidable results
- ☺ Several powerful tools

## ■ Parametric timed automata

- ☺ Very expressive
- ☹ No finite abstract semantics
- ☹ Almost only undecidability results
- ☺ Some powerful tools

# Perspectives

Address harder problems

- Thales challenge: what is the **minimum time between two lost frames**? (due to the uncertain periods)
  - Requires to model check **thousands of frame processings**

Improve the efficiency of parameter synthesis techniques

- Promising heuristics: approximations using the integer hull  
[Jovanović et al., 2015, André et al., 2015]
- Distributed parameter synthesis
  - Multi-core synthesis [Laarman et al., 2013]
  - Distributed synthesis based on locations [Zhang et al., 2016]

# Beyond (parametric) timed automata

## Beyond time...

- Cost, temperature, energy
  - Hybrid automata [Alur et al., 1993a, Alur et al., 1995]
    - Very expressive, but often undecidable
    - Some interesting software (including SpaceEx [Frehse et al., 2011])

## Probabilities

- Useful when a property cannot be proved with full certainty
  - Security
- Another way to model systems known with limited precision

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## Additional explanation

# Explanation for the 4 pictures in the beginning



Allusion to the Northeast blackout (USA, 2003)

Computer bug

Consequences: 11 fatalities, huge cost

(Picture actually from the Sandy Hurricane, 2012)



Error screen on the earliest versions of Macintosh



Allusion to the sinking of the Sleipner A offshore platform (Norway, 1991)

No fatalities

Computer bug: inaccurate finite element analysis modeling

(Picture actually from the Deepwater Horizon Offshore Drilling Platform)



Allusion to the MIM-104 Patriot Missile Failure (Iraq, 1991)

28 fatalities, hundreds of injured

Computer bug: software error (clock drift)

(Picture of an actual MIM-104 Patriot Missile, though not the one of 1991)

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